## Lecture 23: Ray Tracing

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#### CSC 259/459, Fall 2024 **Computer Imaging & Graphics**



### The Roadmap

#### **Theoretical Preliminaries**

#### Human Visual Systems

#### **Digital Camera Imaging**

### Modeling and Rendering



**3D Modeling** 

#### **Rasterization and GPU**

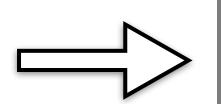
#### **Ray Tracing**

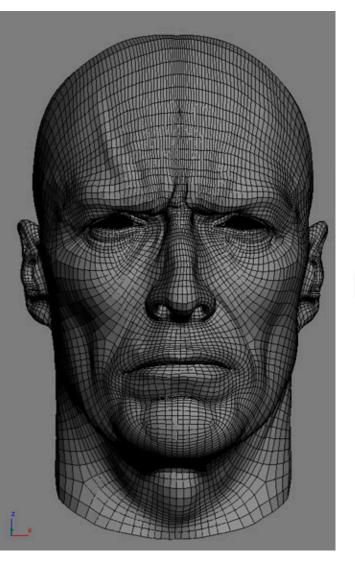
Shading Rendering in AR/VR

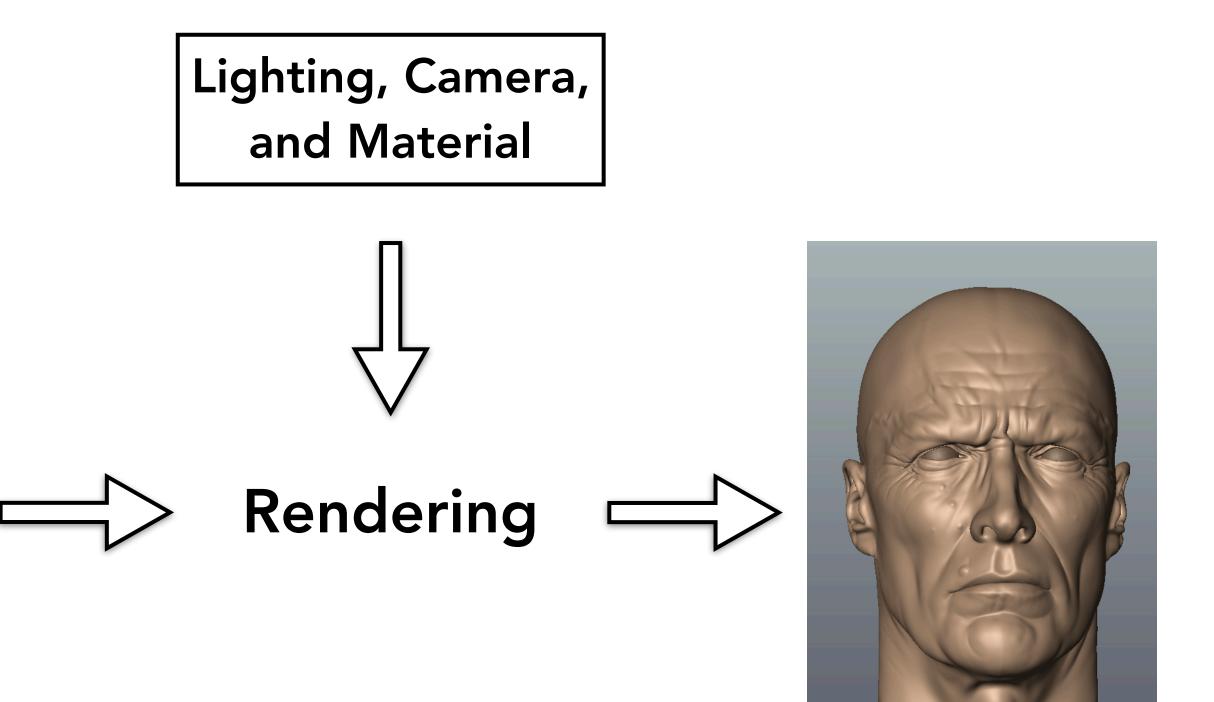


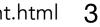
### Graphics







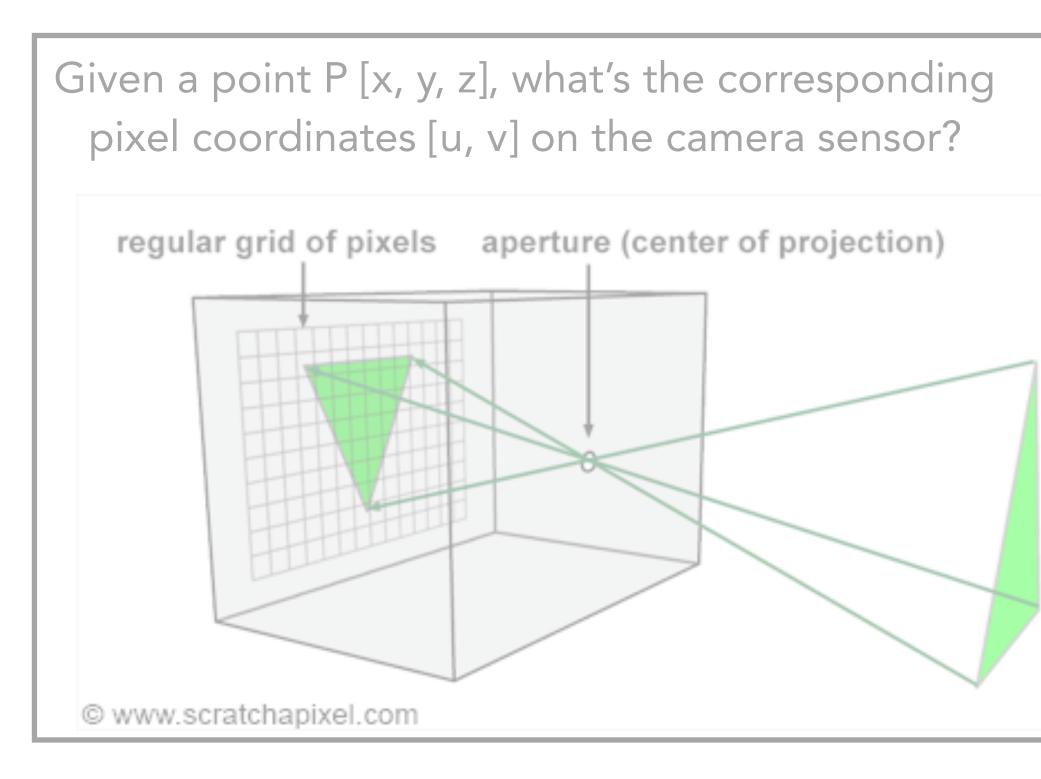


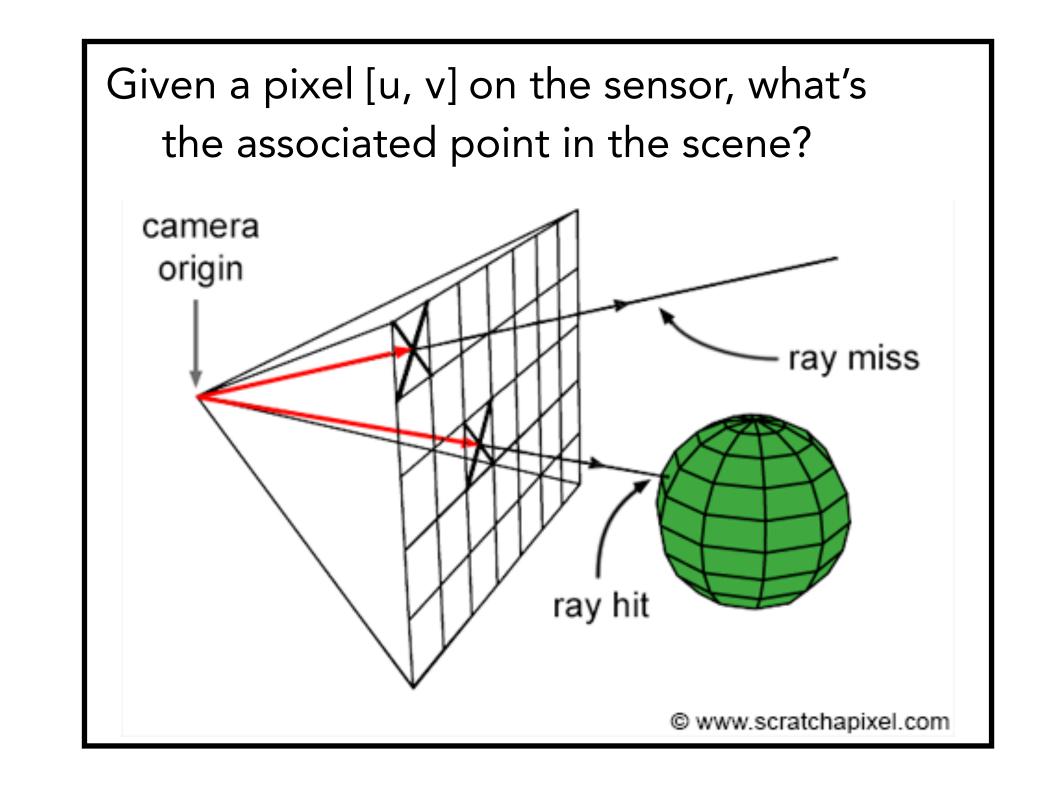


## **Visibility Problem**

### Two fundamental classes of visibility algorithms

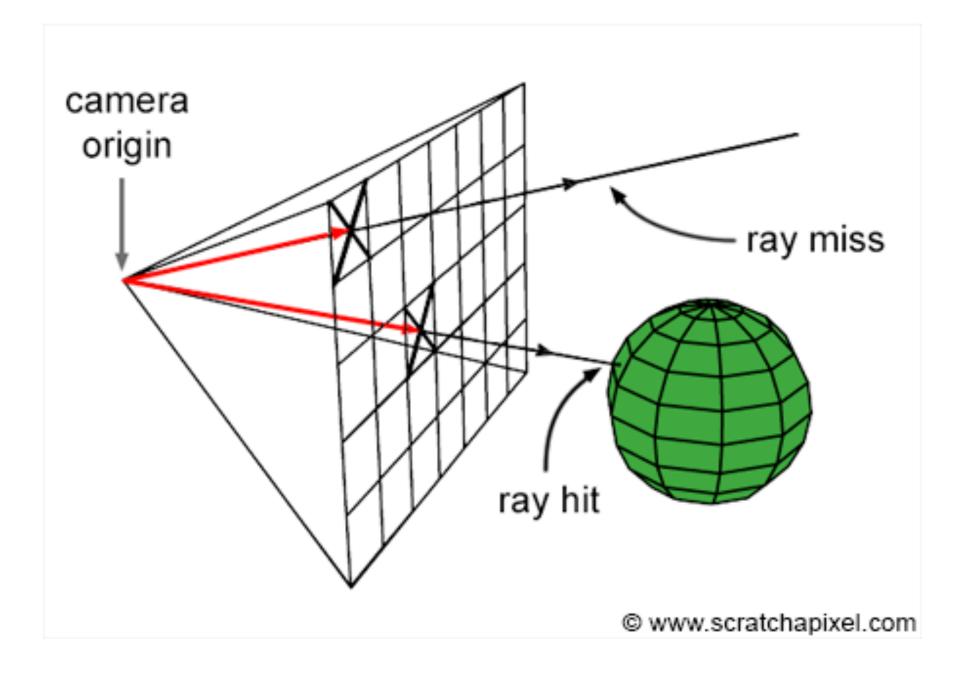
- Object-centric (Rasterization)
- Image-centric (Ray tracing)







### **Basic Idea of Ray Tracing**

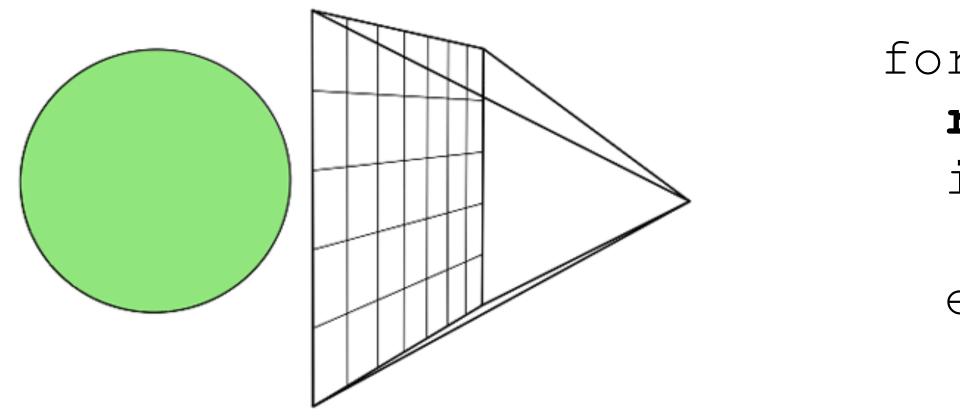


foreach pixel in image
 ray = buildRay(camera, pixel)
 if (P = intersect(ray, mesh))
 pixel.color = shade(P)
 else

pixel.color = backgroundColor



### **Basic Idea of Ray Tracing**



```
Can sample multiple rays
                               per pixel for anti-aliasing
foreach pixel in image
  ray = buildRay(camera, pixel) 
  if (P = intersect(ray, mesh))
    pixel.color = shade(P)
  else
    pixel.color = backgroundColor
```





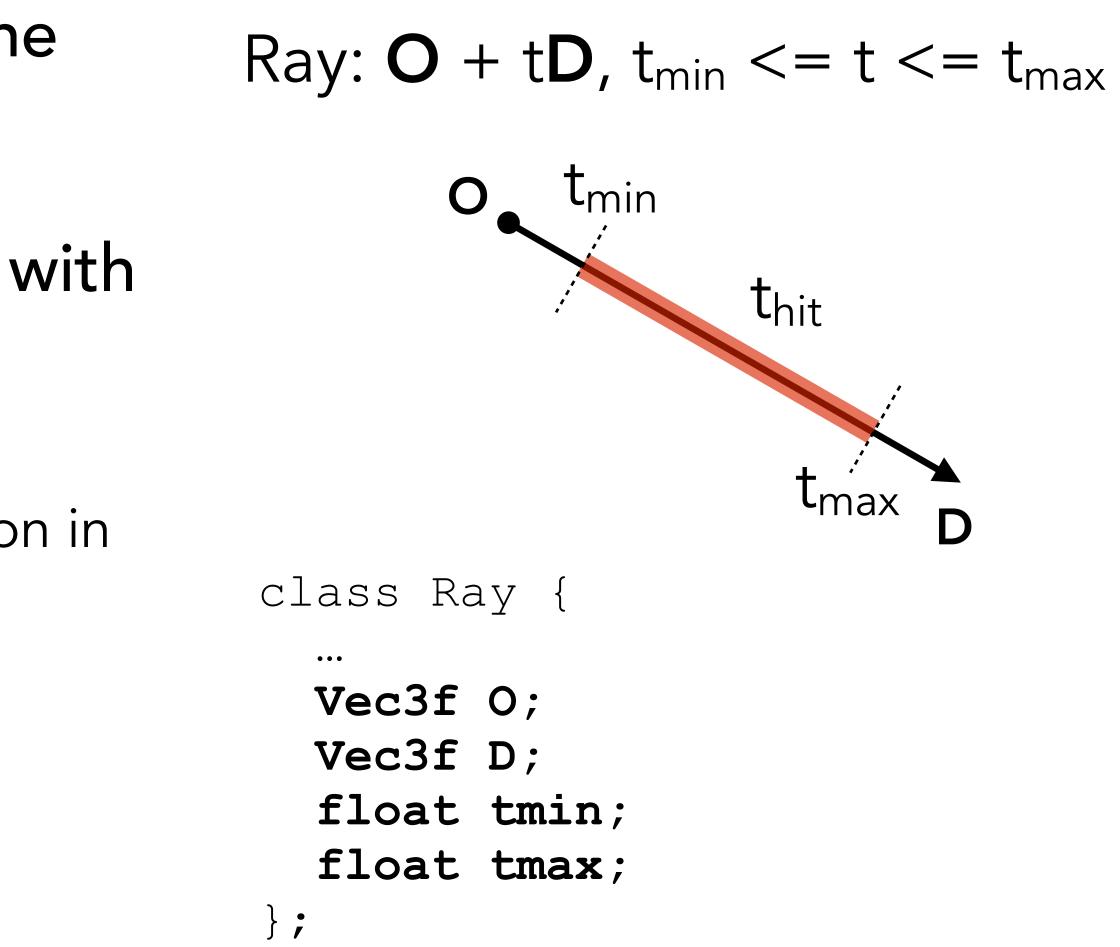
Generating Rays



### What Defines a Ray?

A ray is defined by its original and the directional vector.

- We usually define ray as a segment, with a min and a max.
  - Its purpose will become clear later, but briefly it allows us to reduce computation in visibility test.

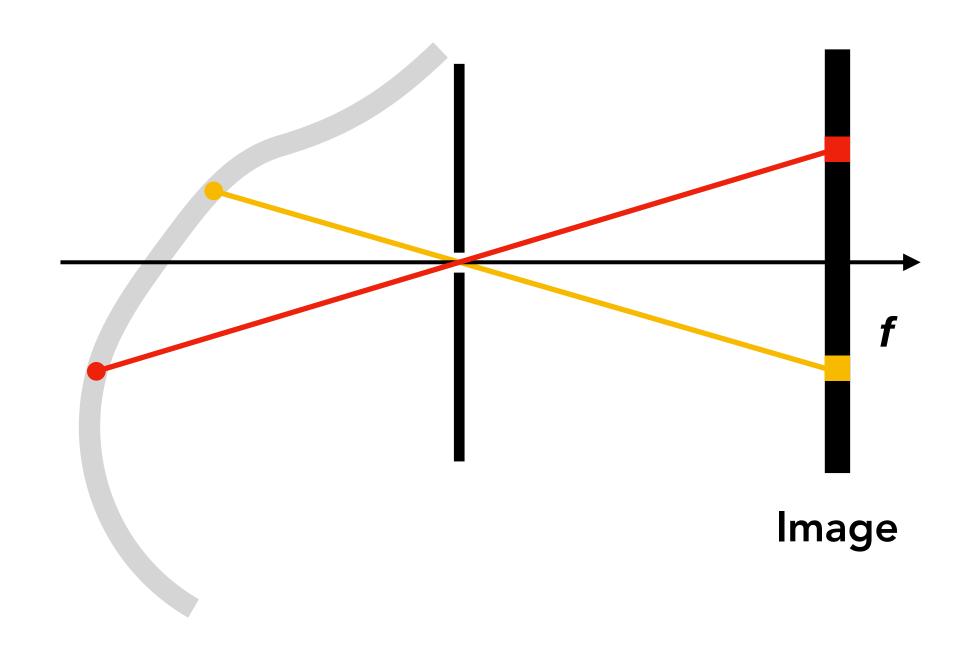


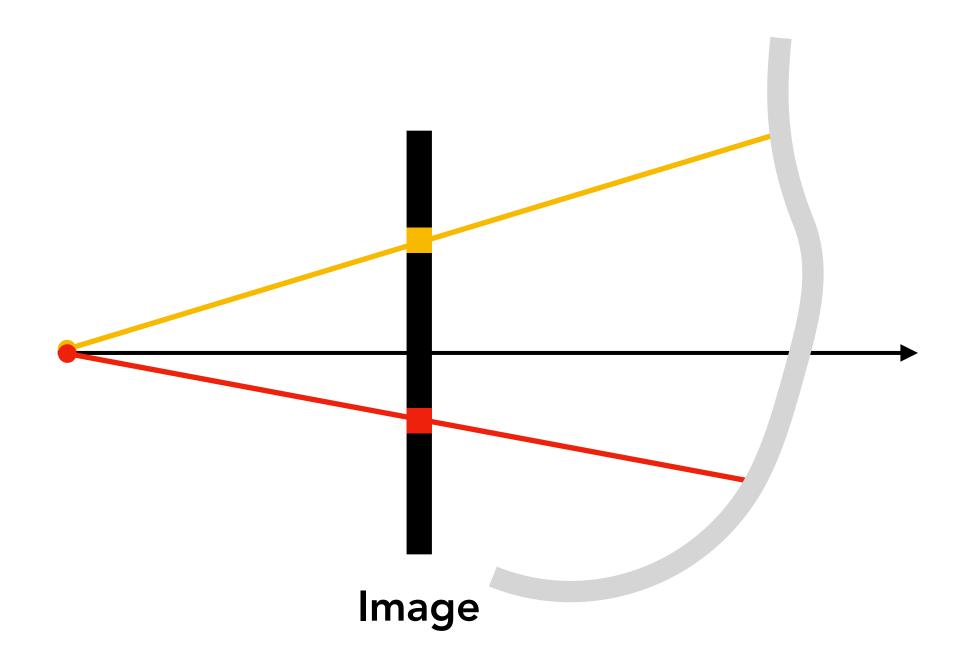


### Generating a Ray in a Pinhole Camera

Very intuitive: connect a pixel and the pinhole to form a ray.

Remember in actual implementations the canvas is before the pinhole.

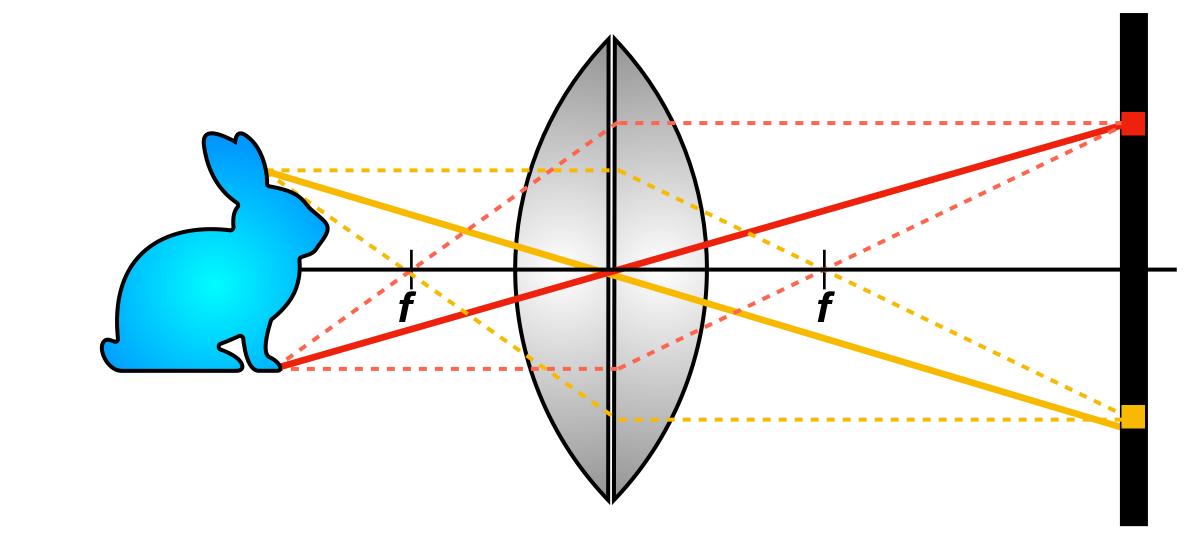






Many rays incident on one pixel. So for each pixel we need to sample the lens multiple times to trace **multiple rays**.

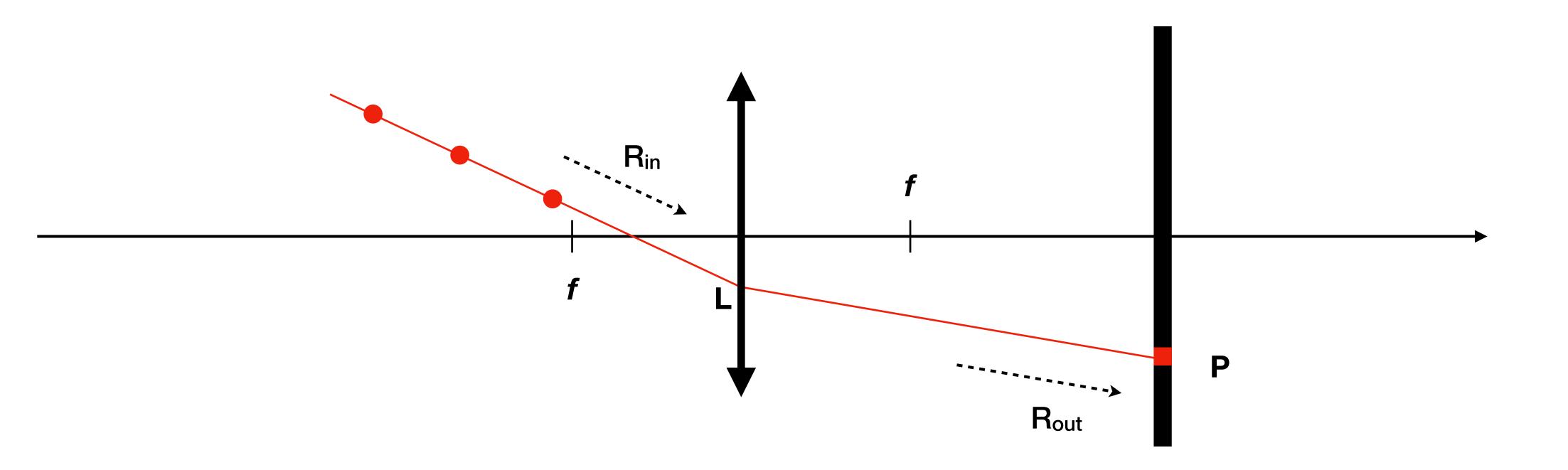
- Why trace many rays? Because the pixel color depends on all incident rays.
- This is not something achievable using only the perspective matrix.





#### Goal: given an arbitrary R<sub>out</sub> how do we find R<sub>in</sub>?

- There is a unique ray,  $R_{out}$ , between a pixel **P** and a sample **L** on the lens
- There is a unique ray,  $R_{in}$ , going into the lens that generates  $R_{out}$
- The closest point on  $R_{\text{in}}$  before the lens will hit  ${\boldsymbol{\mathsf{P}}}$

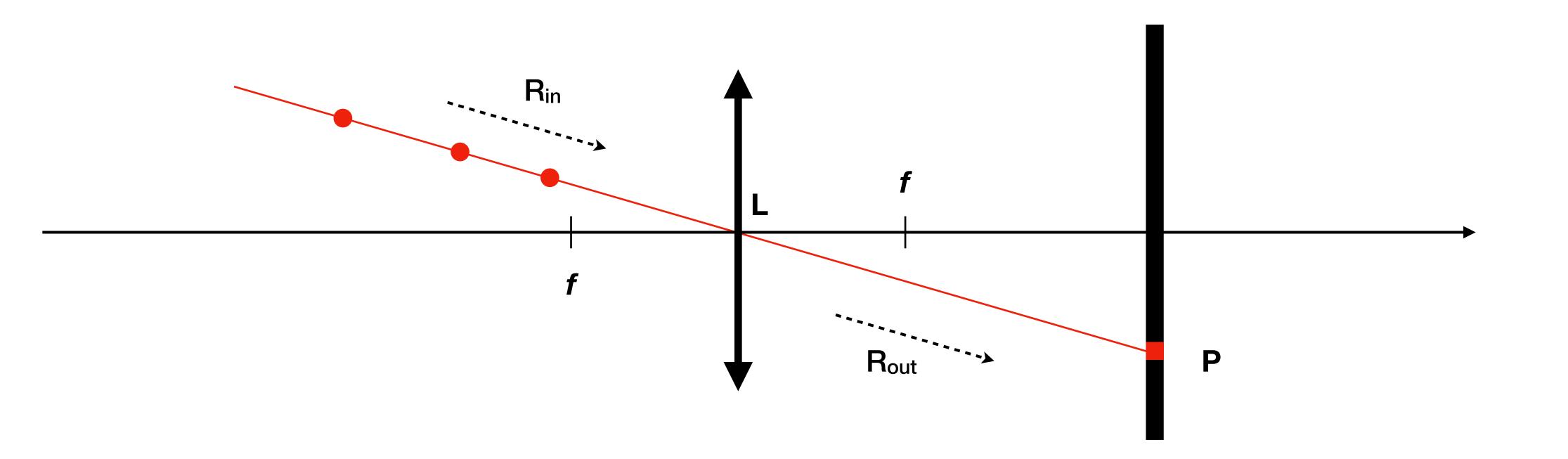


ixel **P** and a sample **L** on the lens e lens that generates R<sub>out</sub> will hit **P** 



11

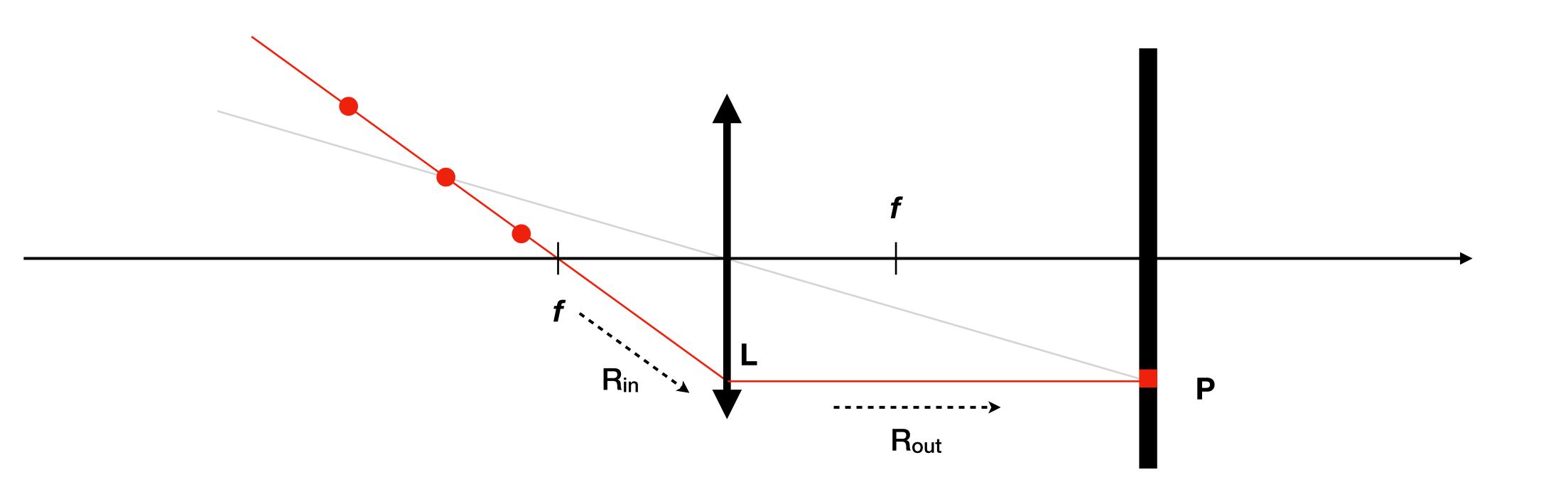
### Use geometrical optics principles to determine R<sub>in</sub> for a given R<sub>out</sub> • Rays go through the lens center (chief ray) don't change their directions





### Use geometrical optics principles to determine R<sub>in</sub> for a given R<sub>out</sub>

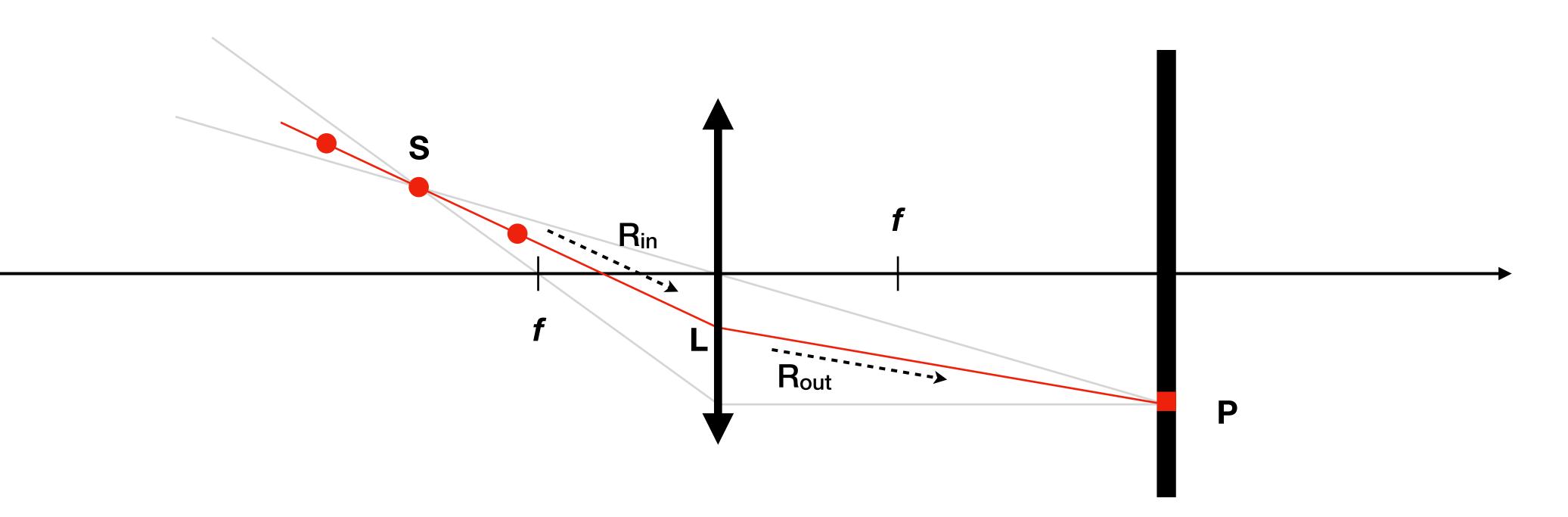
- Rays go through the lens center (chief ray) don't change their directions
- Rays parallel to the optical axis (parallel ray) pass through the lens focus





#### Steps:

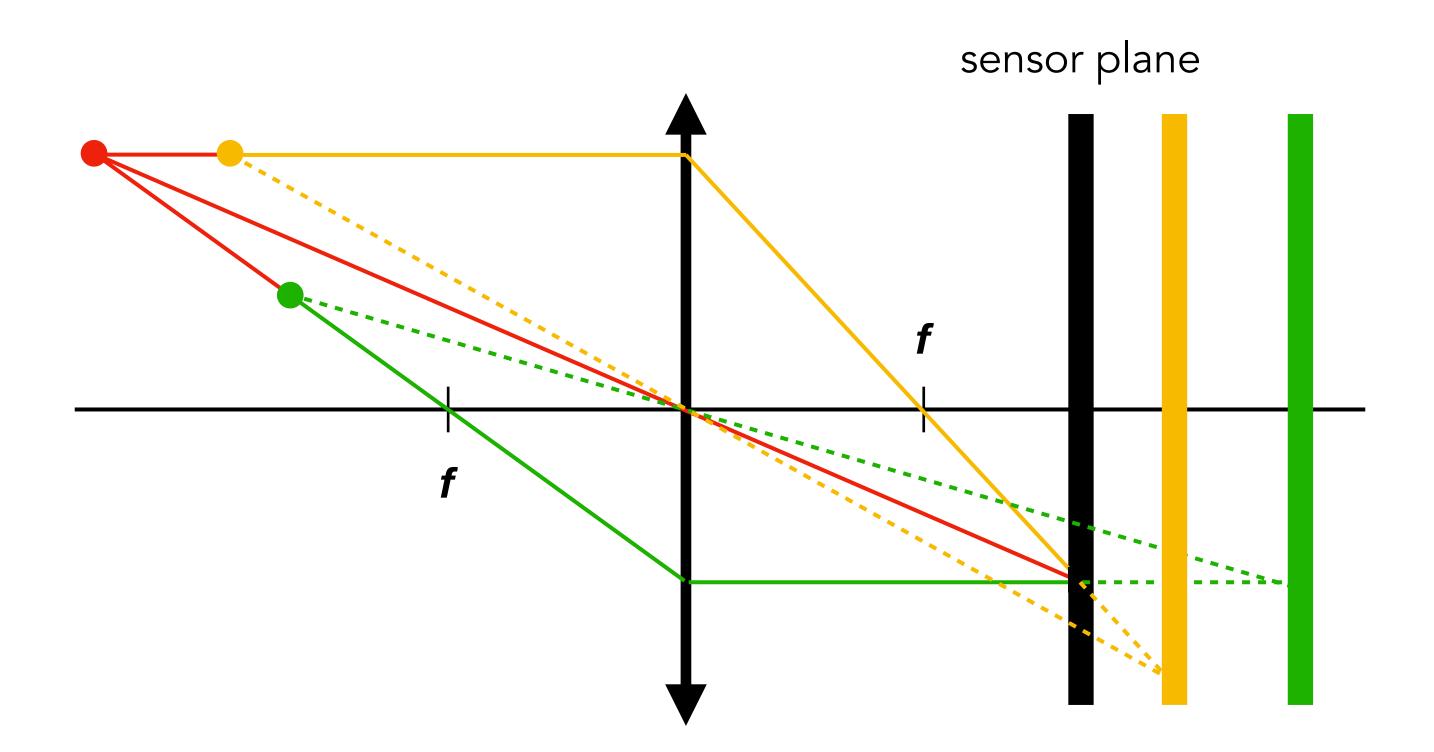
- 1. use chief and parallel rays to find the intersection point **S** in the scene
- 2. find L on the lens from R<sub>out</sub>
- 3. R<sub>in</sub> is the ray between **S** and **L**





### **Can Ray Tracing Capture DOF?**

focus on the pixel.



#### What's described before doesn't rely on whether the closest hit is actually in-

• So it can inherent trace scene points that are out-of-focus, i.e., simulate depth of field.



### Lens Sampling

### Each sensor plane point receives infinitely many rays, so we need to sample many rays for a point to reduce noise (more in shading lecture).

• This is orthogonal to sampling multiple points per pixel.



\* the artifacts from low sampling rate here is not aliasing; it's due to high variance in Monte Carlo integration.



http://www.pbr-book.org/3ed-2018/Camera\_Models/Projective\_Camera\_Models.html 16



**Ray-Scene Intersection** 

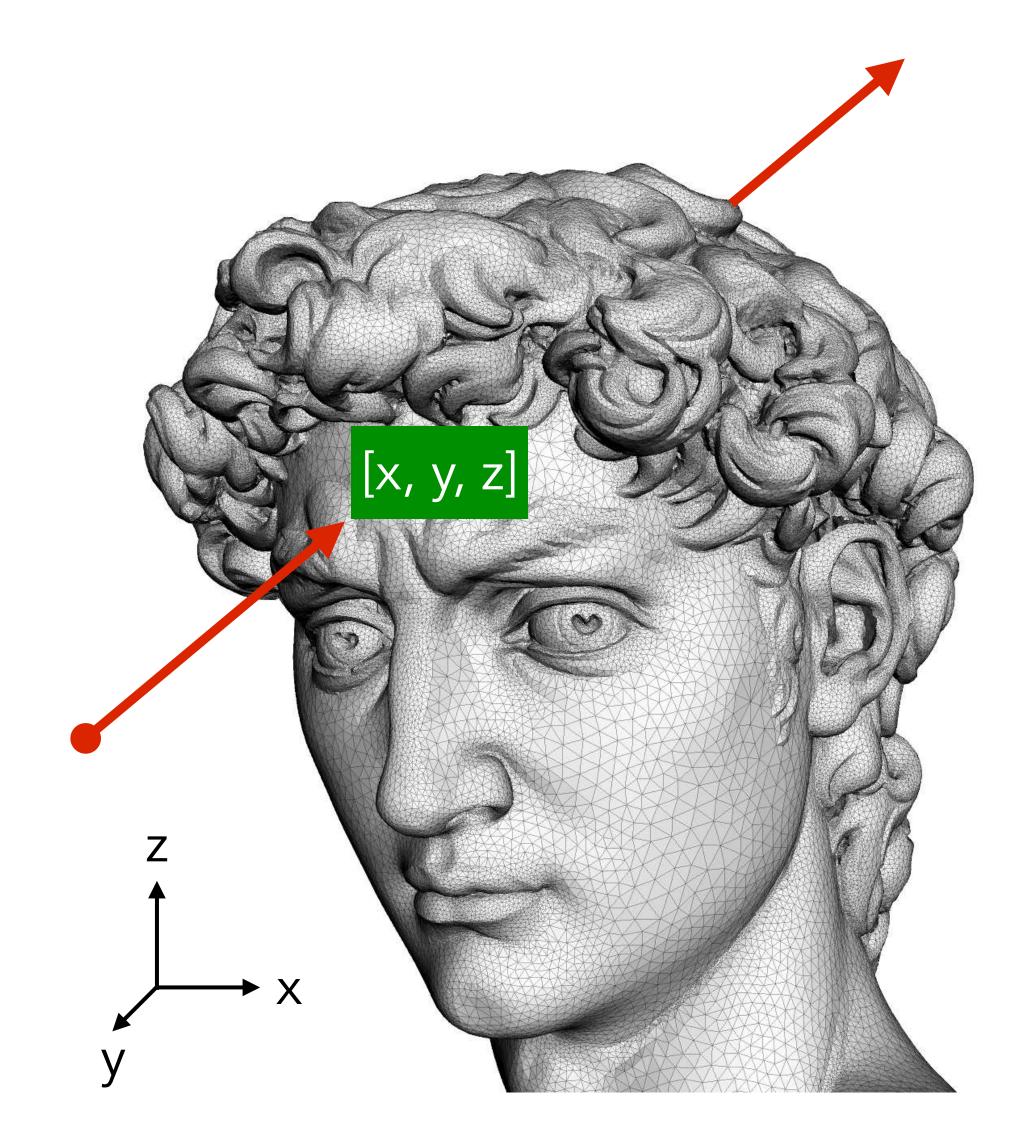


### **Ray-Scene Intersection**

Goal: calculate the [x, y, z] coordinates of the closest hit between the ray and the mesh.

### Why closest hit?

Preserve visibility (like the z-buffer in rasterization)



Valette, et al. [TVCG'08]



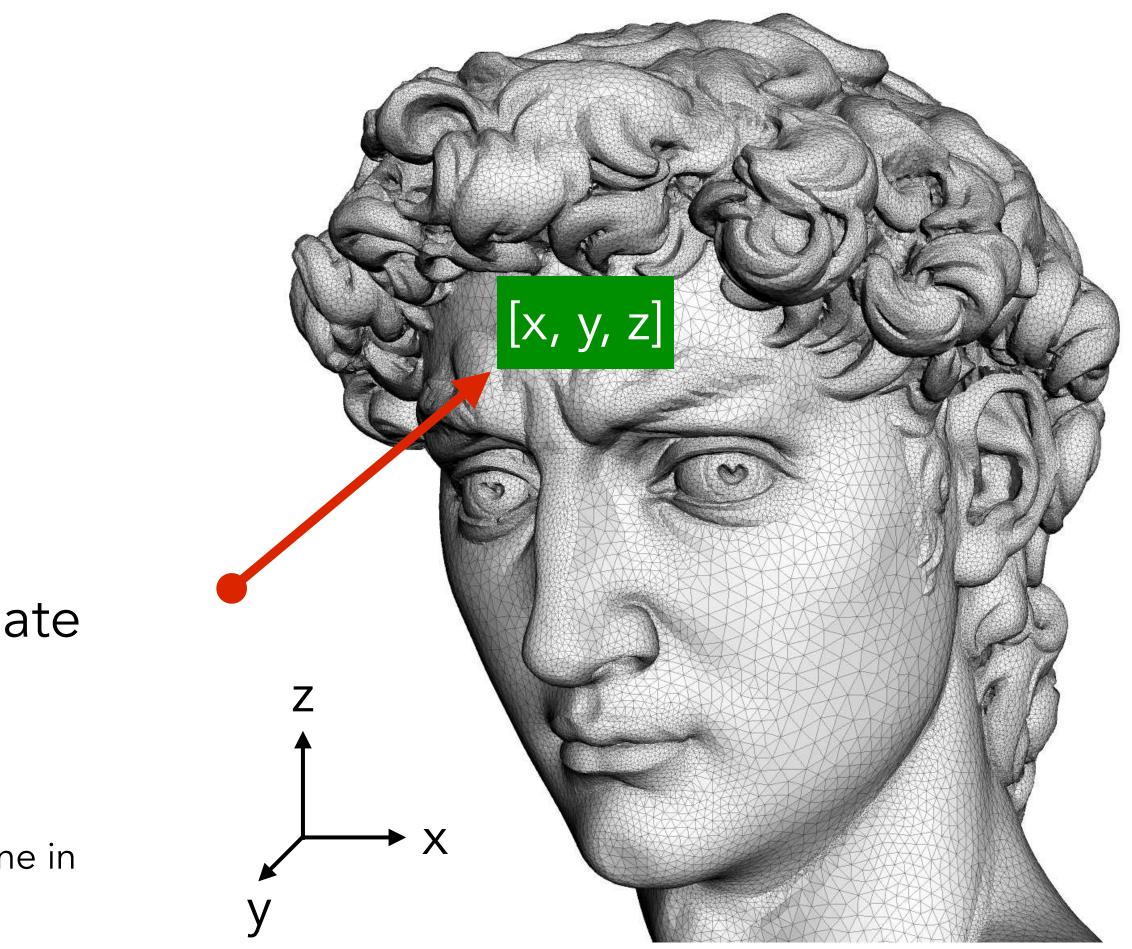
## The Simplest Algorithm

### Brute-force approach:

- iterate all triangles
- test intersection for each triangle
- return the closest hit, if any

#### Key task:

- Ray-triangle intersection test and calculate the coordinates of the hit point, if any.
- General plan:
  - Identify the intersection point between the ray and the plane in which the triangle lies
  - Test whether the intersection point is inside the triangle



Valette, et al. [TVCG'08]



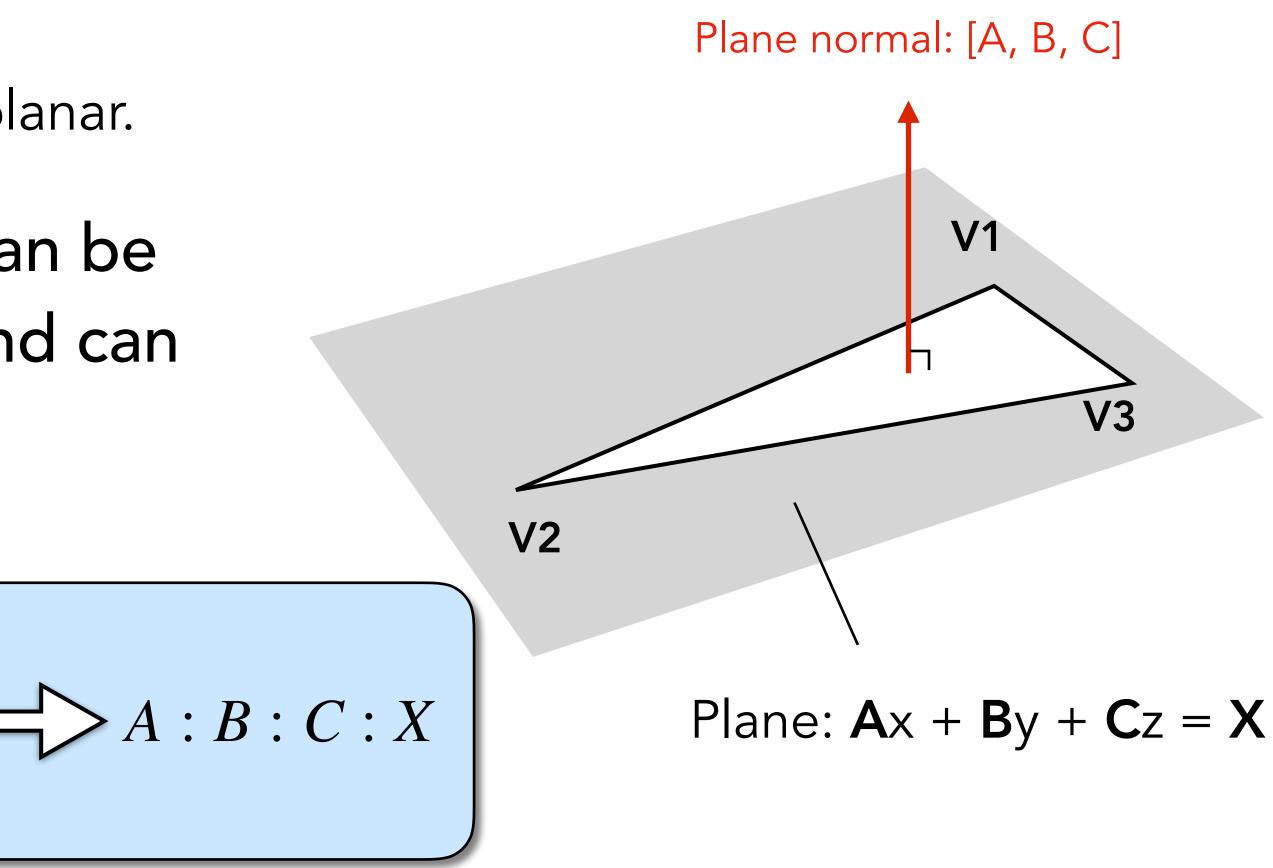
### What Defines a Triangle?

#### A plane with three vertices.

• The vertices are guaranteed to be co-planar.

The plane that the triangles are in can be expressed as an implicit equation and can be calculated from the vertices.

$$\begin{cases} A(V1_x - V2_x) + B(V1_y - V2_y) + C(V1_z - V2_z) = 0 \\ A(V1_x - V3_x) + B(V1_y - V3_y) + C(V1_z - V3_z) = 0 \\ A \times V1_x + B \times V1_y + C \times V1_z = X \end{cases} \square$$

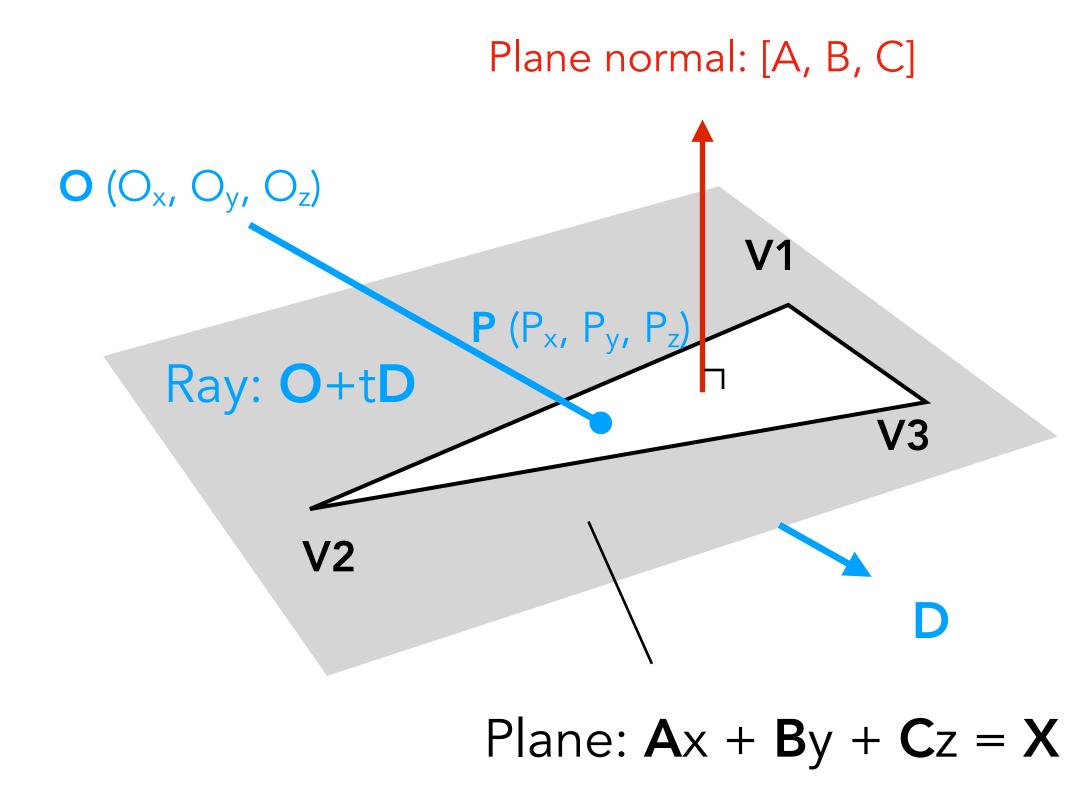






### **Ray-Triangle Intersection**

 $P_x = O_x + D_x \times t$  $P_y = O_y + D_y \times t$  $P_{z} = O_{z} + D_{z} \times t$  $A \times P_x + B \times P_y + C \times P_z = 1$  $\frac{1 - (A \times O_x + B \times O_y + C \times O_z)}{A \times D_x + B \times D_y + C \times D_z}$ 

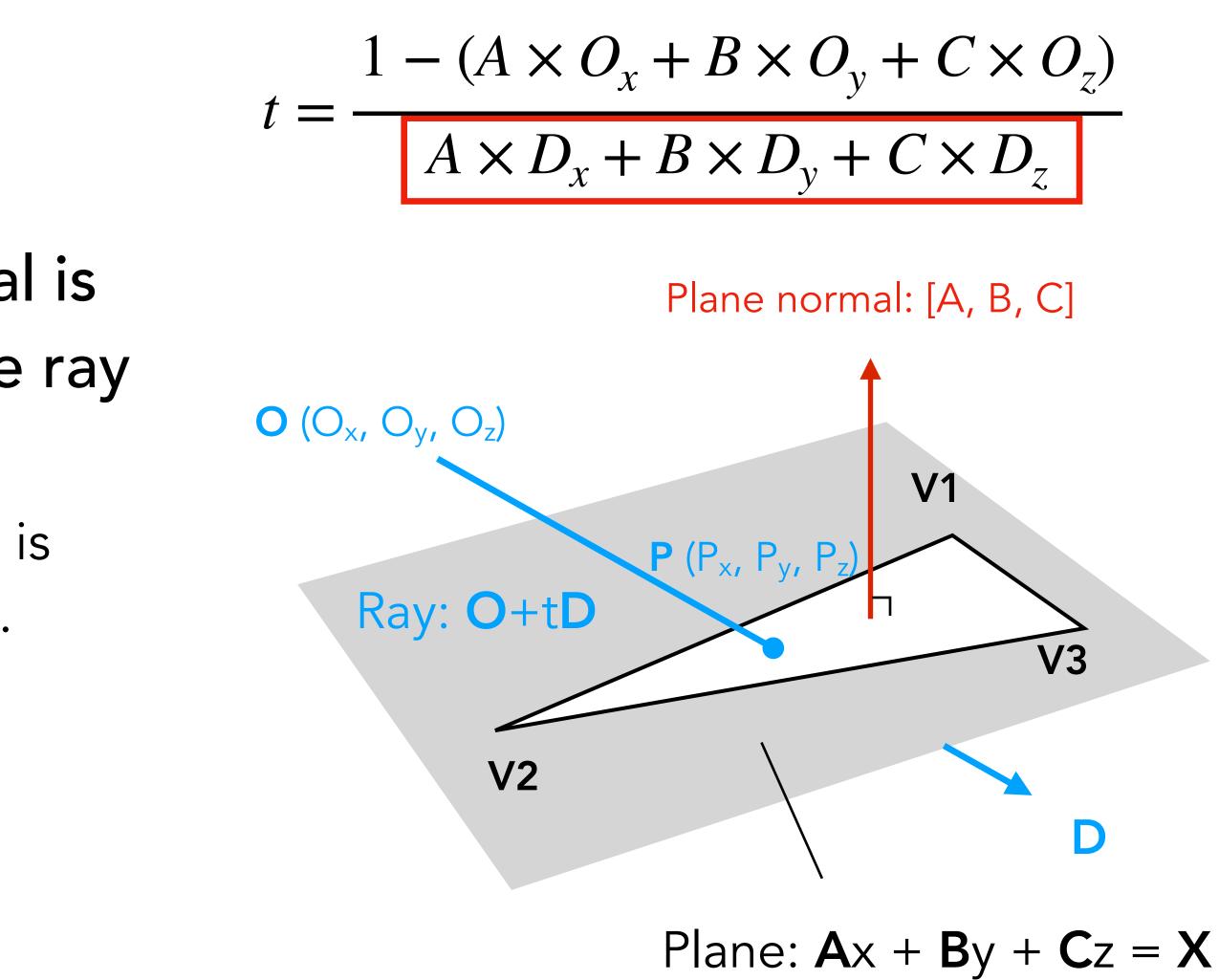




### **Three Caveats**

1. The denominator is 0 if the normal is perpendicular to the direction of the ray (i.e., ray is parallel to the plane).

• Need a special test for whether the ray is parallel with the plane (before division).



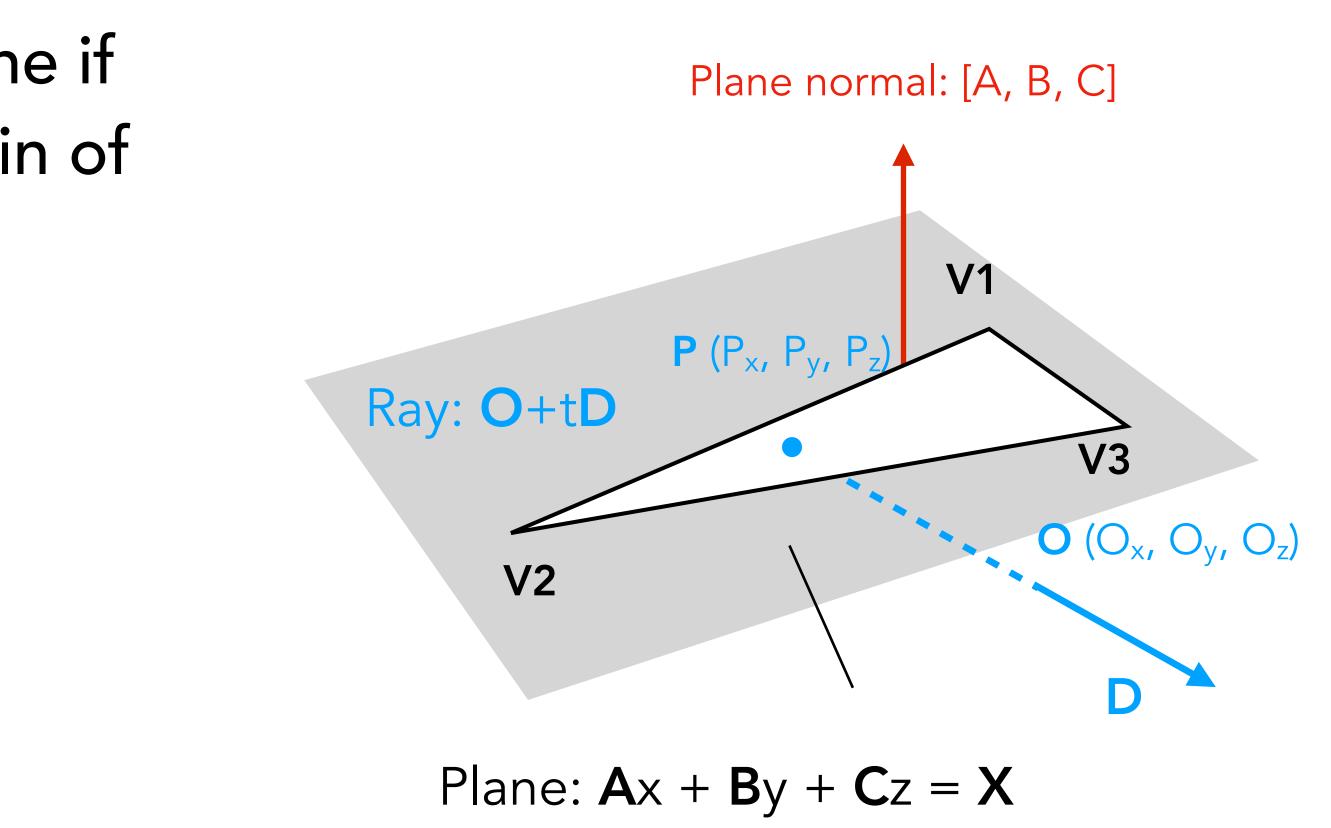




### Three Caveats

2. A ray doesn't intersect with a plane if the triangle plane is behind the origin of the ray

• i.e., t is negative.





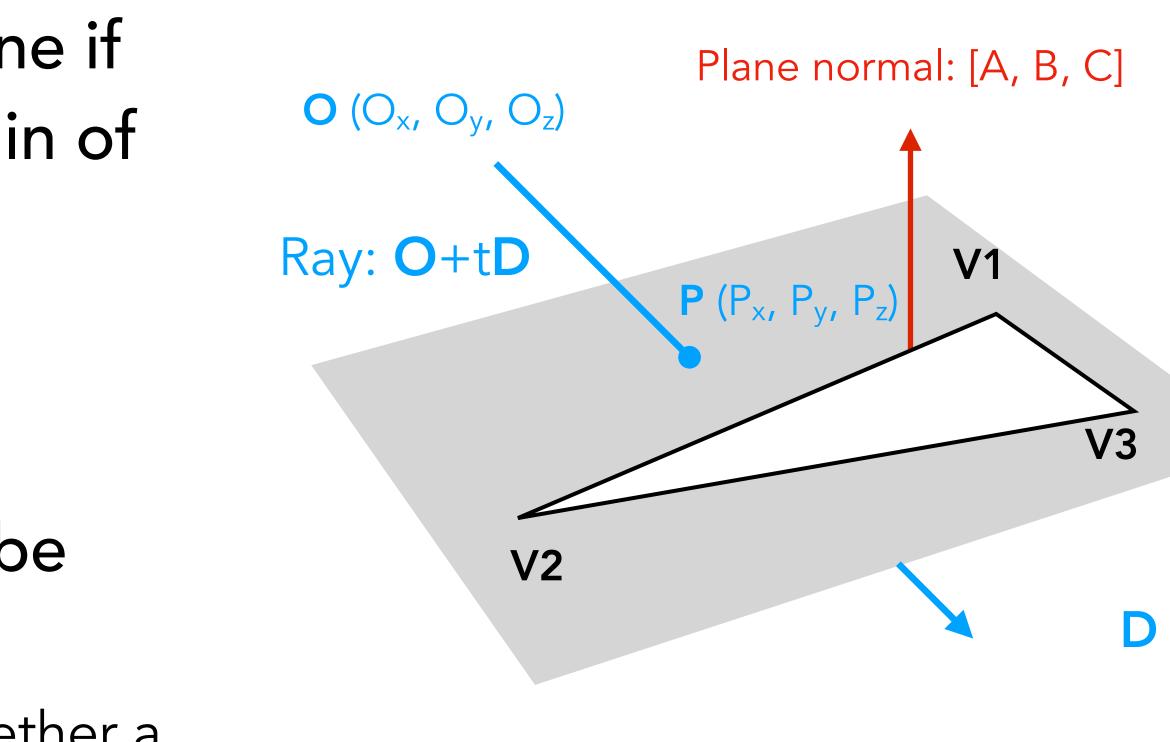
### Three Caveats

2. A ray doesn't intersect with a plane if the triangle plane is behind the origin of the ray

• i.e., t is negative.

3. Even if a real intersection point is found, the intersection point could be outside the triangle.

• Use barycentric coordinates to test whether a point is outside of a triangle.





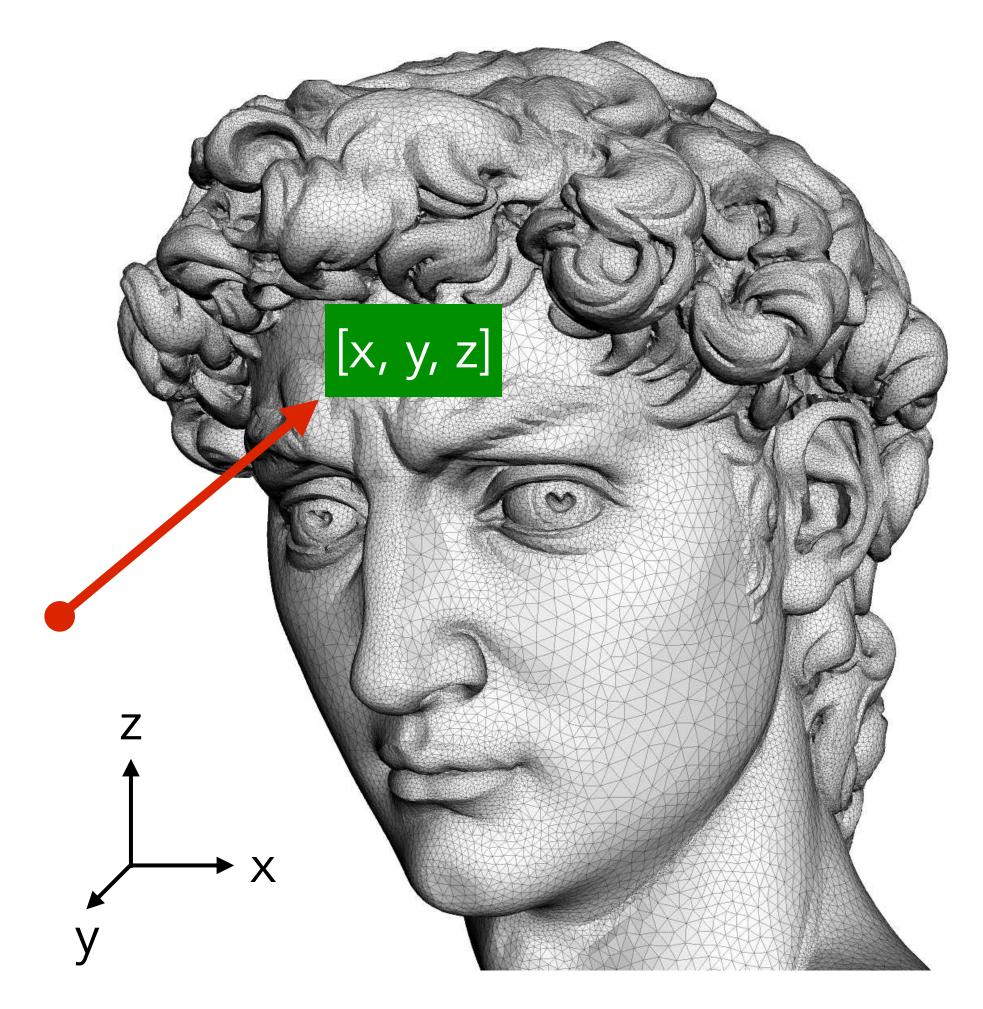
### **Brute-Force Approach is Extremely Inefficient**

### Brute-force approach:

- iterate all triangles
- test intersection for each triangle
- return the closest hit, if any

#### Time complexity:

• O(# of rays x # of triangles)



Valette, et al. [TVCG'08]





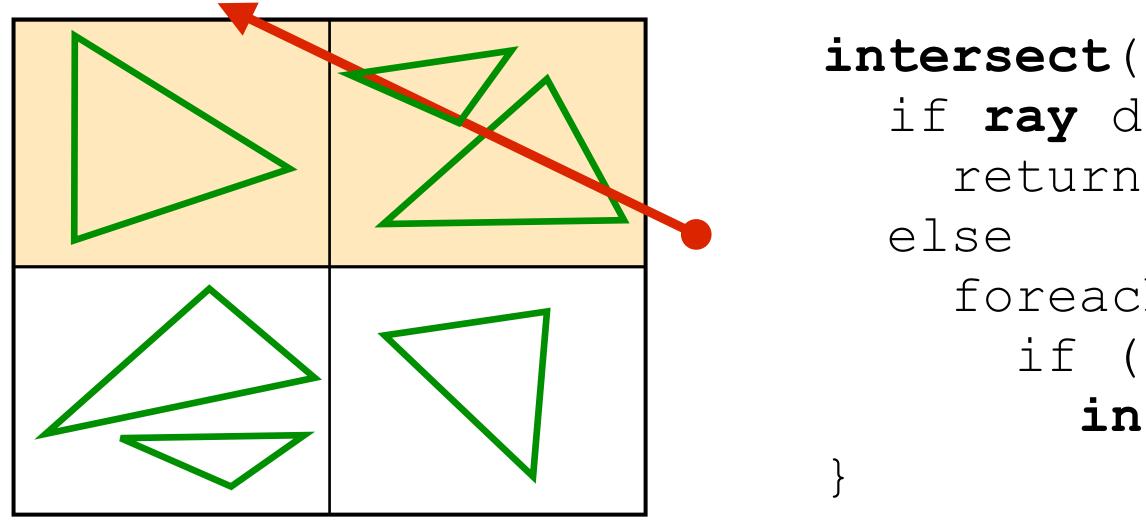
# Accelerating Ray-Scene Intersection



### **Speeding Up Ray-Triangle Intersection Test**

Prune the search space.

Only search part of the scene that does intersect the ray. Key: how to partition the space?



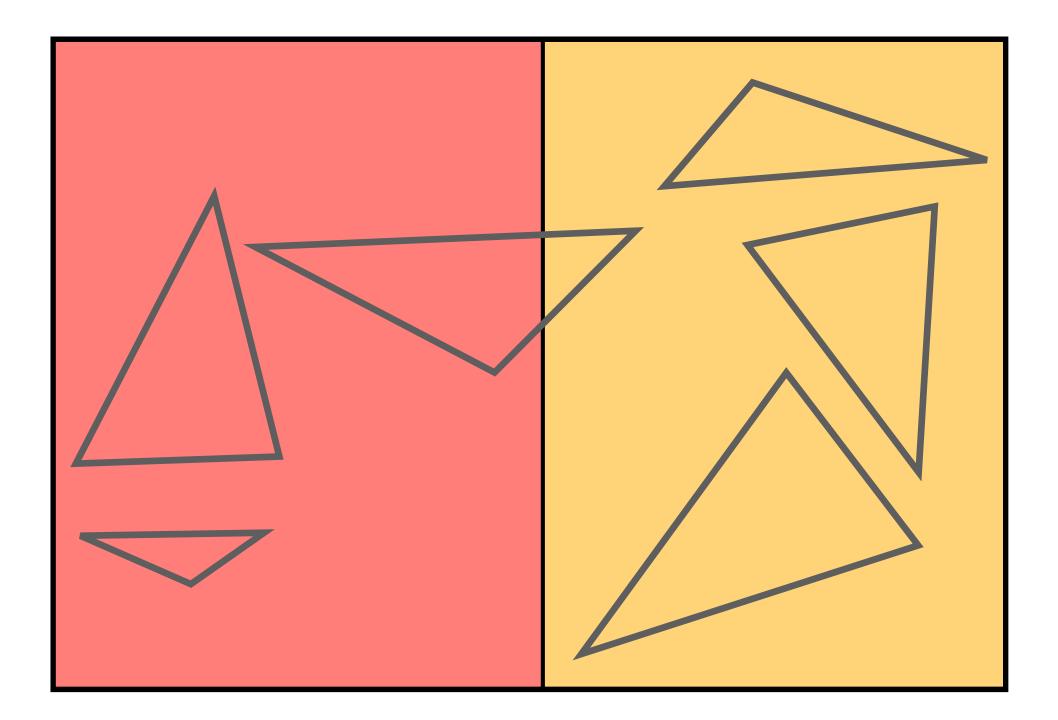
intersect(space, ray) {
 if ray doesn't intersect space boundary:
 return

foreach subspace in space
if (subspace != empty)
intersect(subspace, ray)

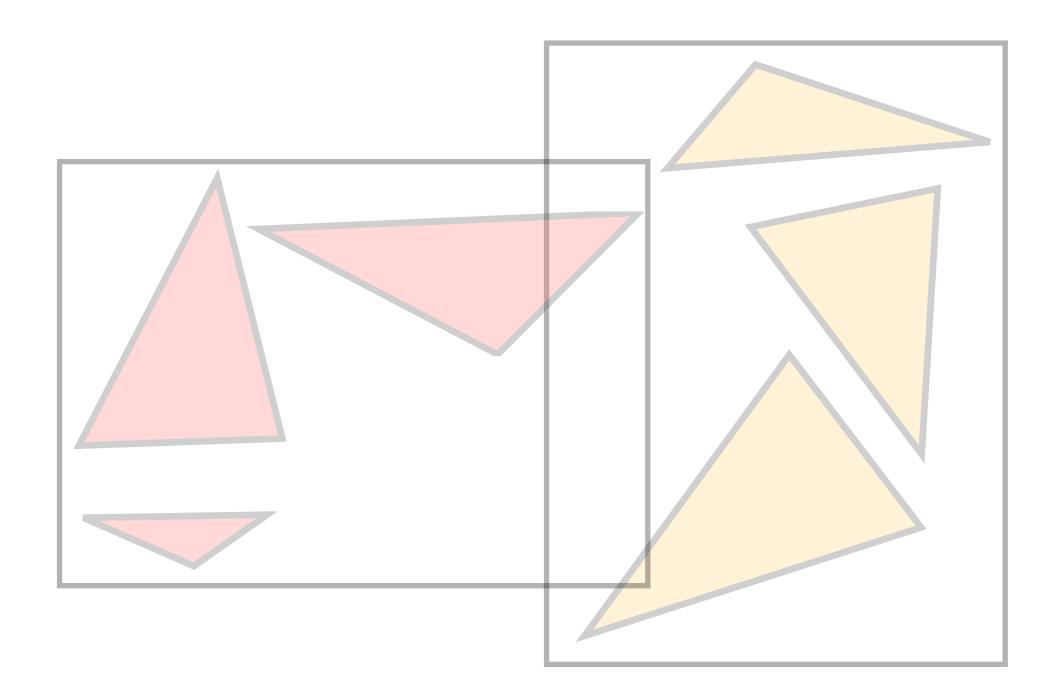


### Space vs. Object Partitioning

**Space partitioning**: One object could be in different partitions

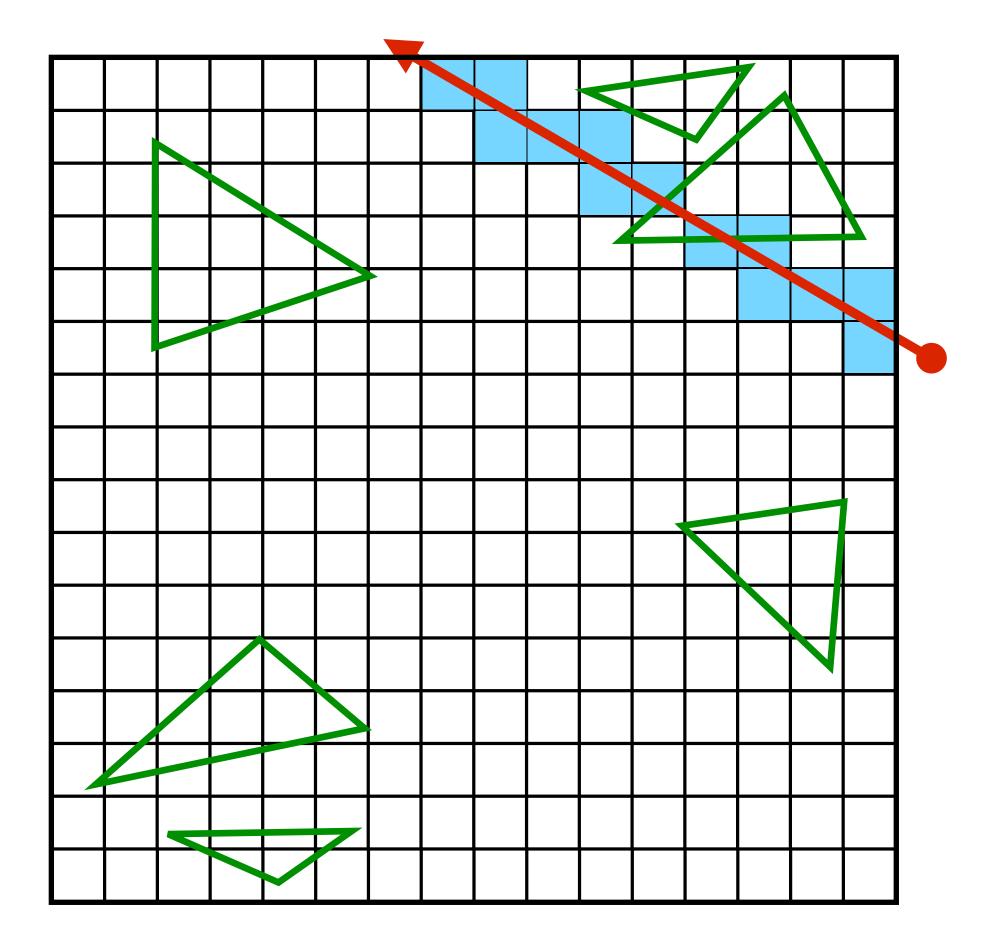


## **Object partitioning**: different partitions could overlap in space





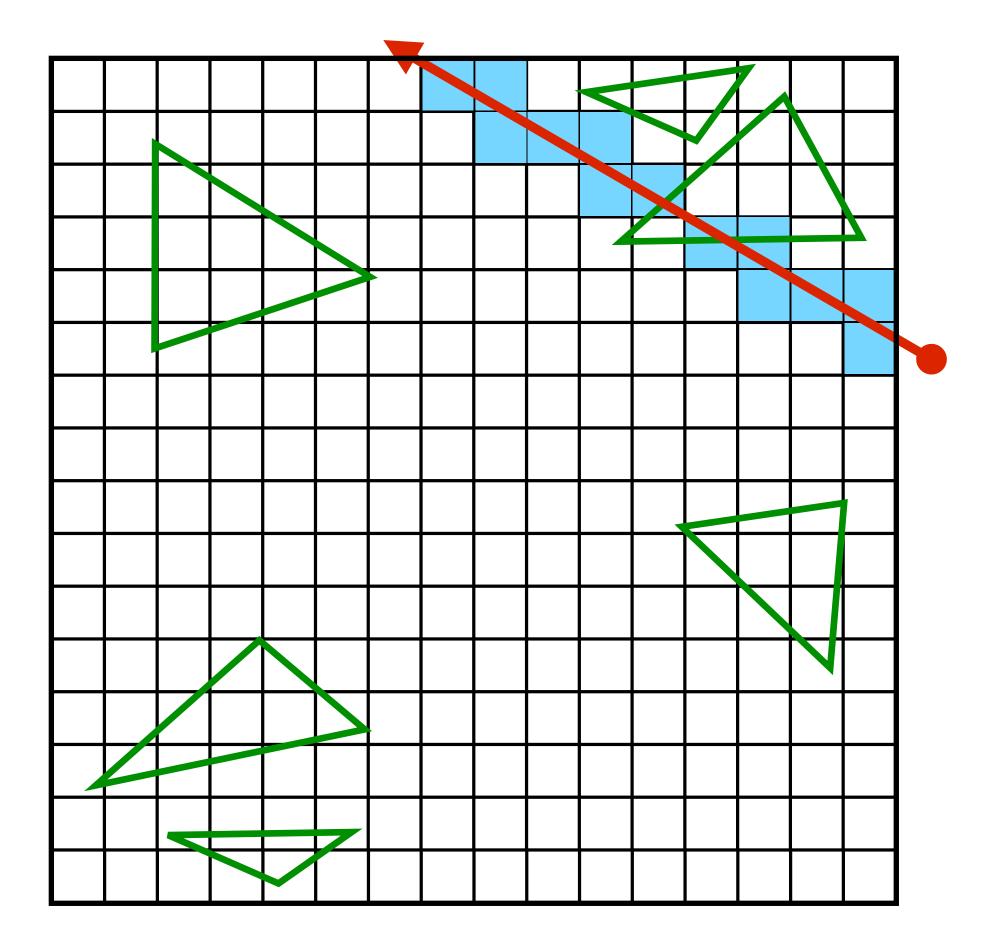
### **Uniform Grid**



- Find the bounding box of the scene
- Generate a uniform grid
- Find intersecting cells
- For each intersecting cell:
  - Iterate over all the containing triangles
  - Get the closet intersection within the cell
  - Update the global closet intersection



### **Grid Resolution**



#### Too few cells:

• Little speedup

#### Too many cells:

Many empty cells to check and to store

#### A useful heuristics:

- The number of cells should be proportional to the number of triangles
- #cell in each dimension =  $n^{1/3}$



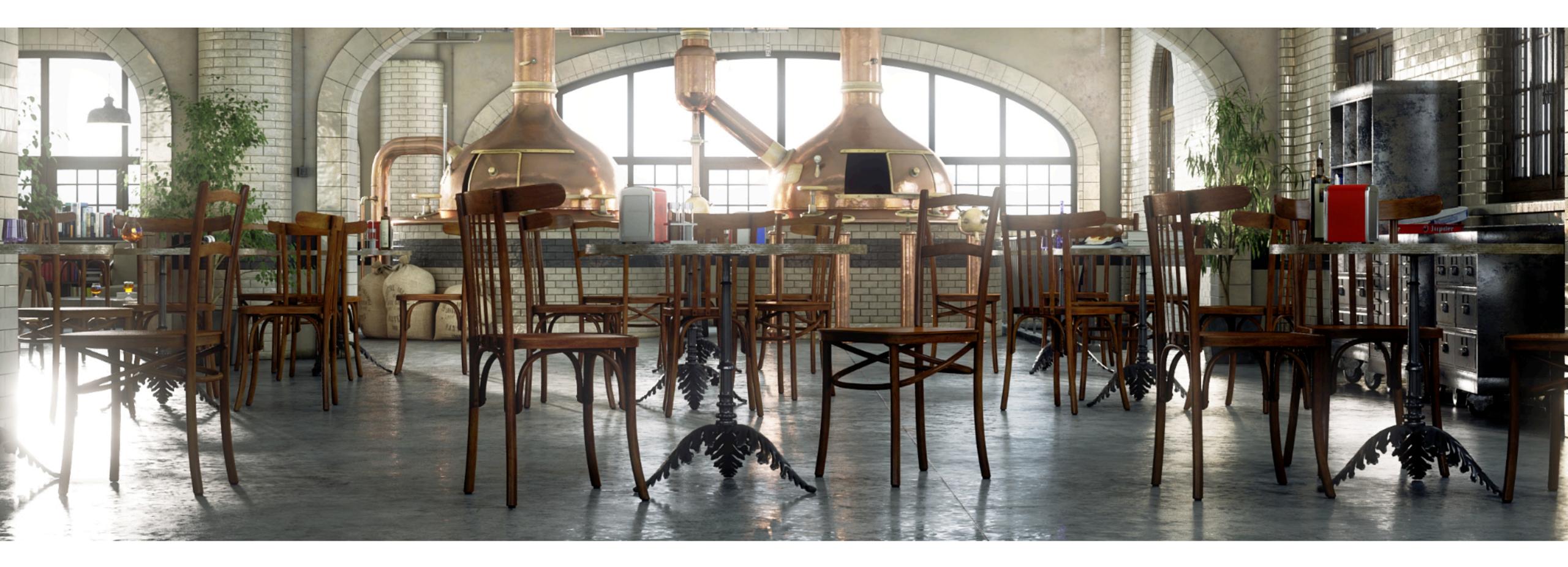
### When Uniform Grid Works



#### Small objects roughly uniformly distributed in space



### When Uniform Grid is Inefficient

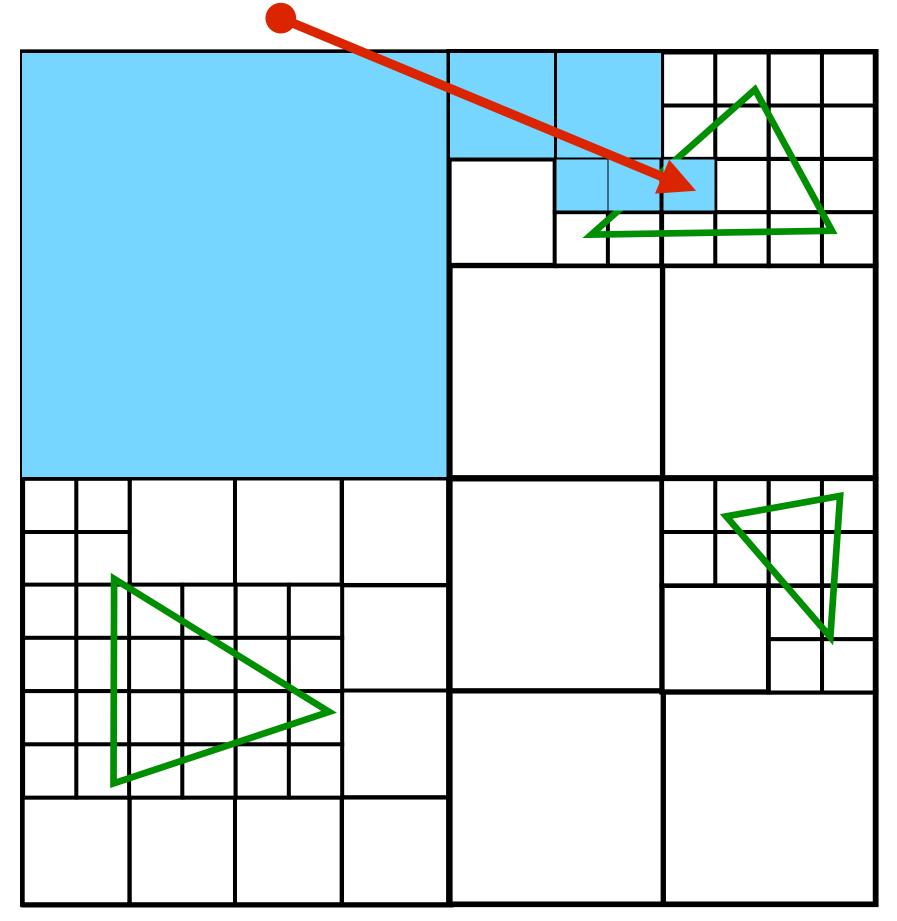


**Objects sparsely distributed in space ("teapot in a stadium")** 



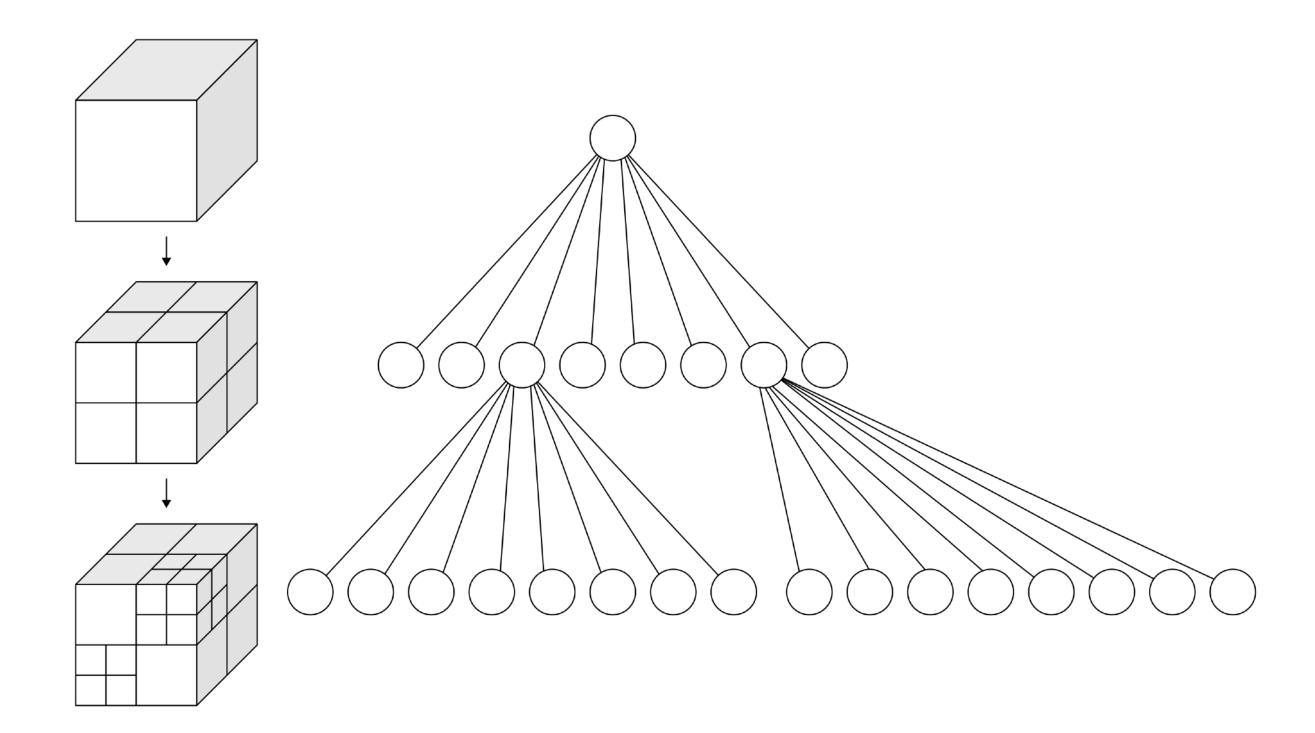
### Non-Uniform (Adaptive) Grid

Quadtree (2D)



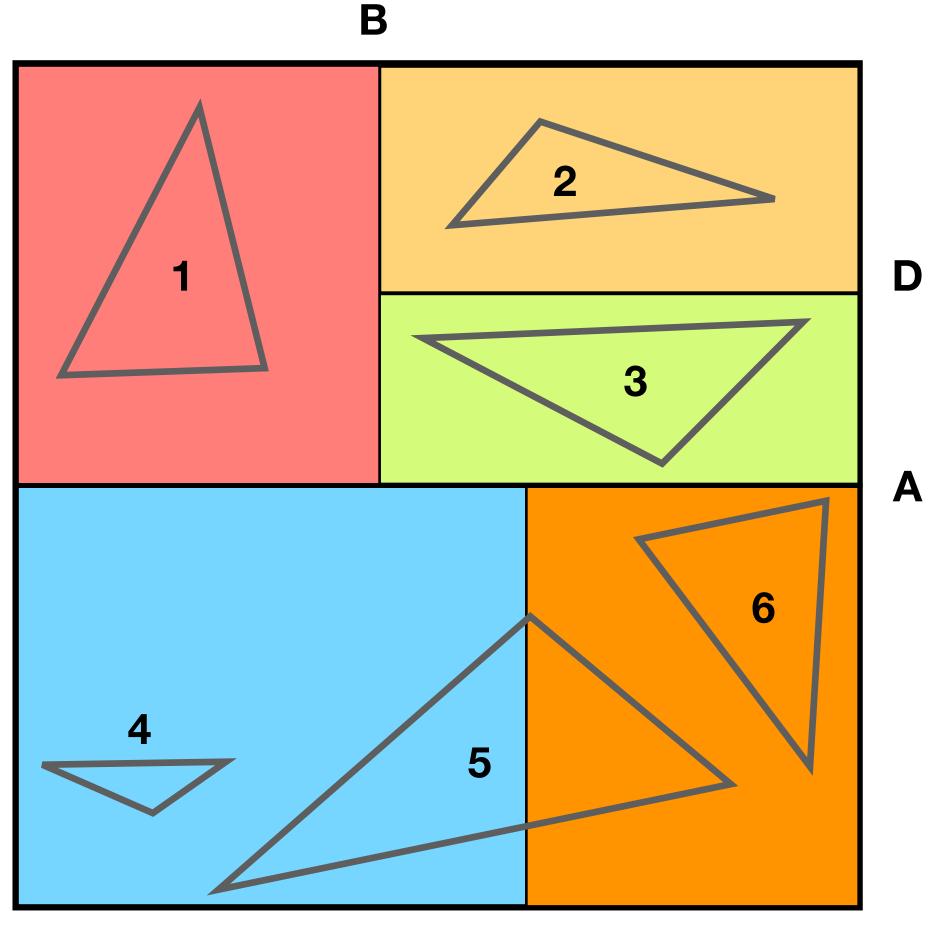


#### Octree (3D)





### **Building K-D Tree**



С

- Recursively using axis-aligned planes to split the space
- Stop when certain terminating conditions are met
  - # of objects in a cell < threshold</li>
  - Max tree depth met
- Organize the splits using a tree
- Find the closest hit by traversing the tree

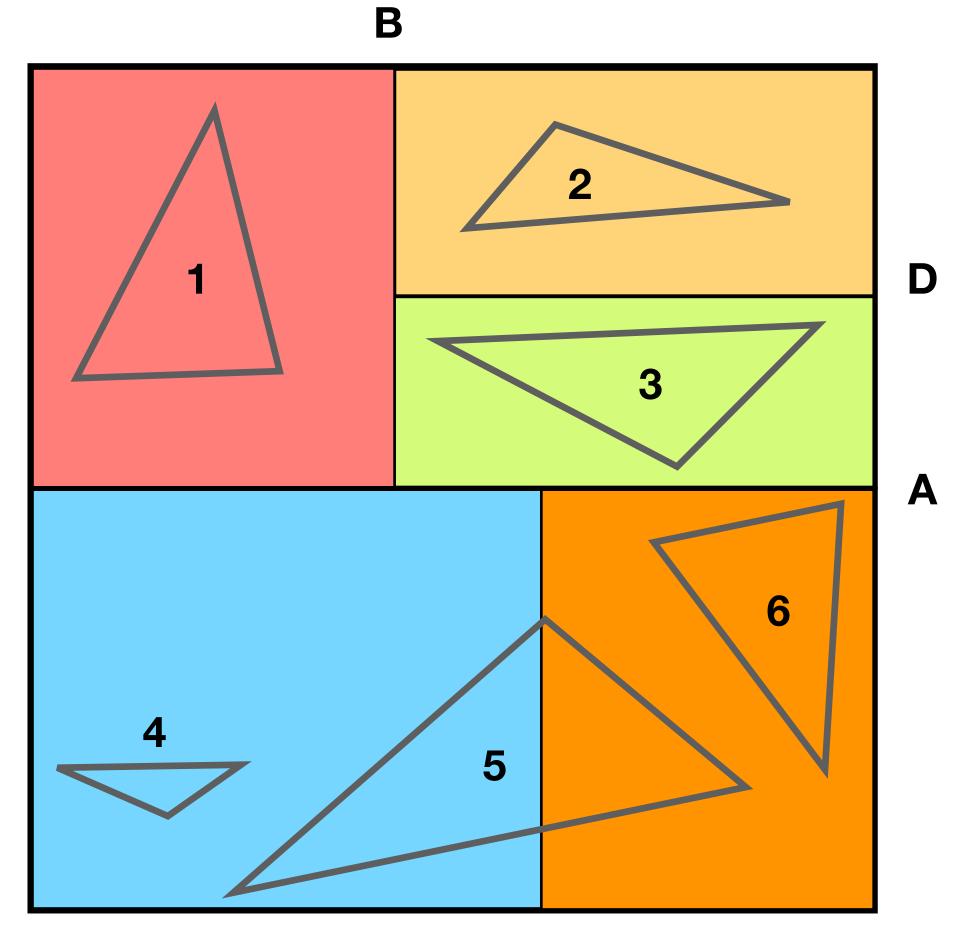




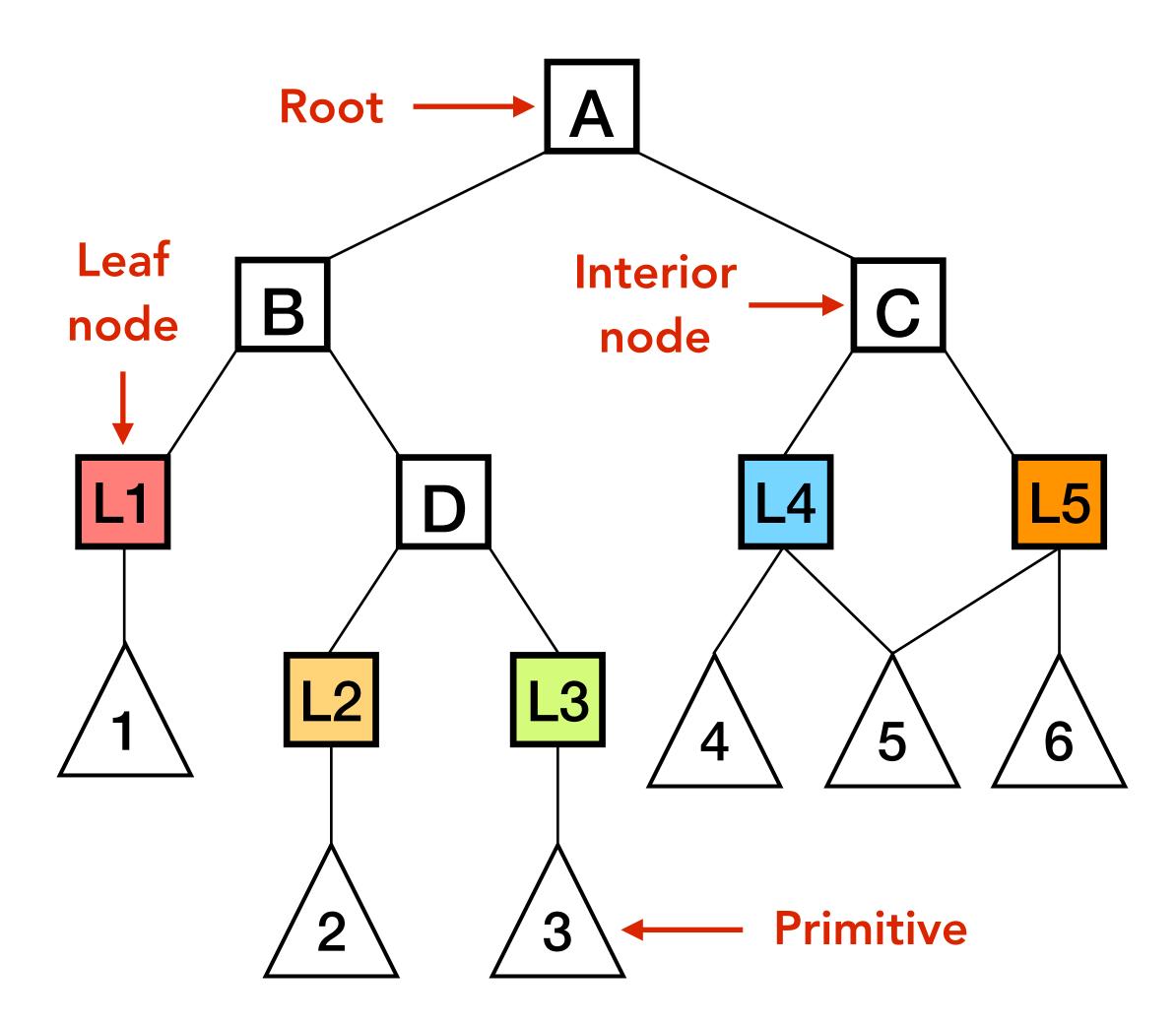








С

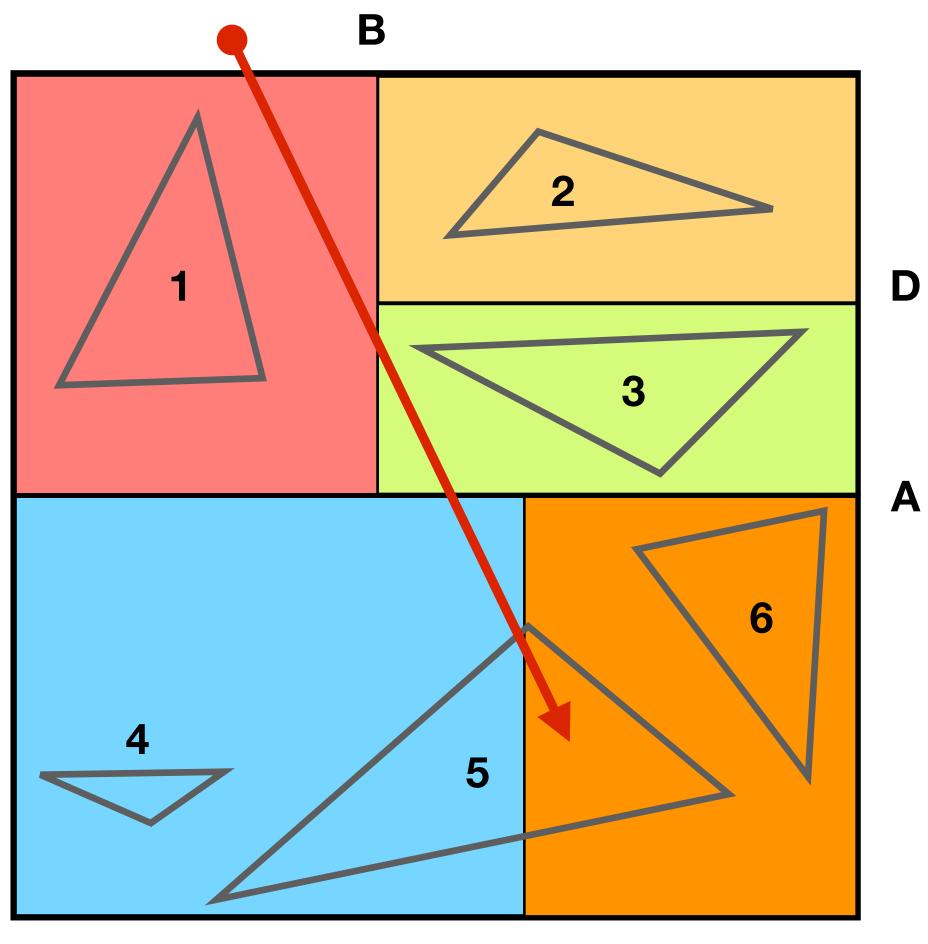


http://groups.csail.mit.edu/graphics/classes/6.838/S98/meetings/m13/kd.html

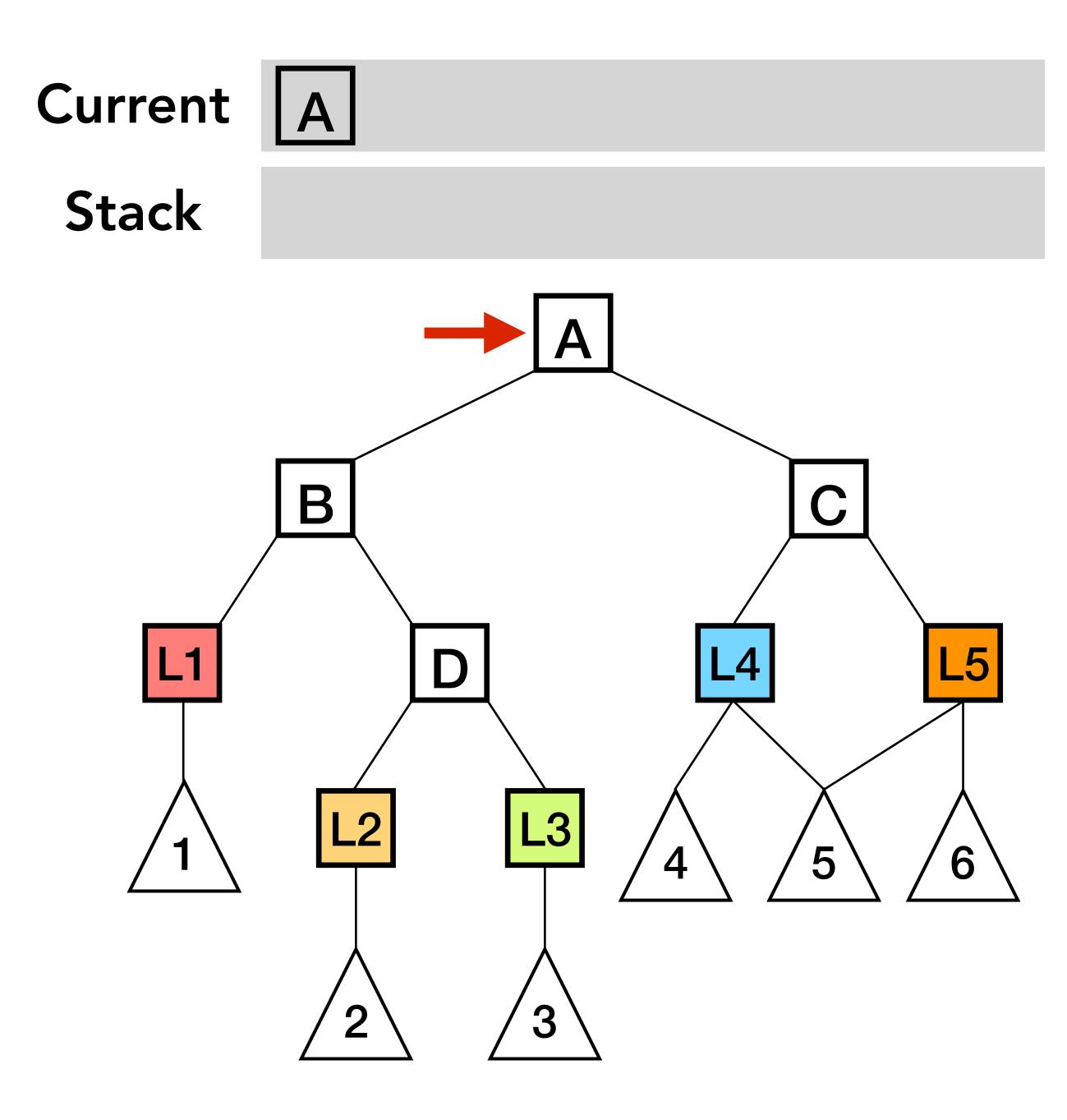




### **Traversing K-D Tree**



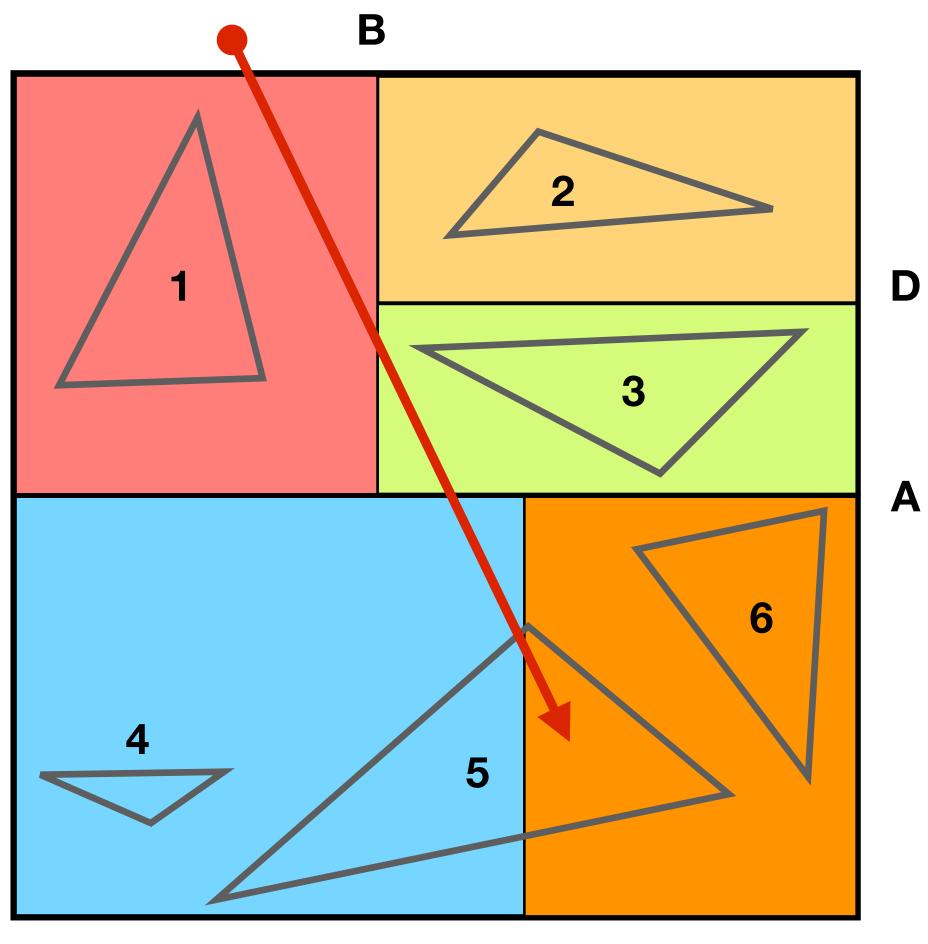
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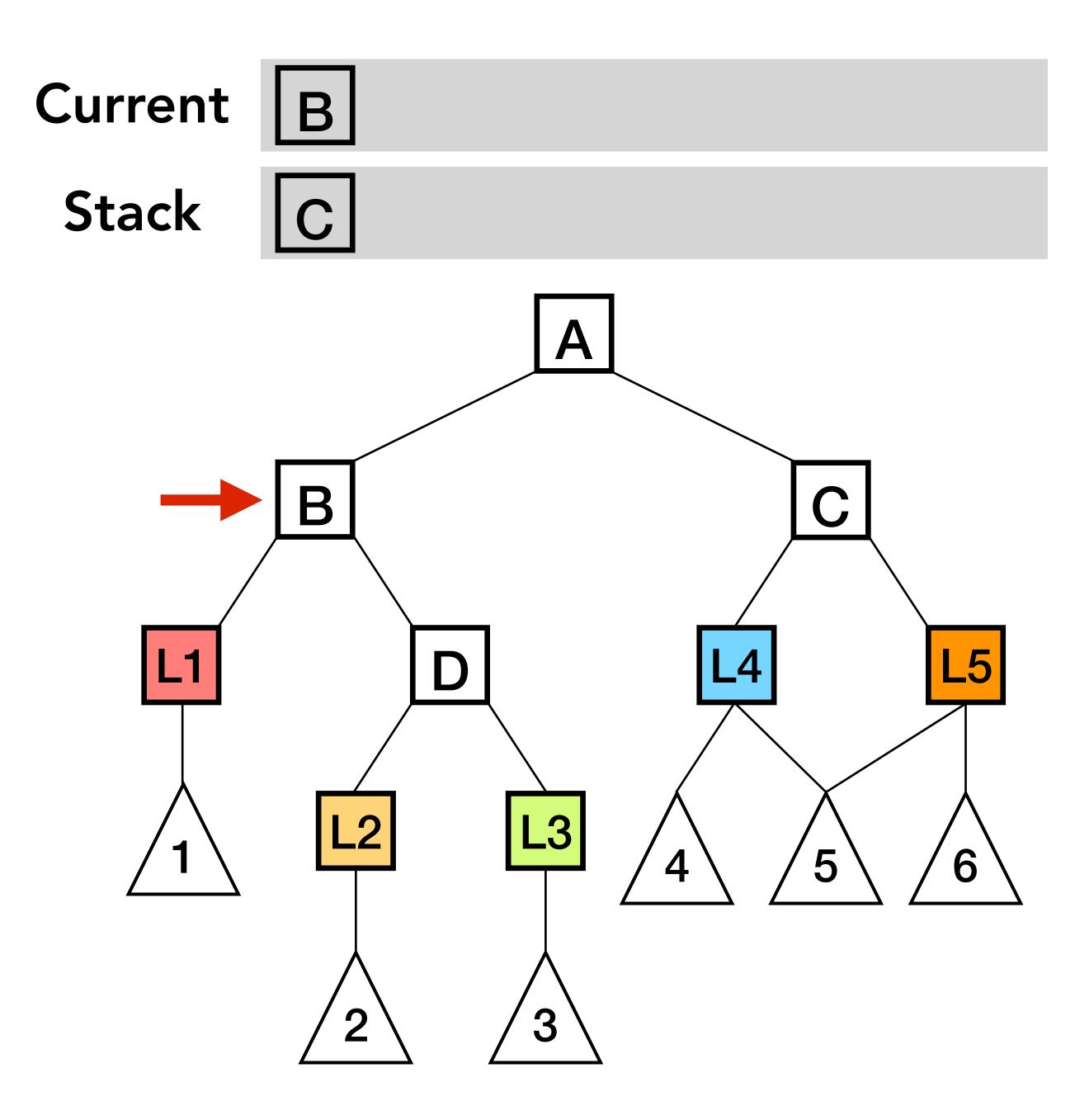


http://groups.csail.mit.edu/graphics/classes/6.838/S98/meetings/m13/kd.html



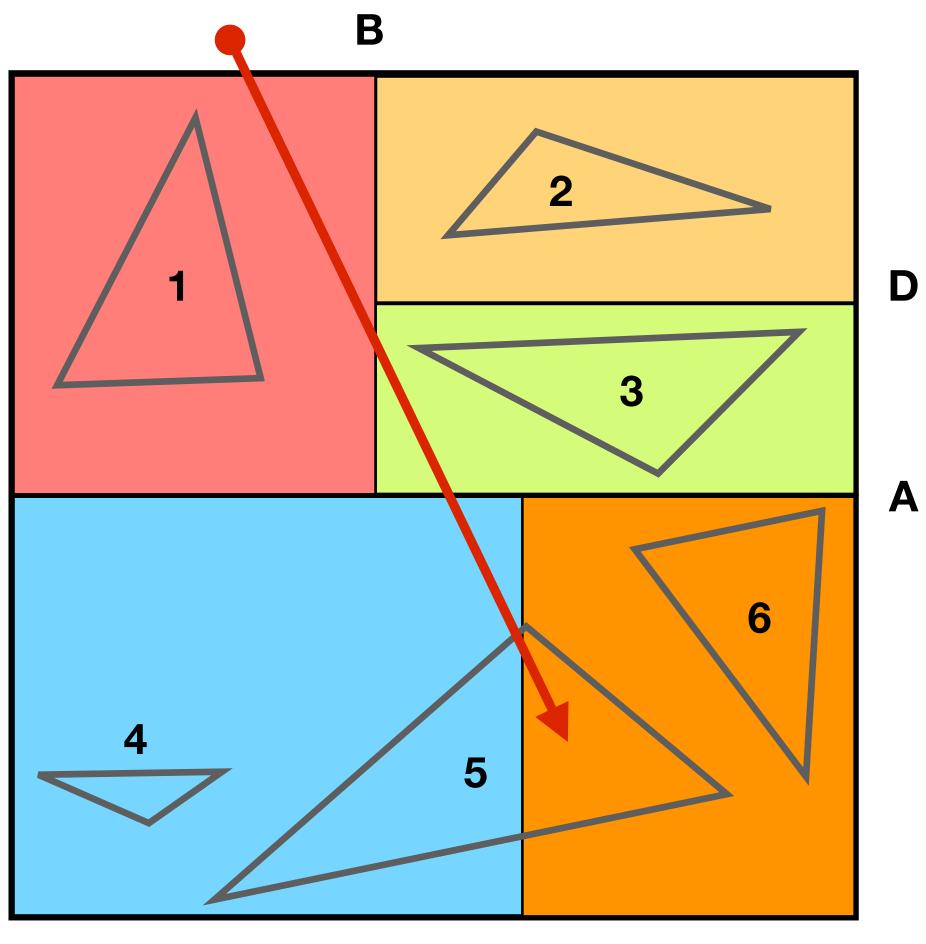


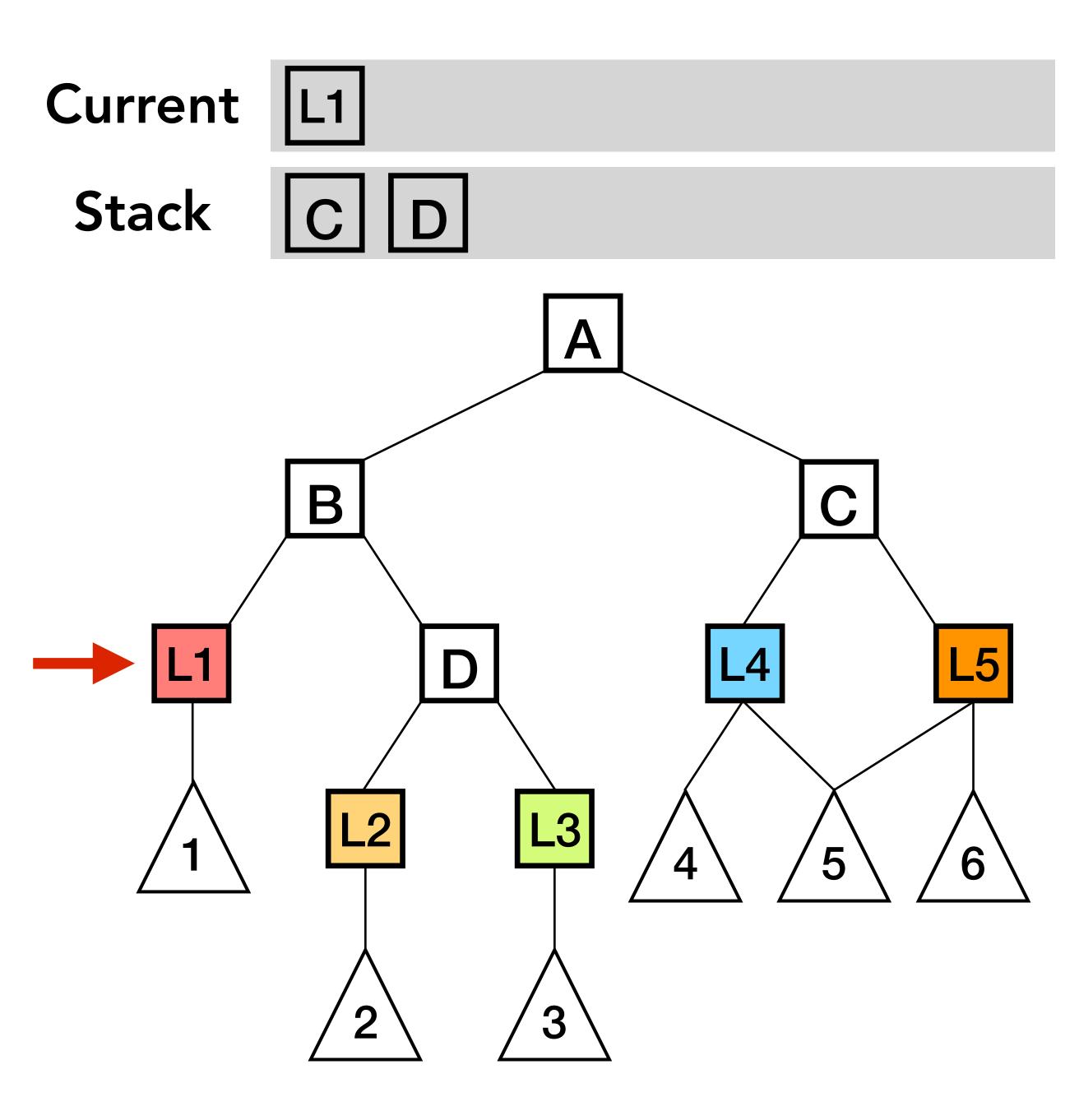






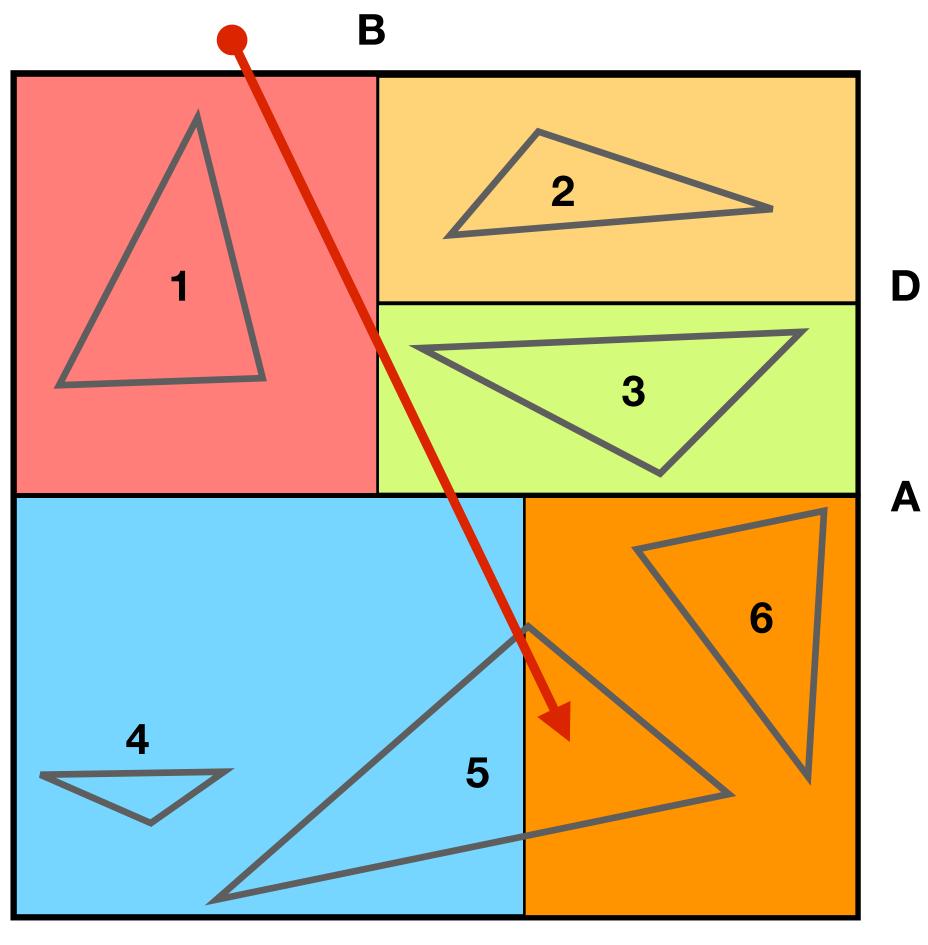


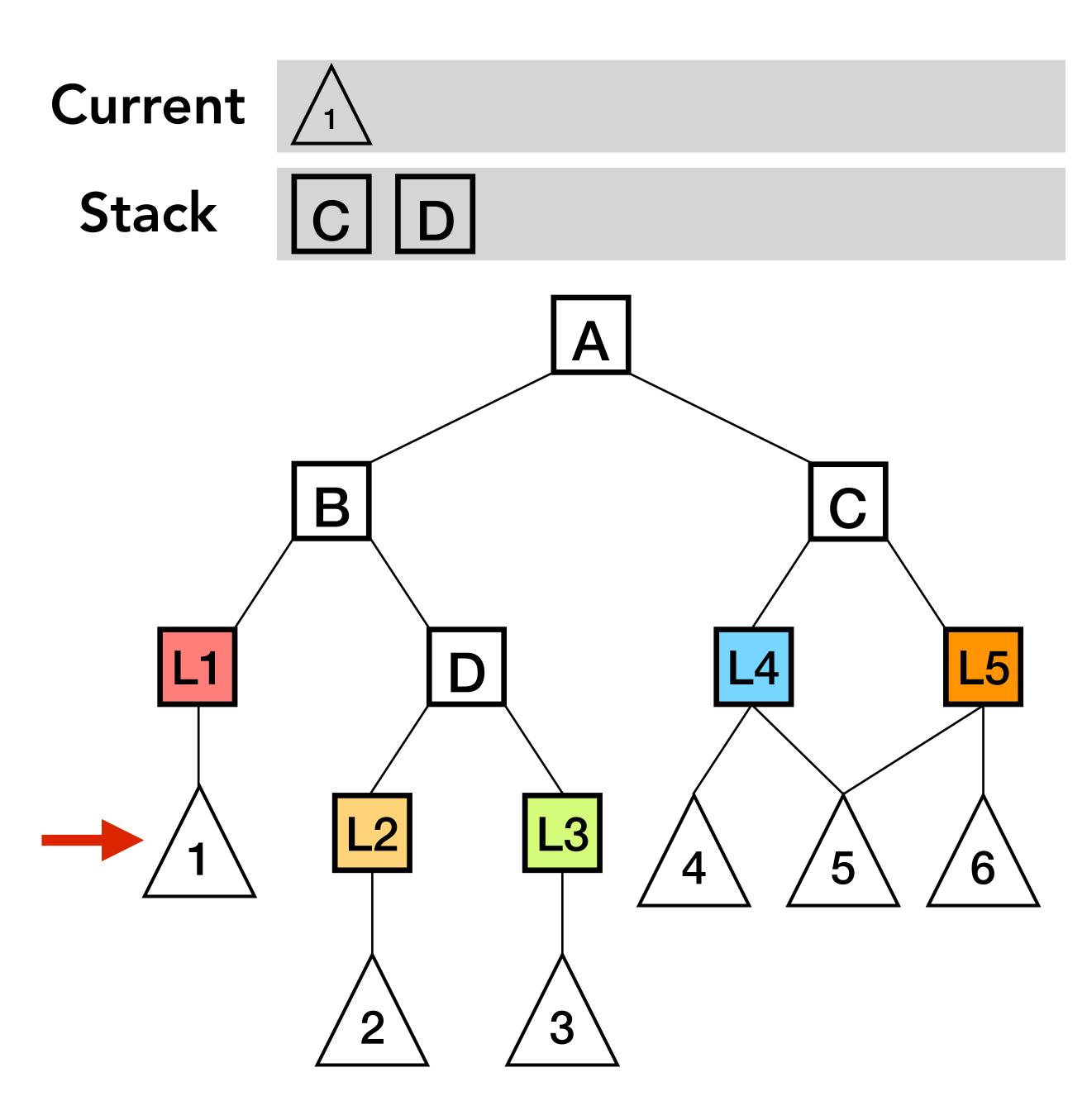






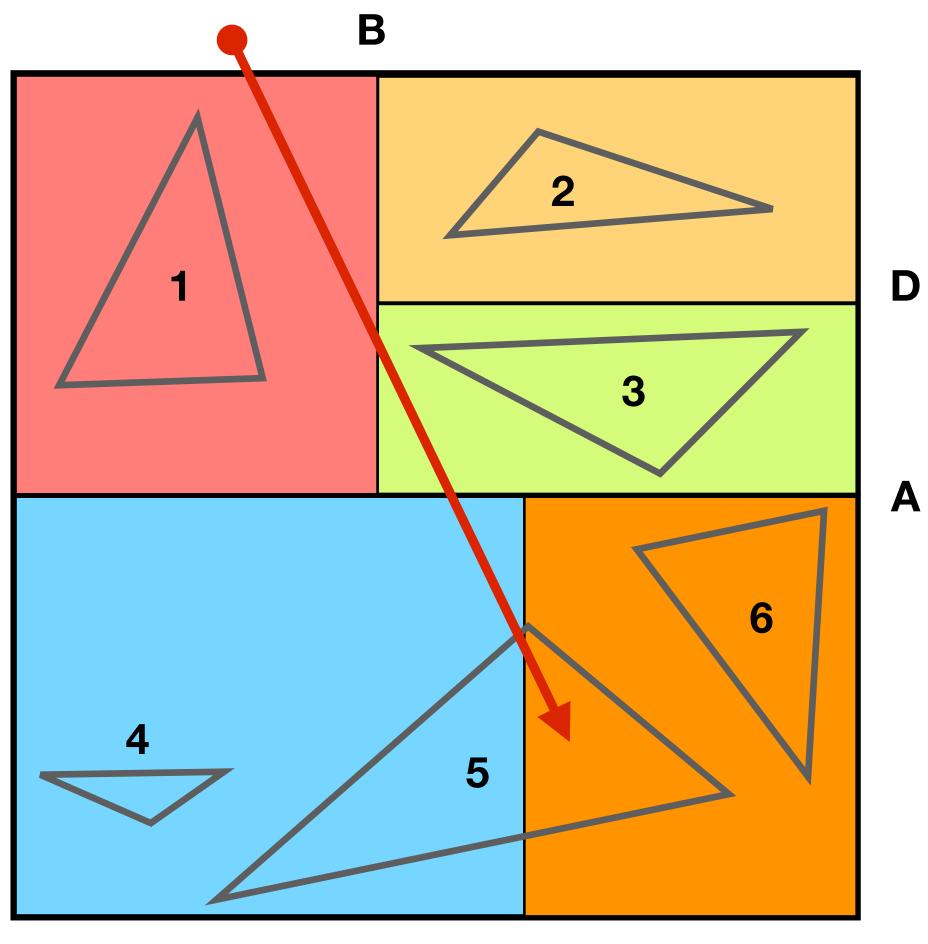


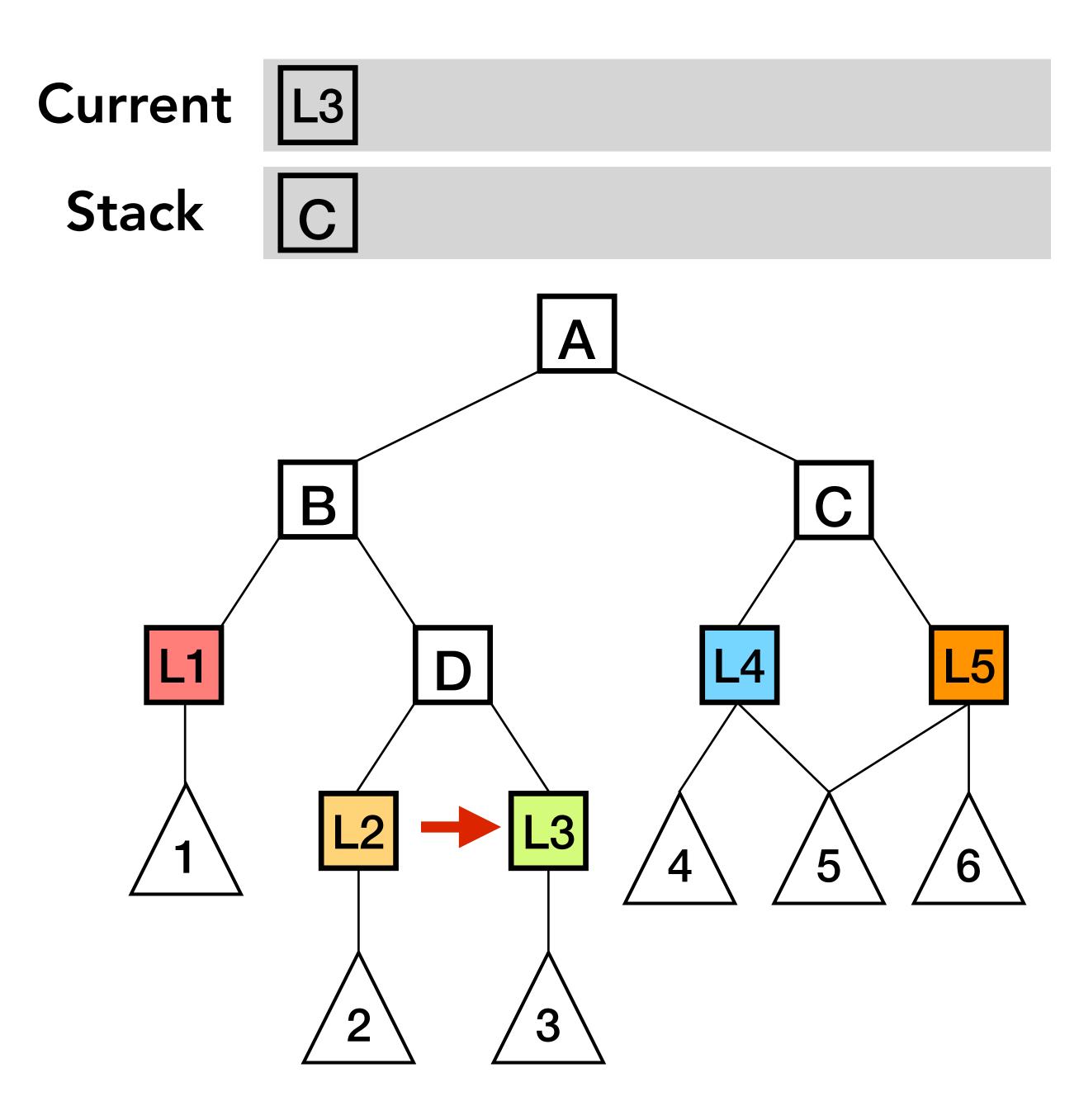






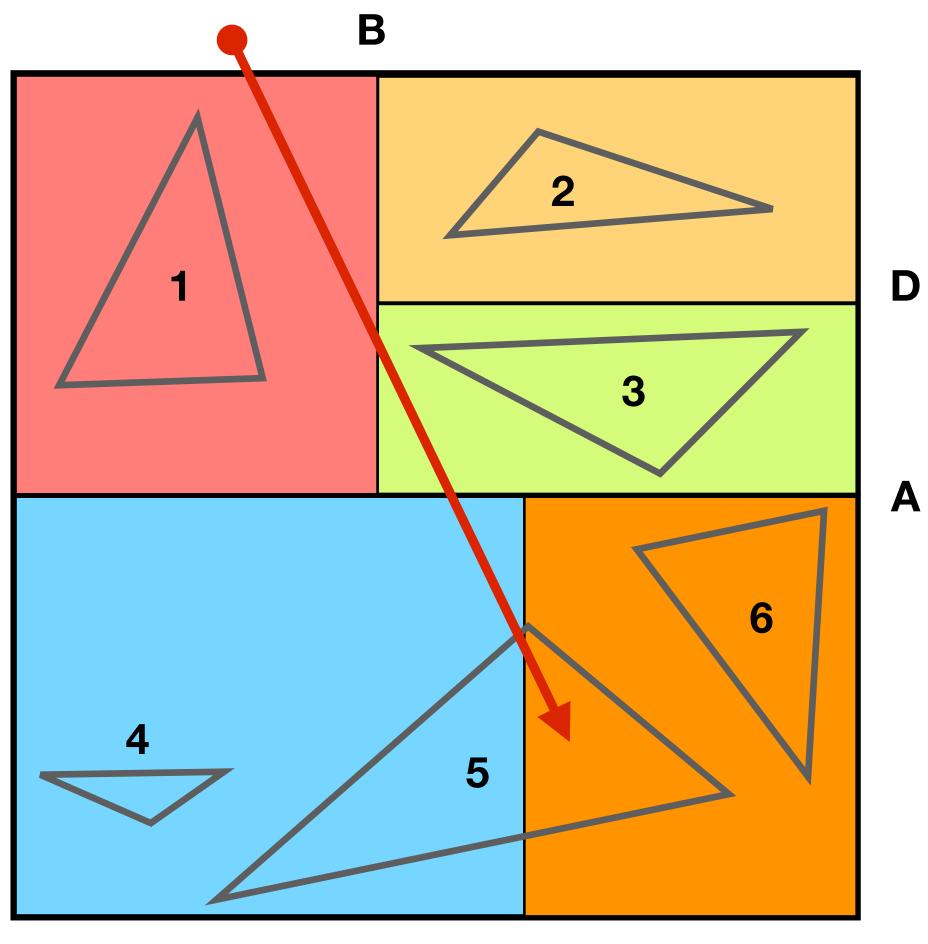


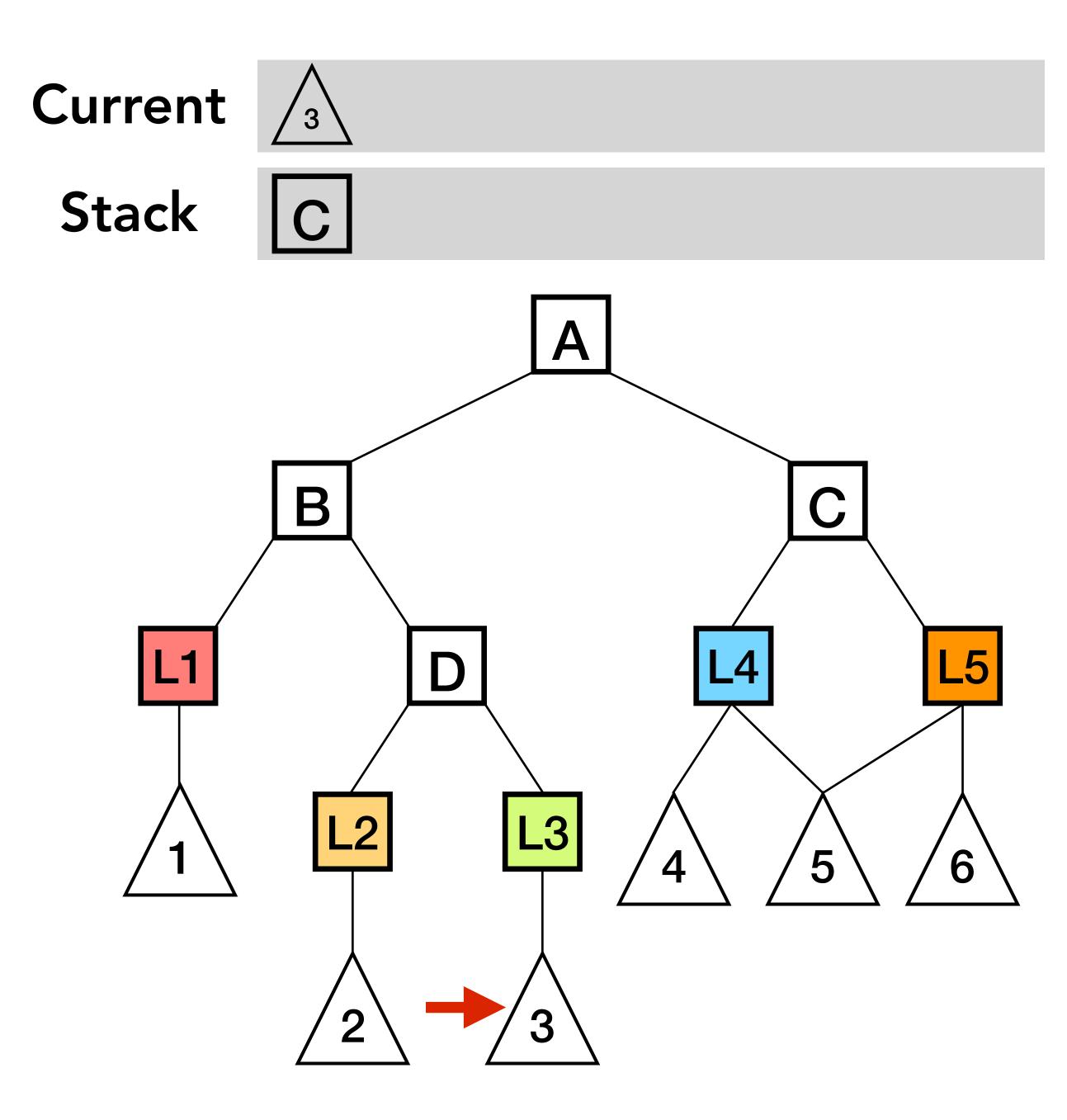






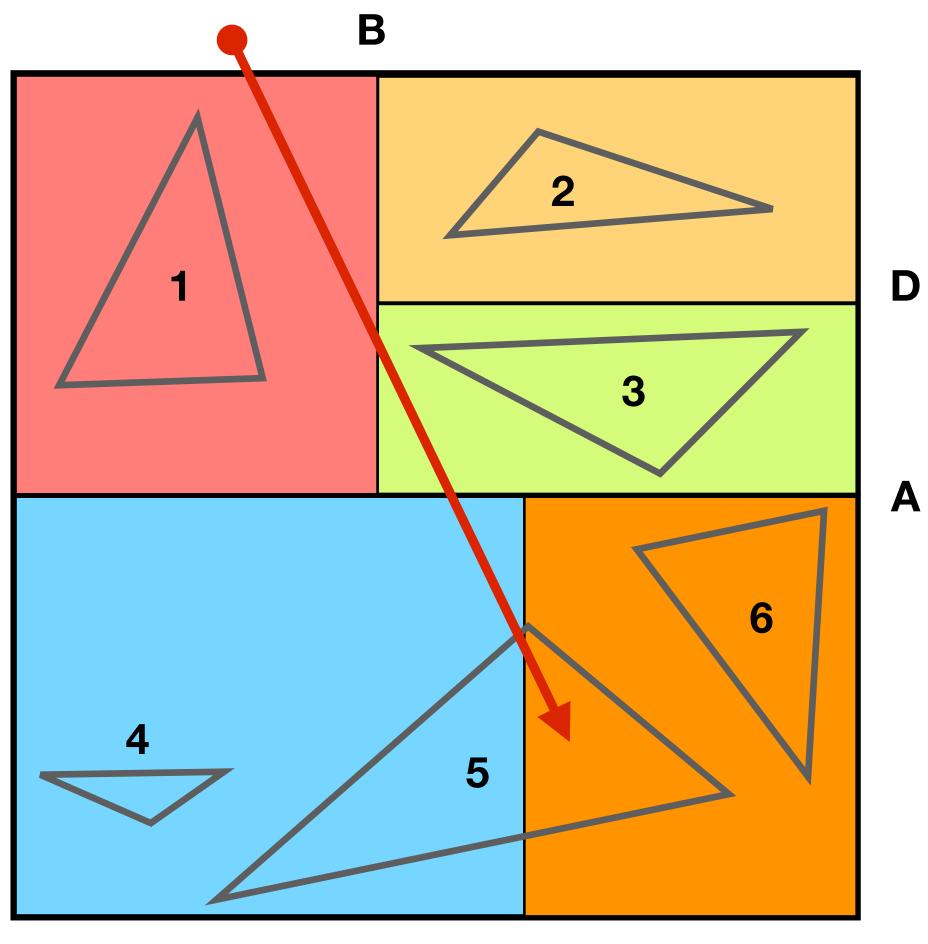


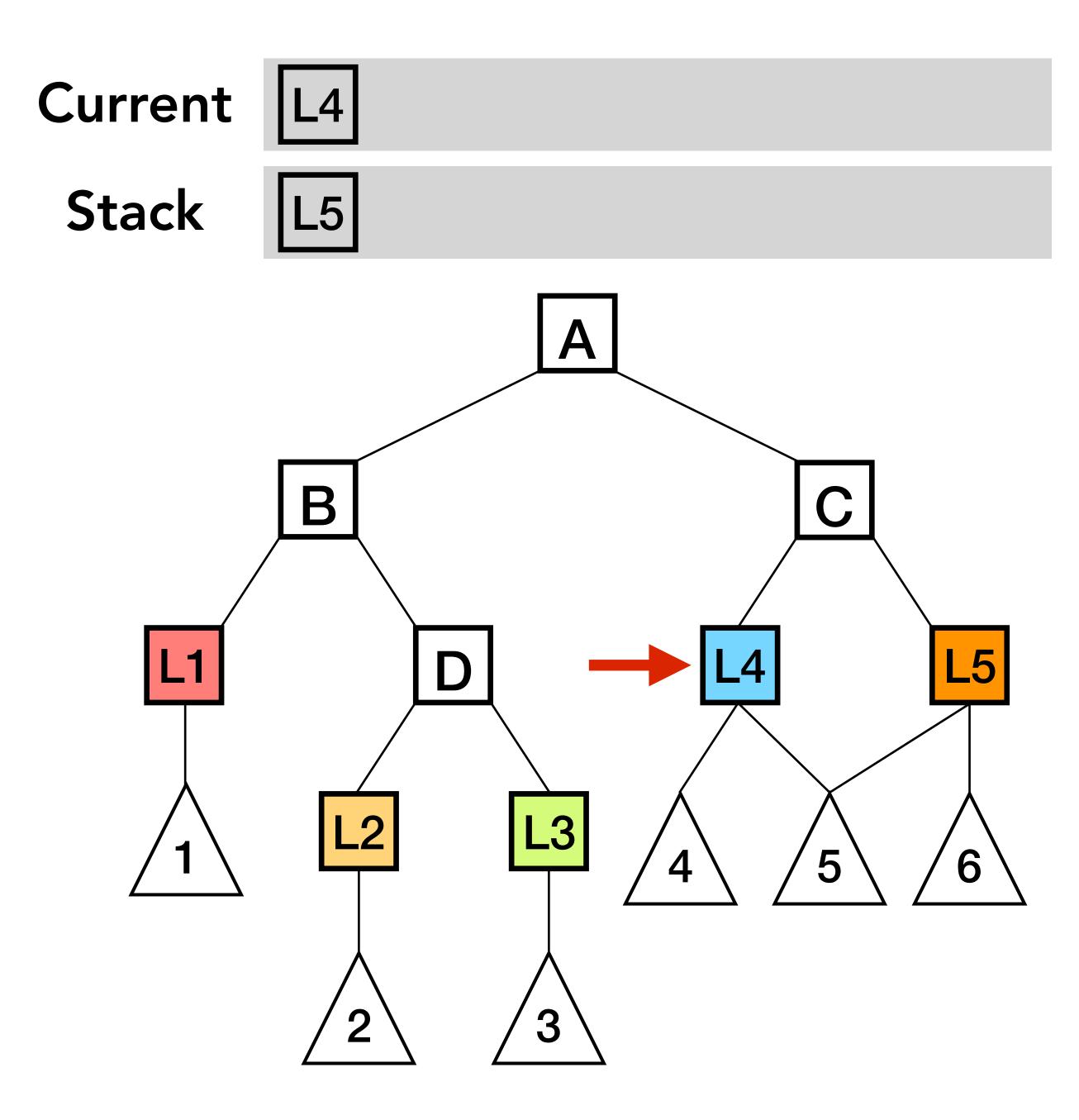






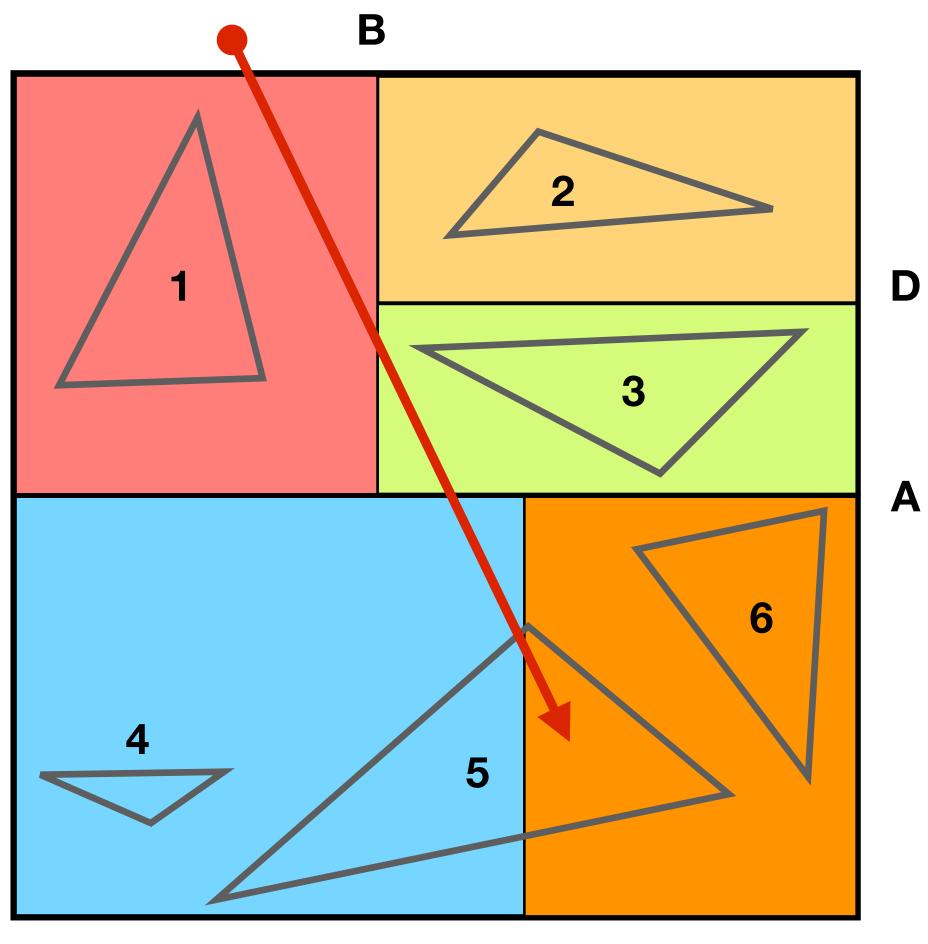


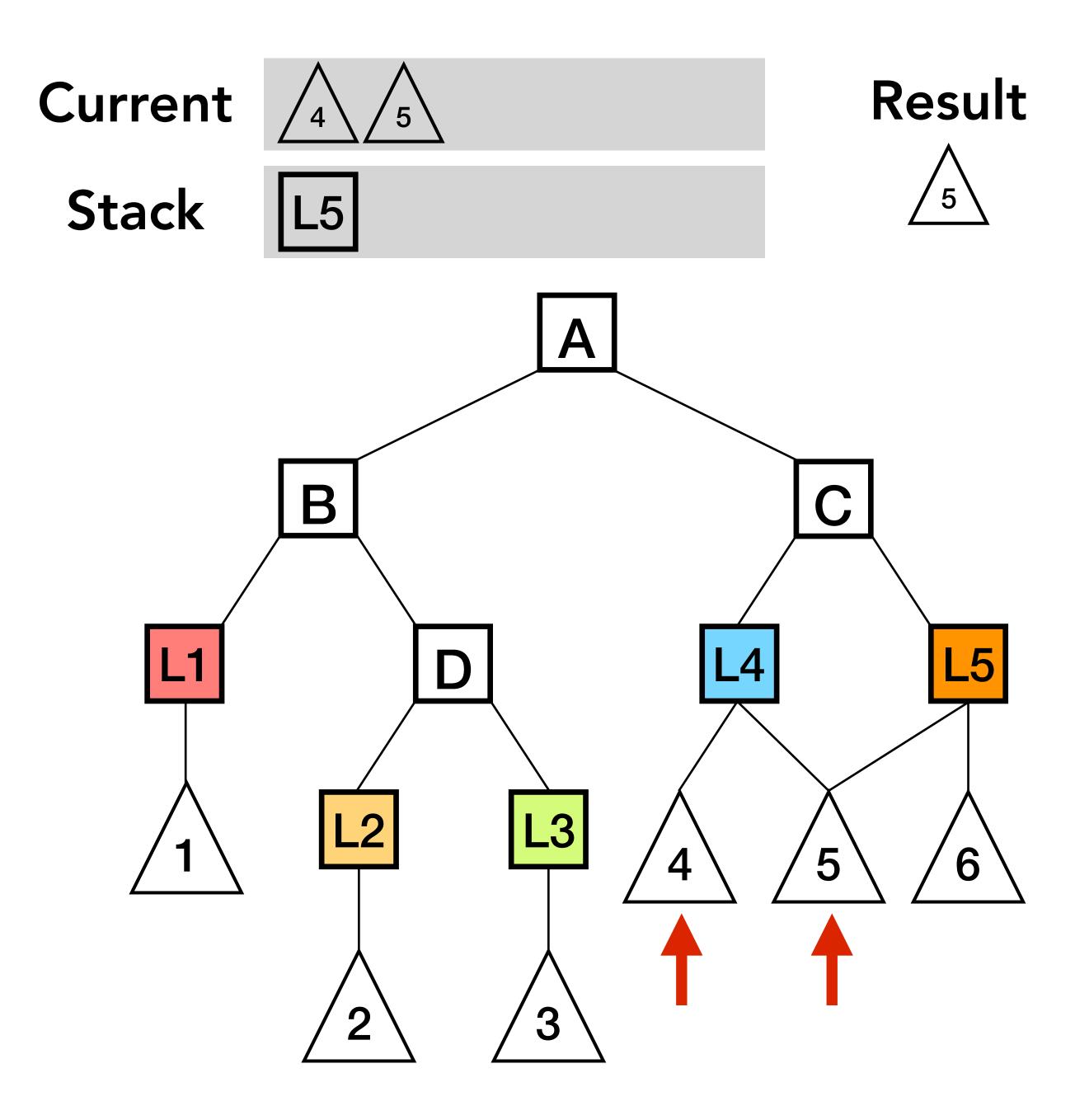






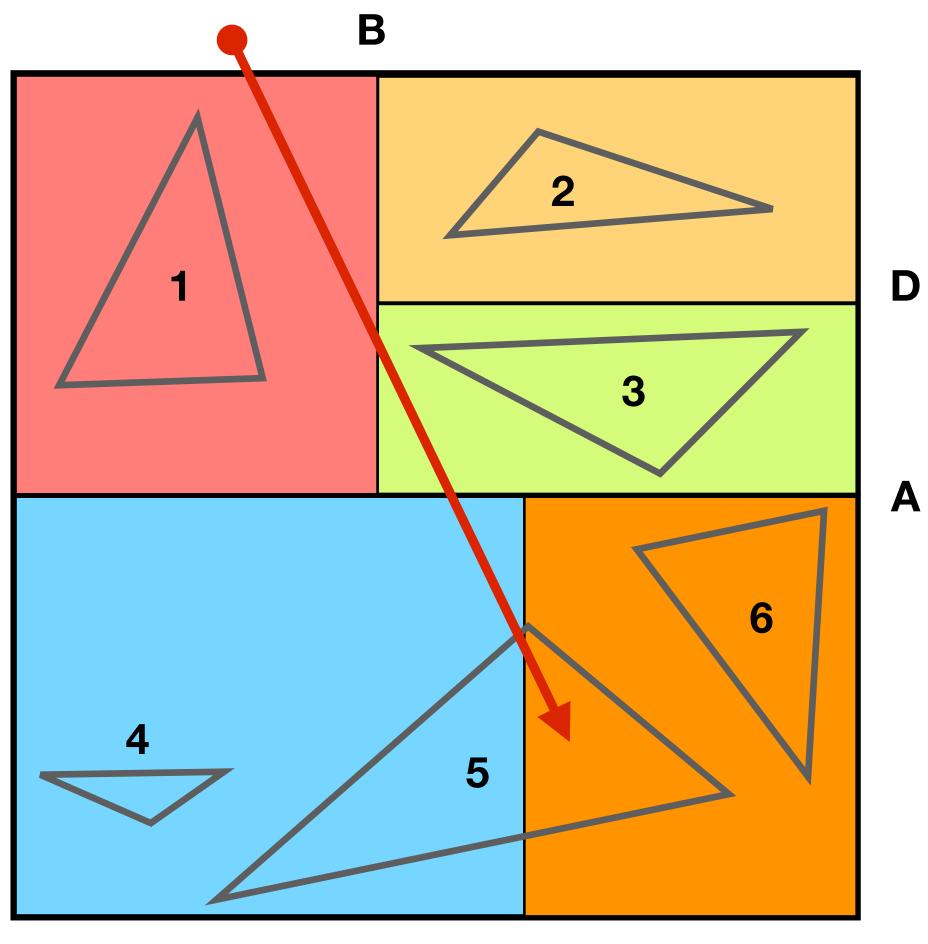


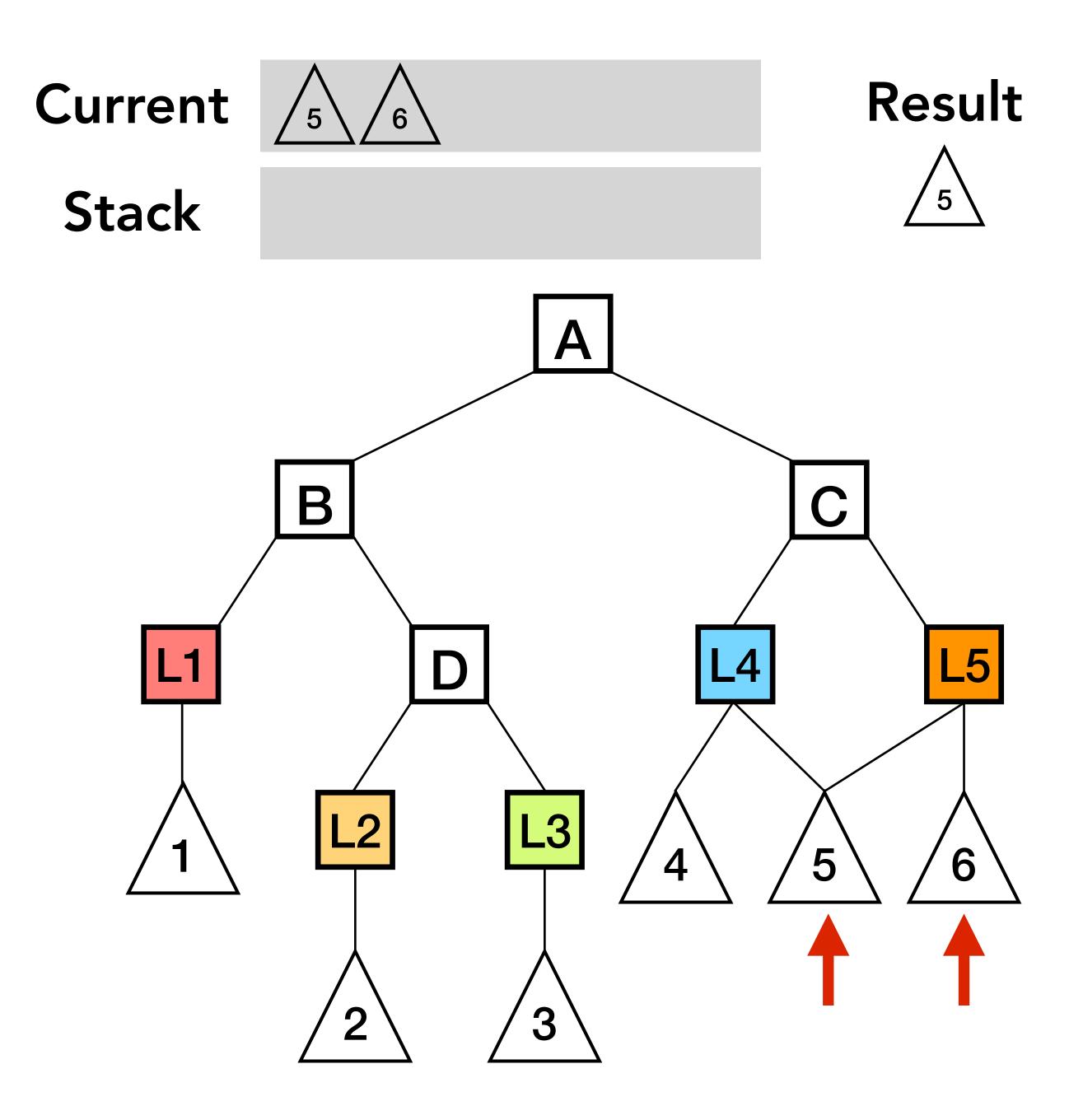








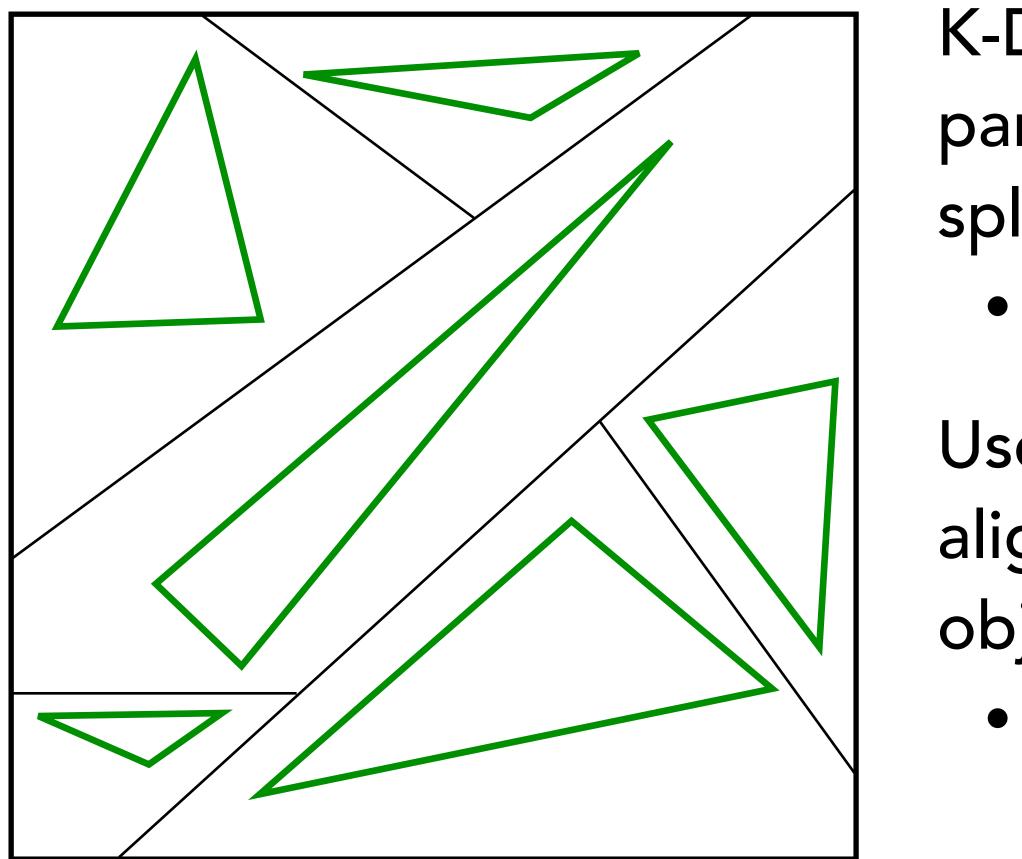








## **Binary Space Partitioning Tree**



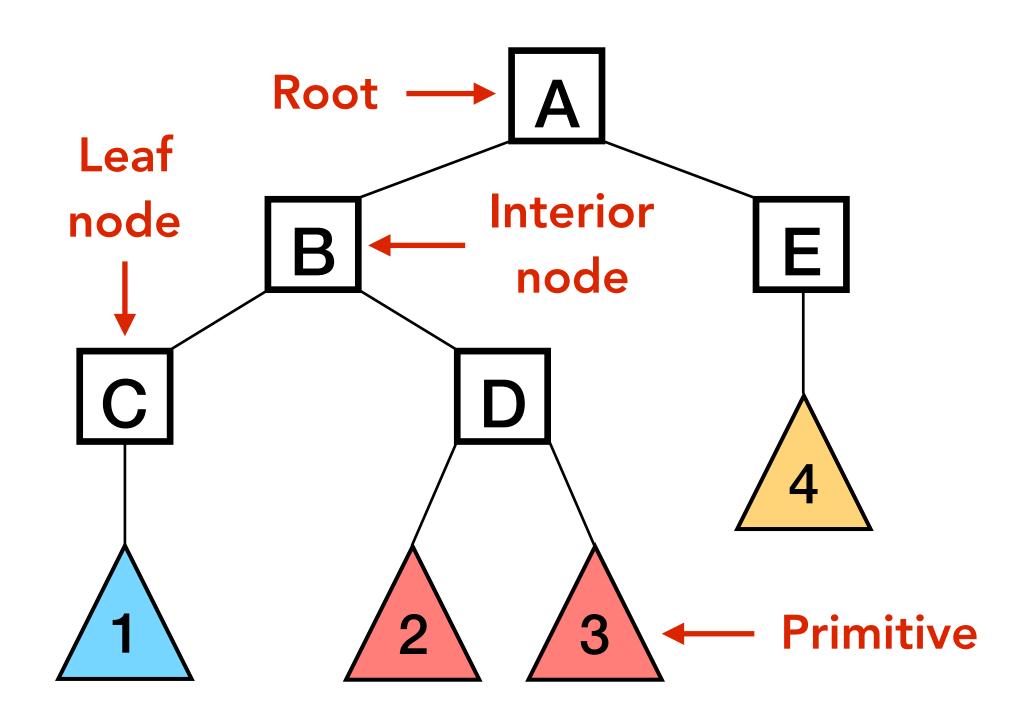
- K-D tree is a special case of binary space partitioning (BSP) tree, which recursively split the space with planes (3D) or lines (2D)
  Arbitrary split planes here
- Useful when objects are large and non-axisaligned, in which case K-D tree will split objects into different partitions
  - Good reference: Ray Tracing with the BSP Tree [Ize, Wald, Parker, 2008]



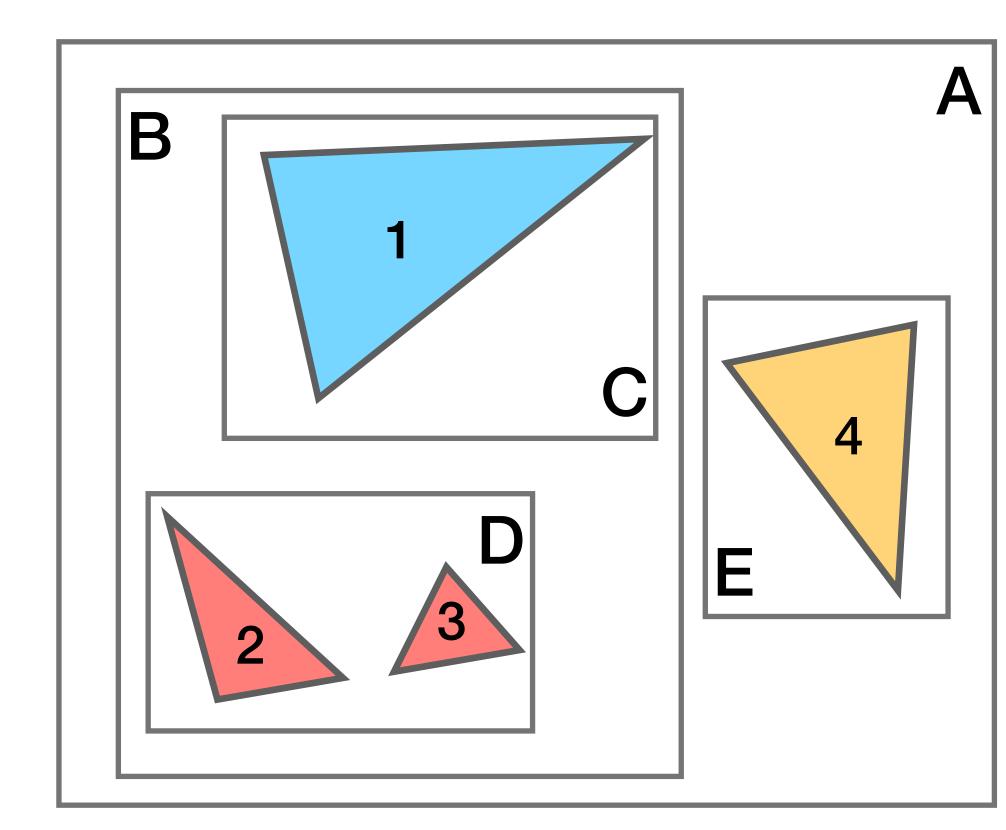


# Bounding Volume Hierarchy (Object Partition)

**BVH Tree** 



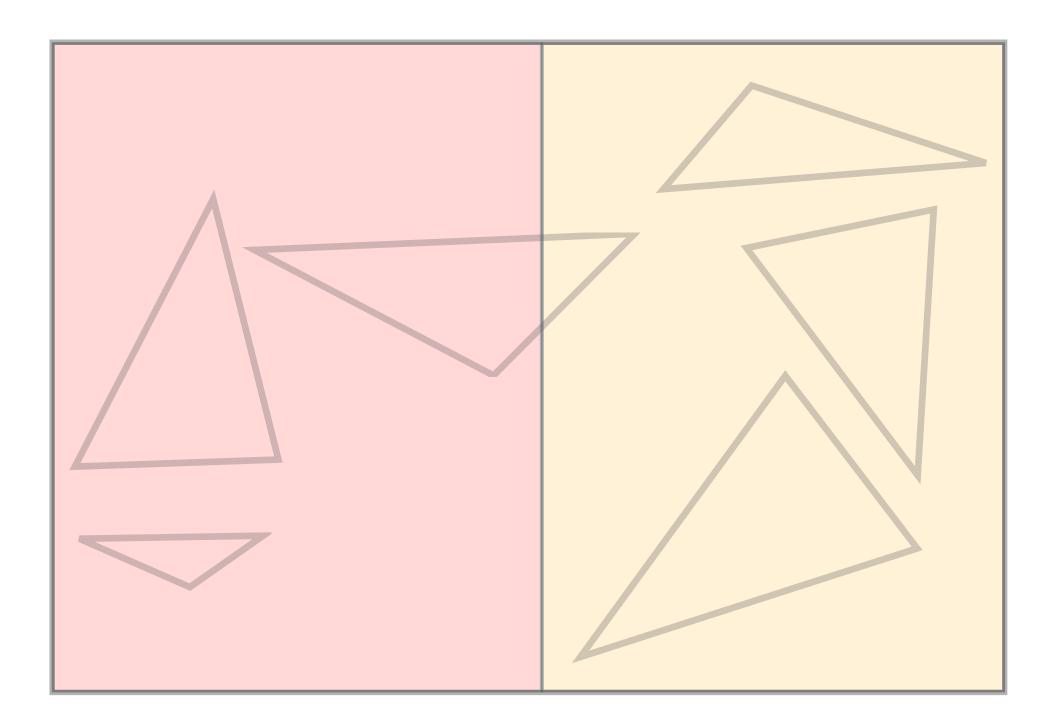
Scene



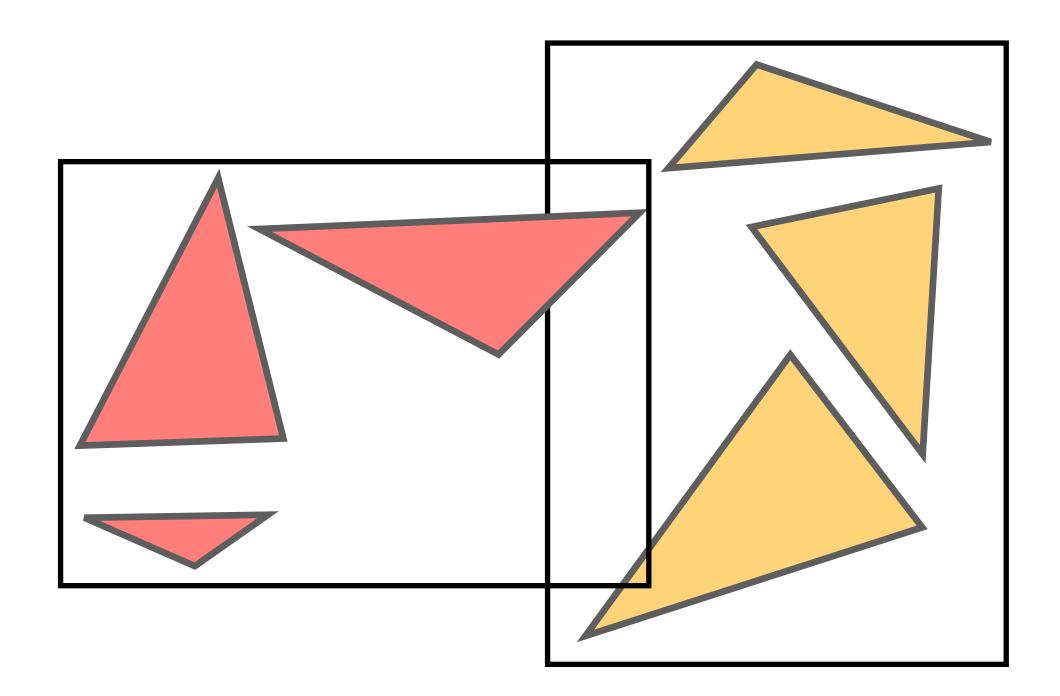


# **Object vs. Space Partitioning**

**Space partitioning**: One object could be in different partitions

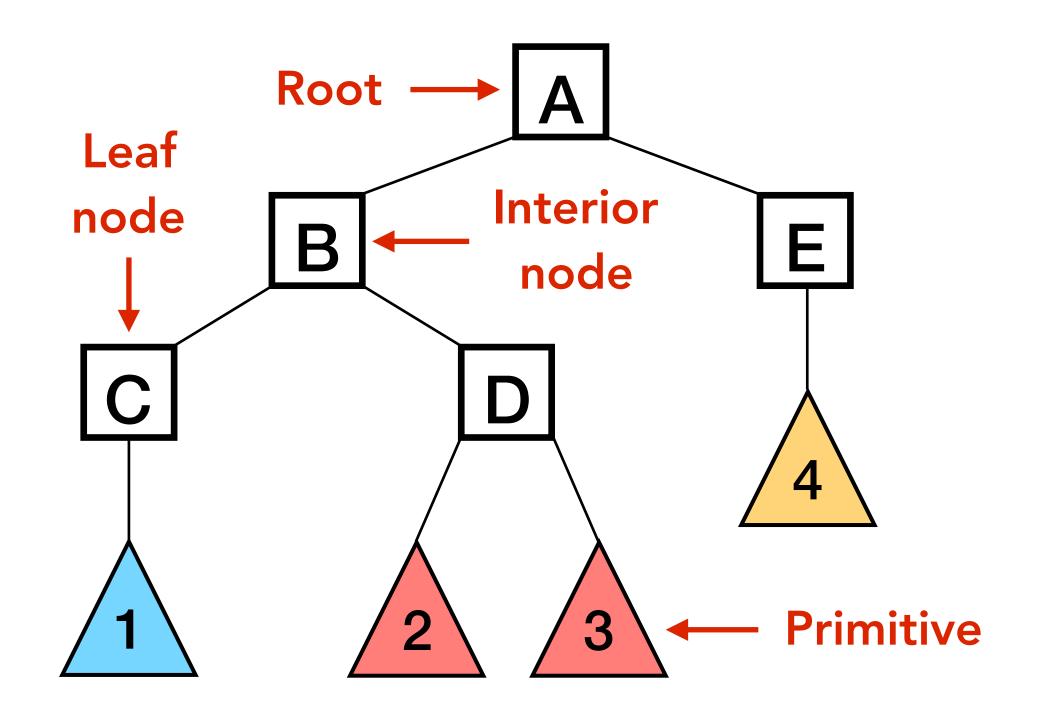


# **Object partitioning**: different partitions could overlap in space

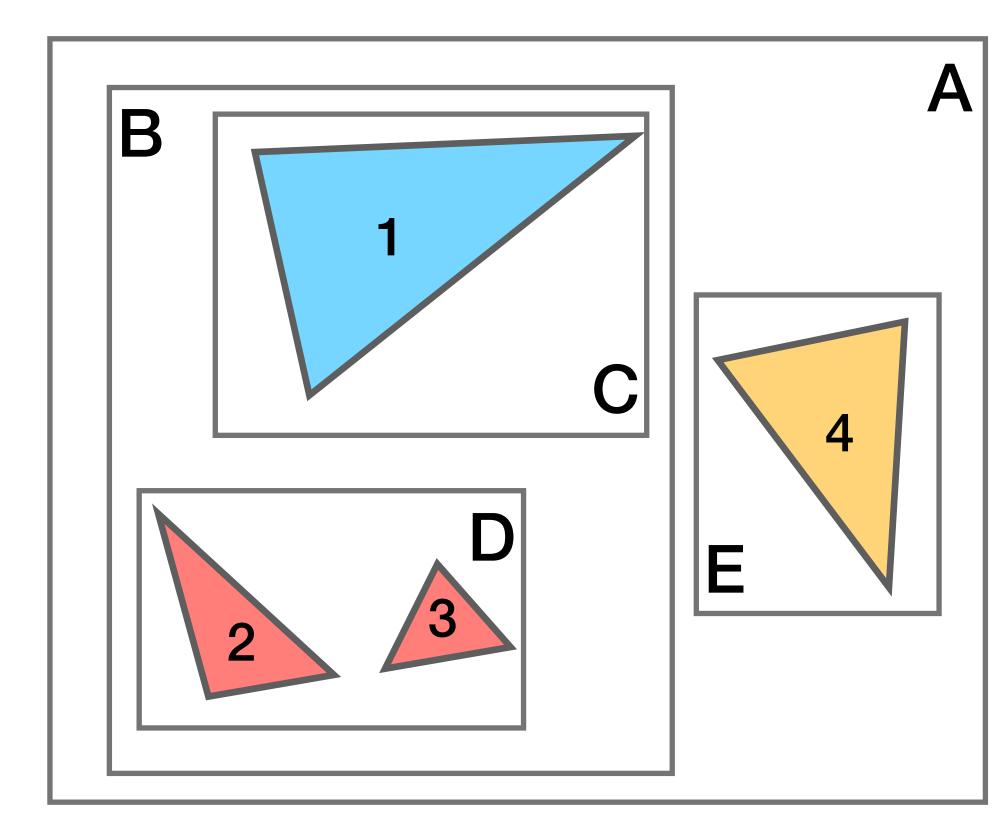




# **Bounding Volume Hierarchy** (Object Partition)



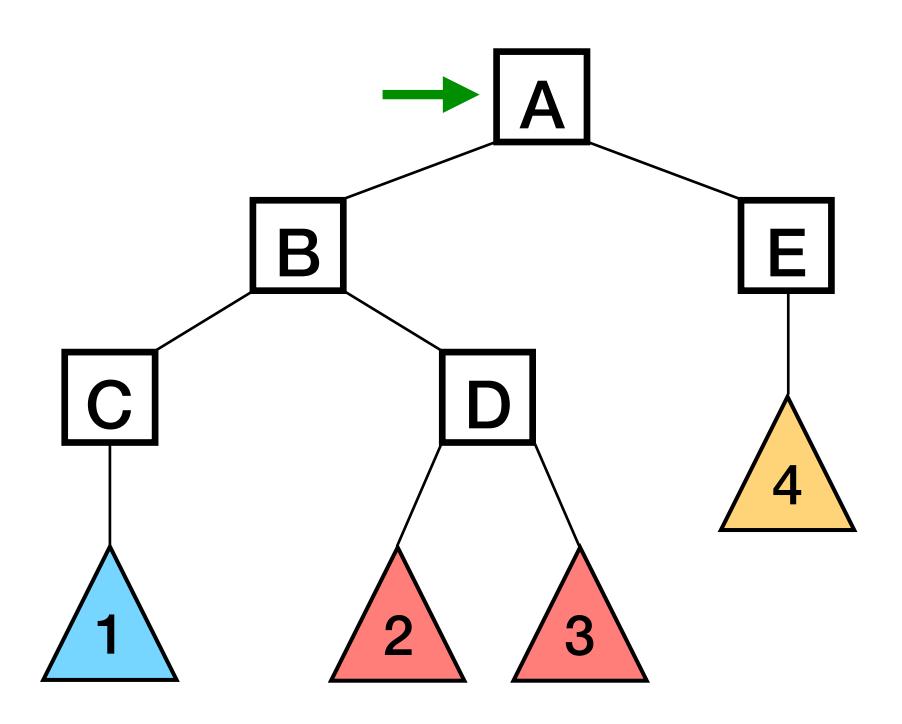
• A, B, C, D, E are the bounding volumes, which are Axis-Aligned Bounding Boxes (AABBs) here. Other (irregular) bounding volumes are possible.







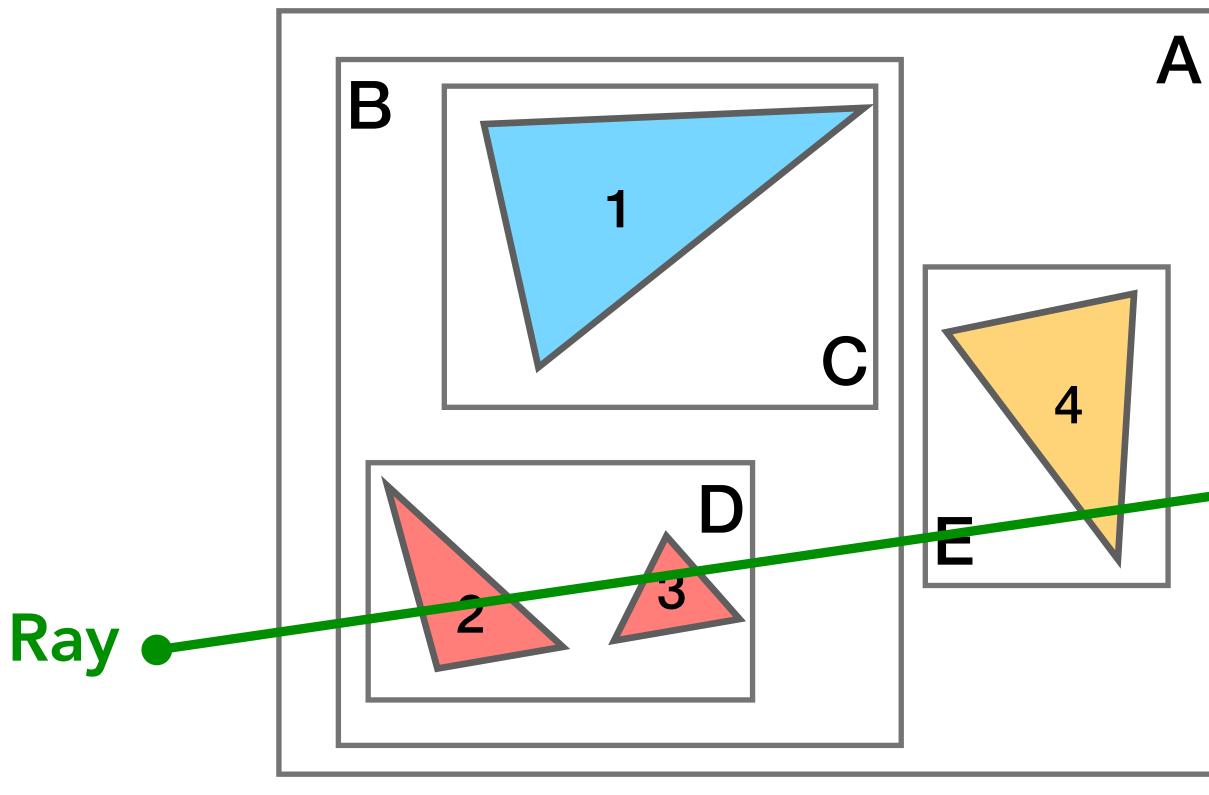
### ClosestHit = NA



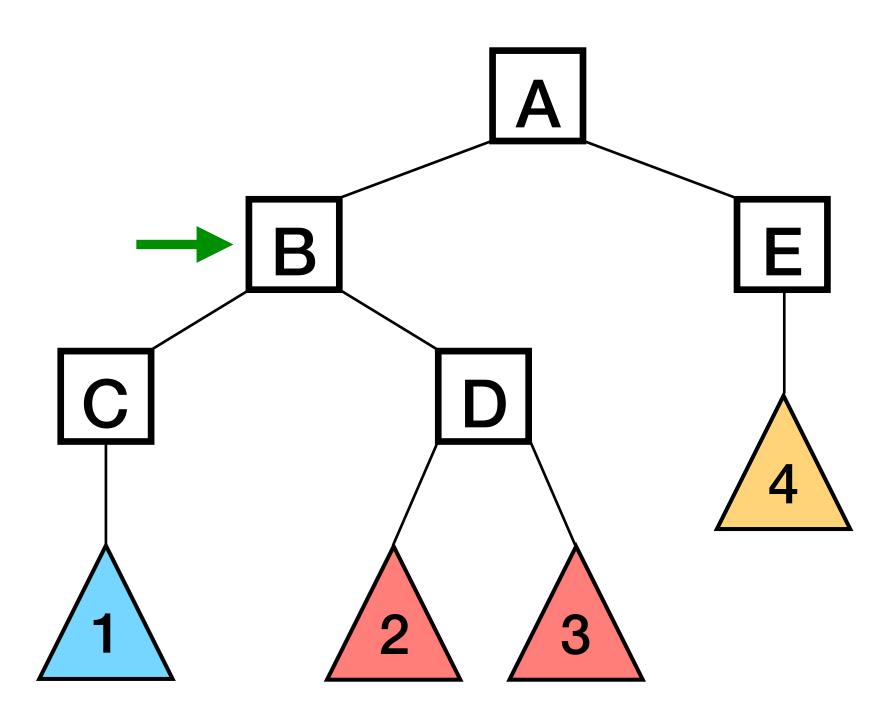
Current

### **A** Ray-AABB Intersection Test

Stack

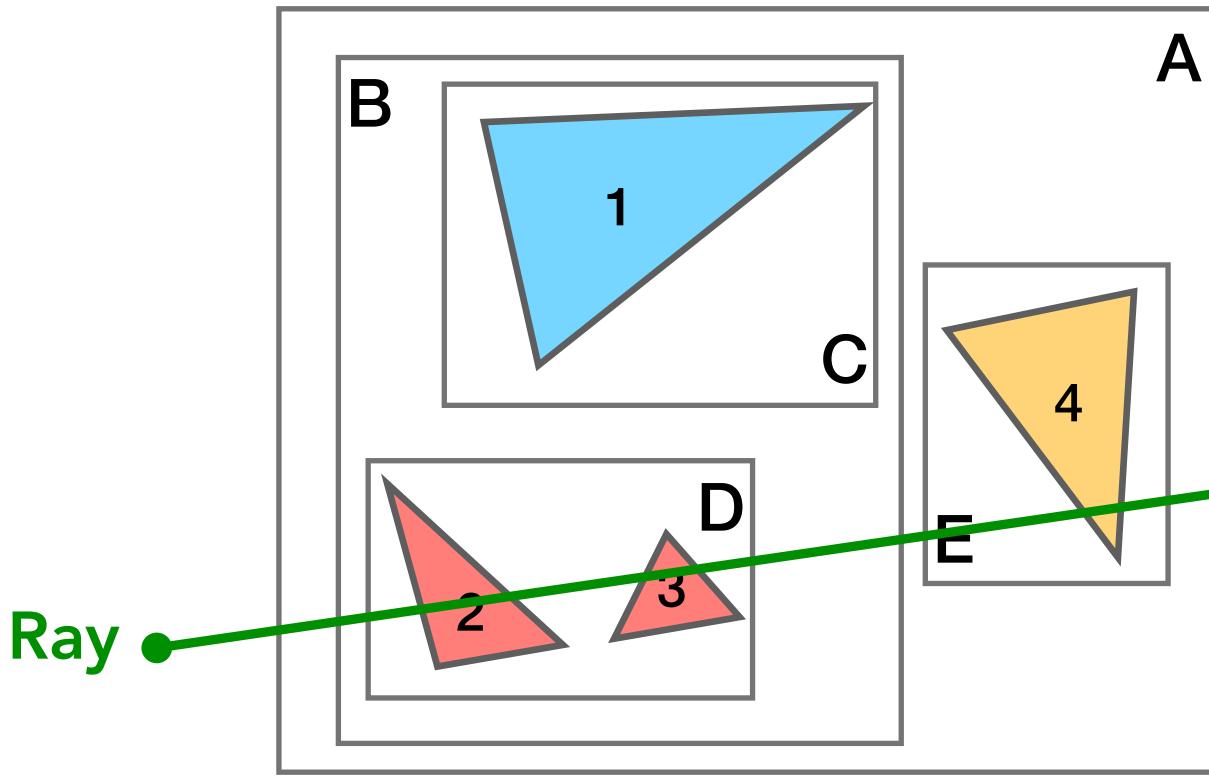




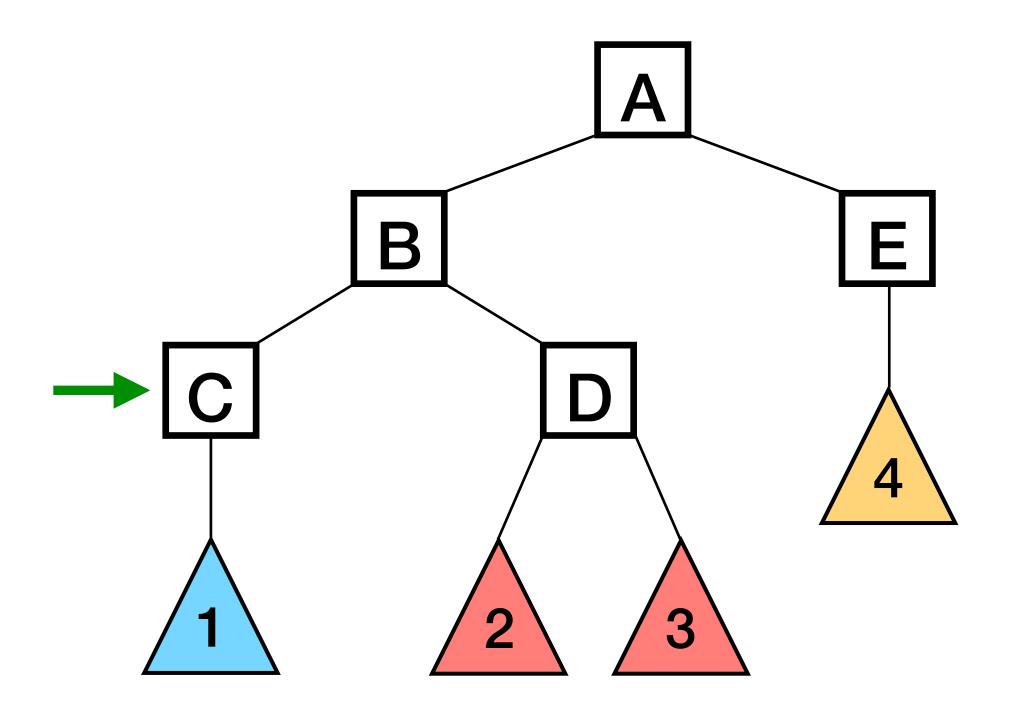


- Current
  - Stack

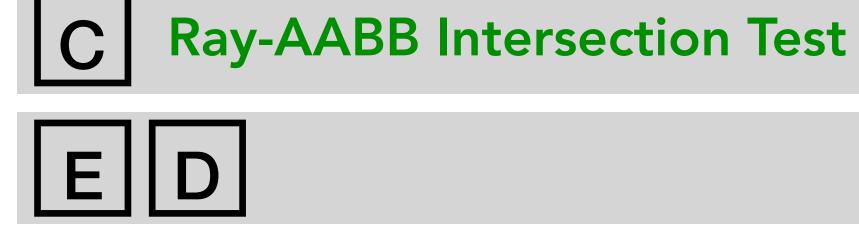


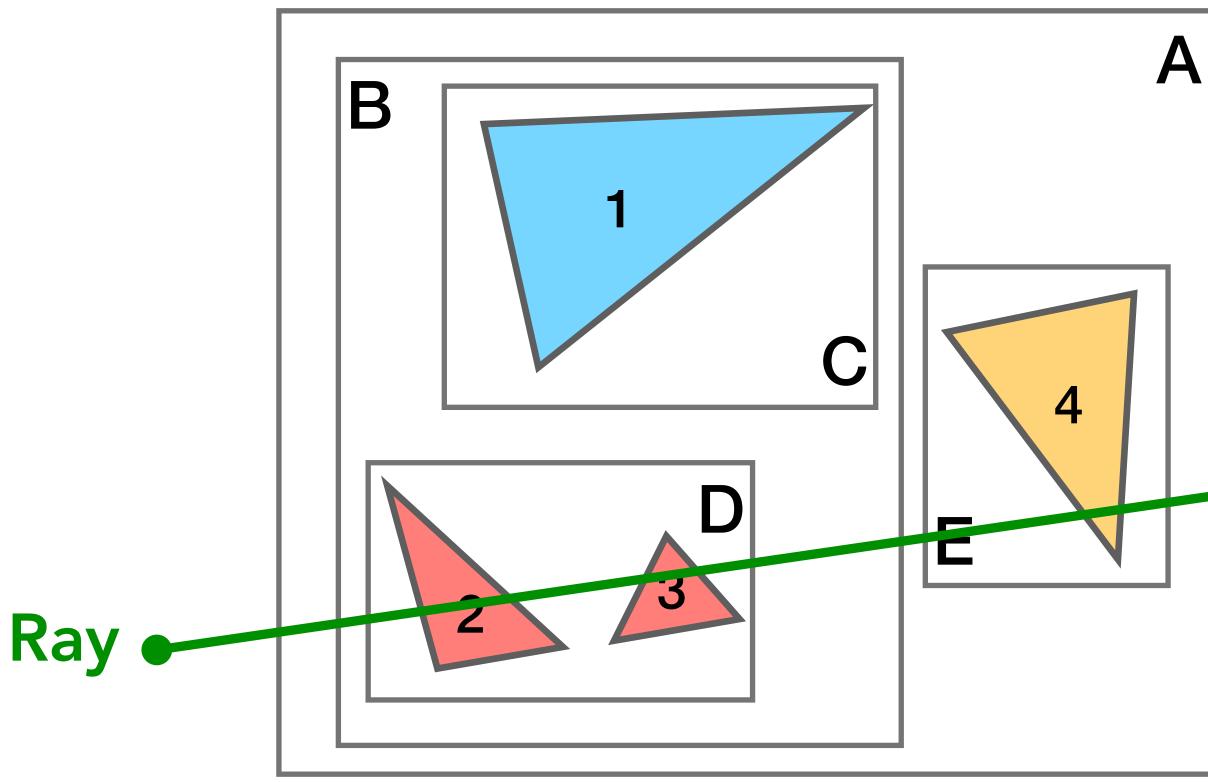




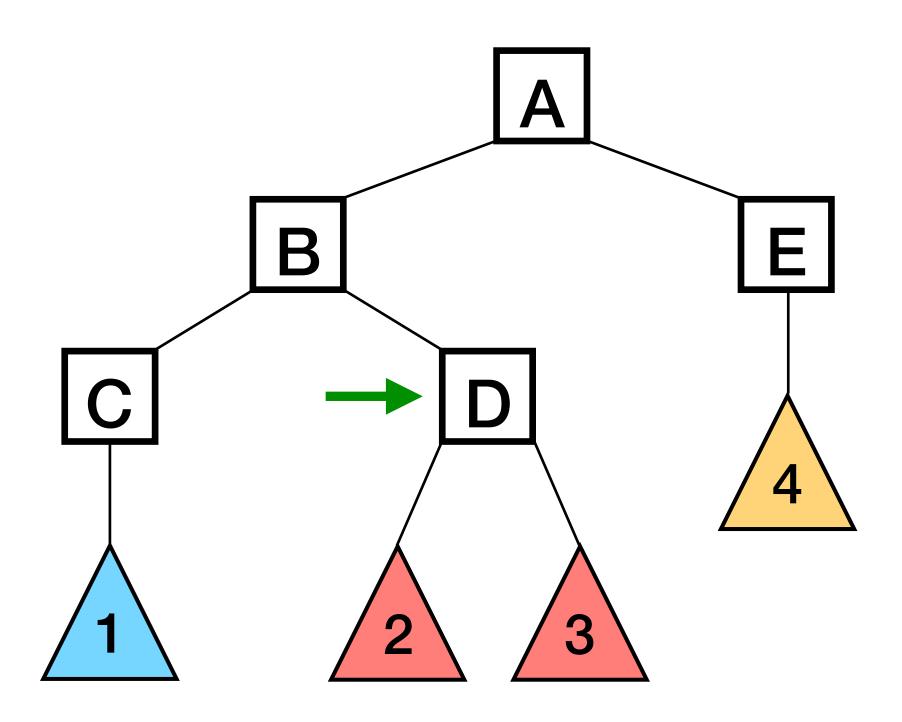


- Current
  - Stack



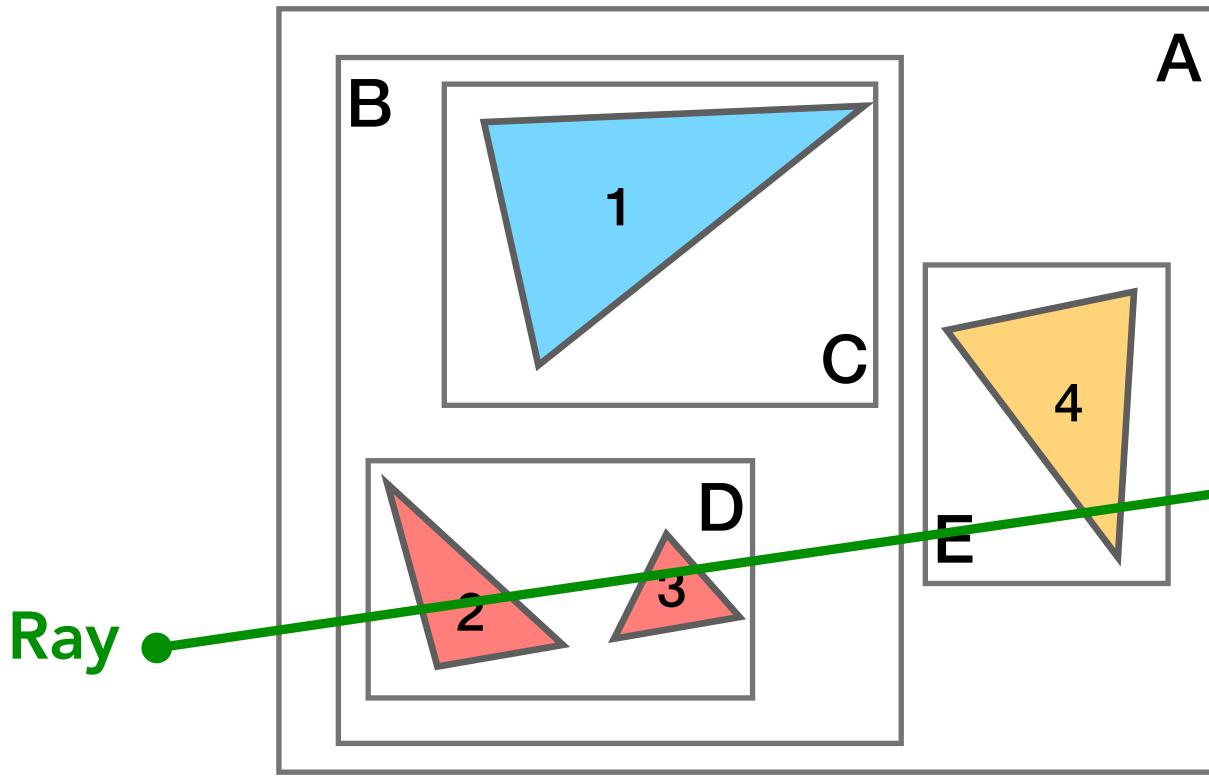




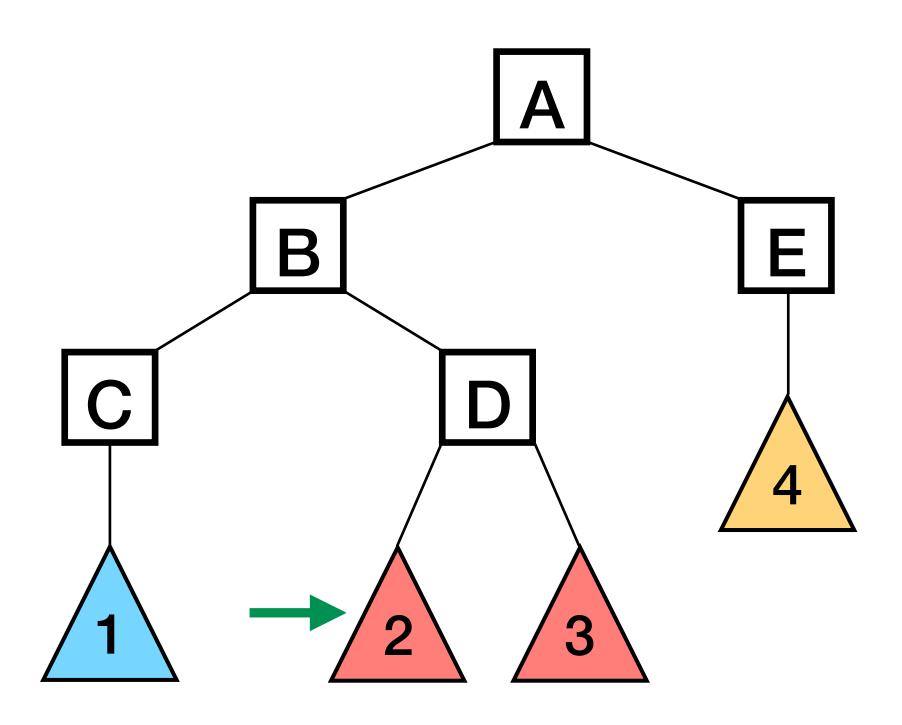


- Current
  - Stack



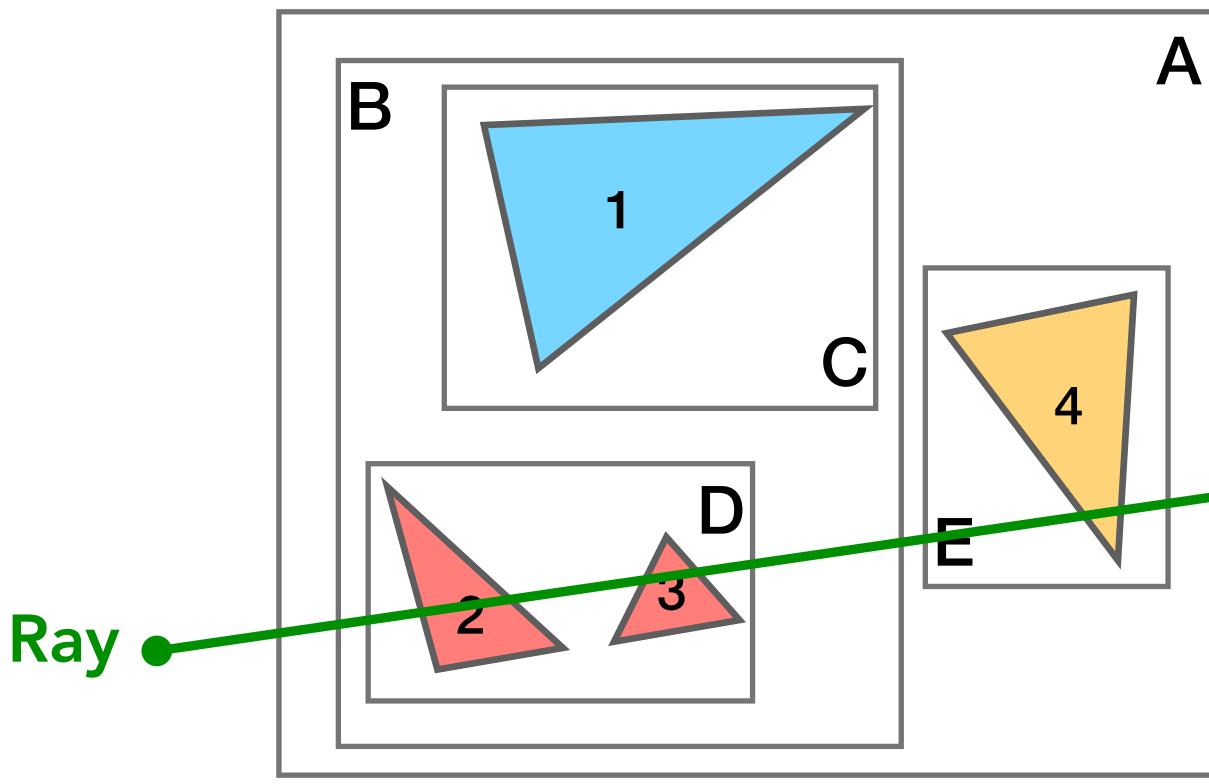






- Current
  - Stack

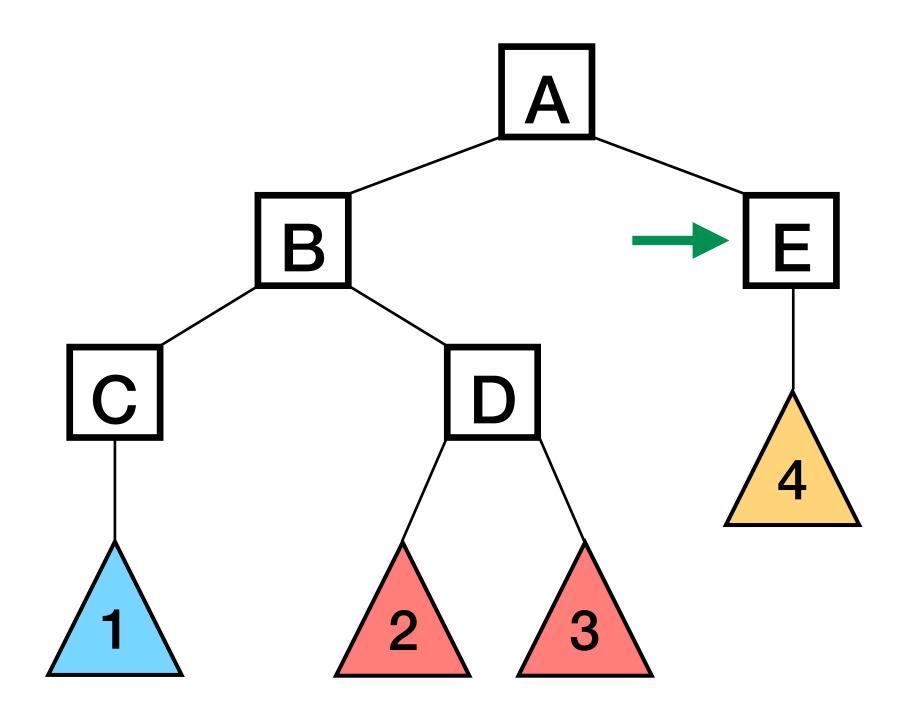






ClosestHit = 2

Distance to E > Distance to 2; Stop!

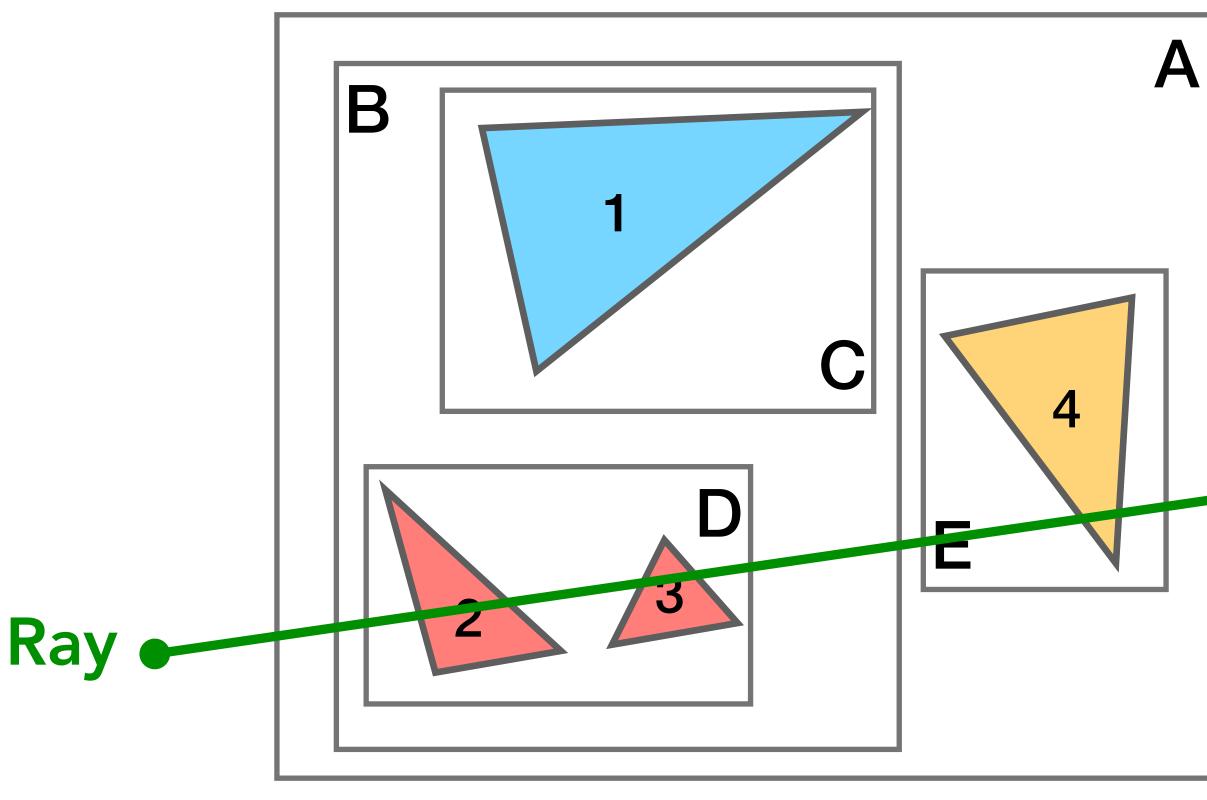


# Intersection Test Using BVH

Current

### **Ray-AABB Intersection Test** IEI.

Stack



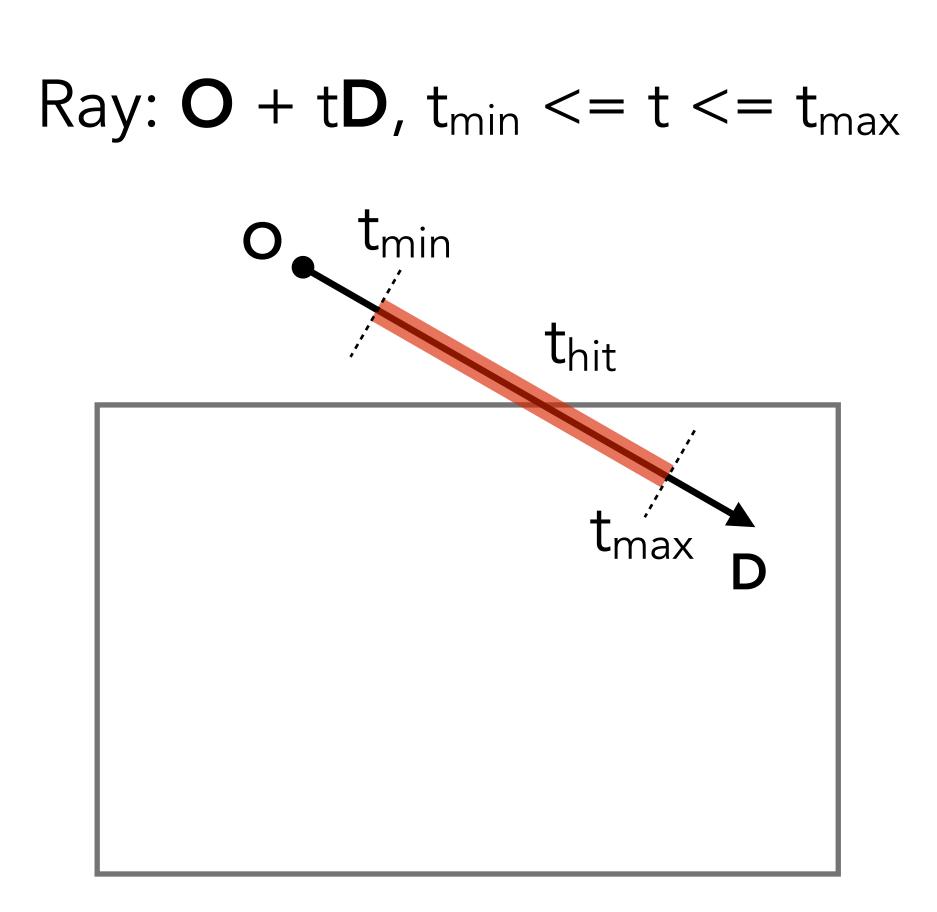


# **Ray-AABB** Intersection

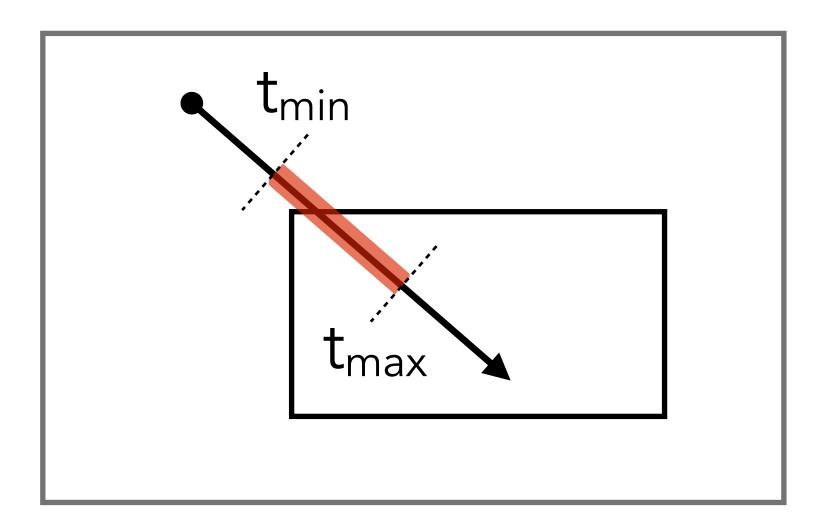
# Ray: $\mathbf{O} + t\mathbf{D}$ , $t_{min} \le t \le t_{max}$ 0 t<sub>min</sub> t<sub>hit</sub> t<sub>max</sub> D



# A Subtle but Critical Case



### Should this be counted as a hit? Yes; any ray segment that originates from within an AABB must be treated as intersecting.





## Various Trade-offs Worth Considering

Time to build the tree vs. time to search.

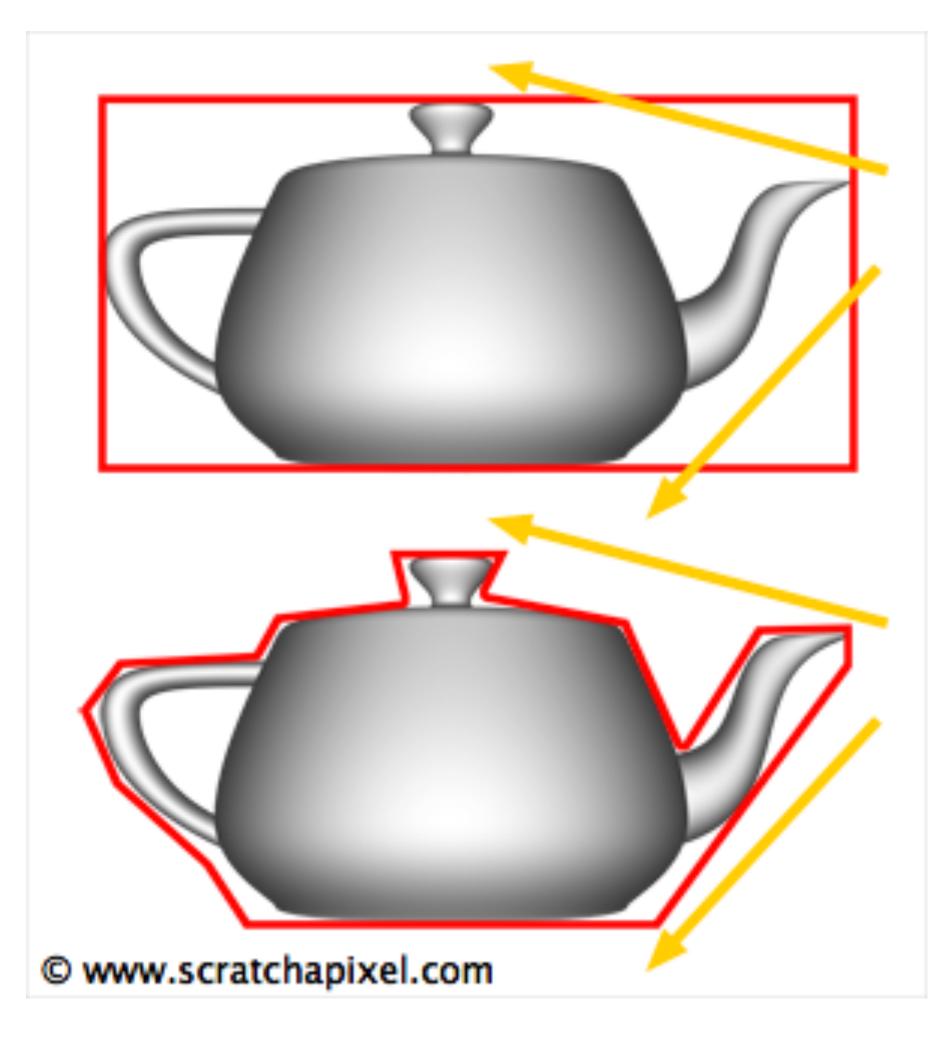
- Incrementally update a tree (e.g., scene) slowing changing in an animation)?
- Can we built the tree offline?

Shape of the bounding volume.

• Tight bounding volumes provide more precise intersect test, but are costly to build and to search.

Tree structures take memory.

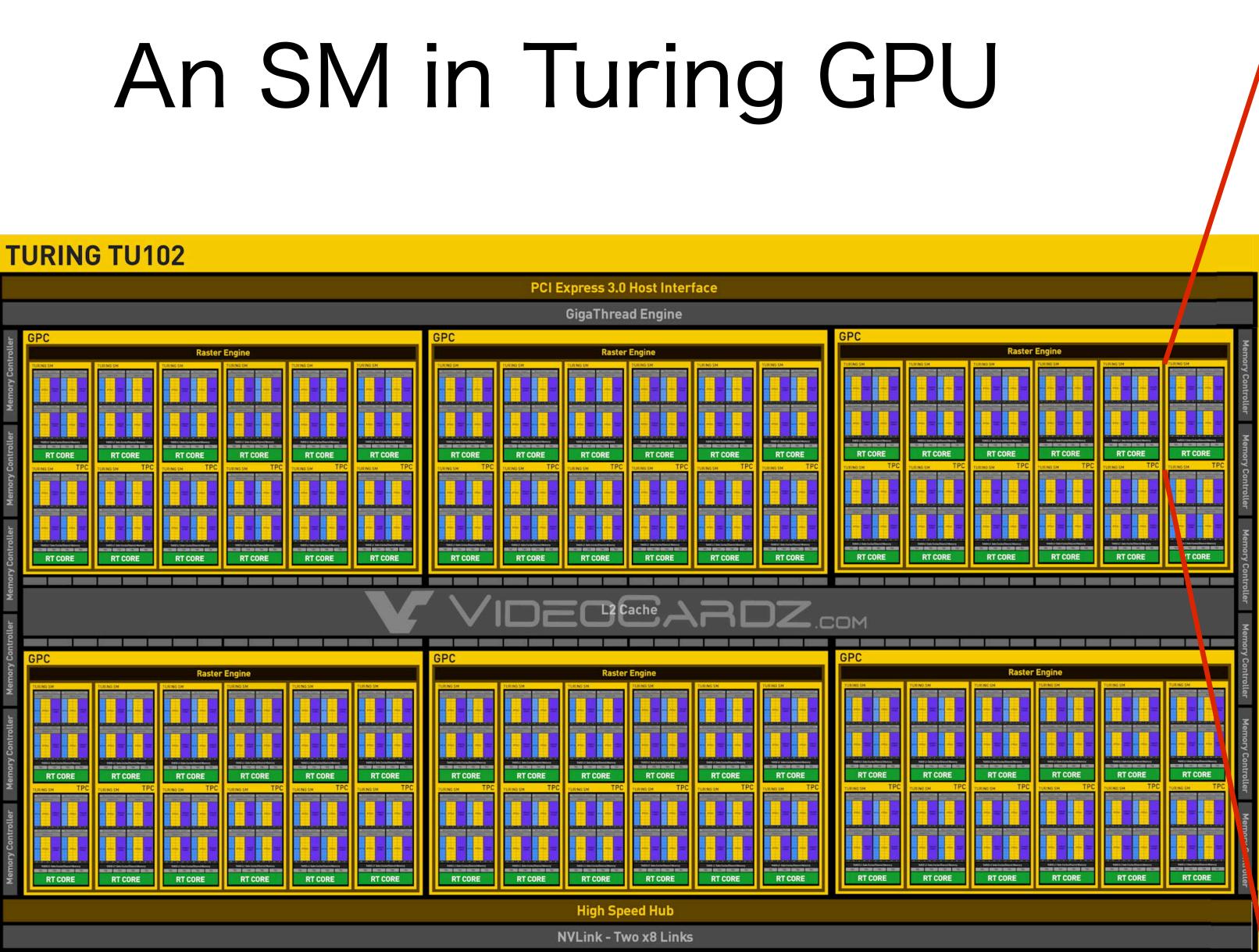


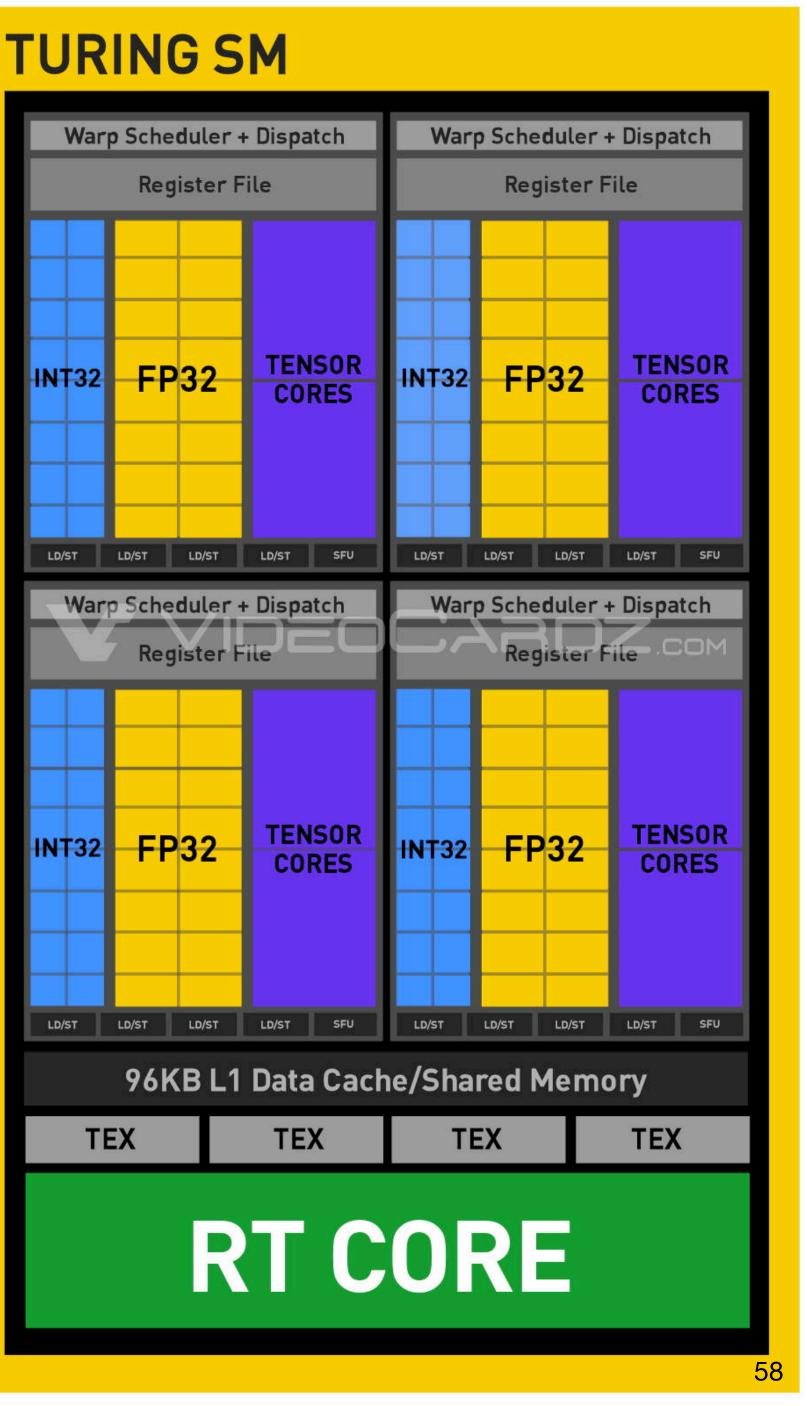


https://www.scratchapixel.com/lessons/advanced-rendering/introduction-acceleration-structure/bounding-volume-hierarchy-BVH-part1 57







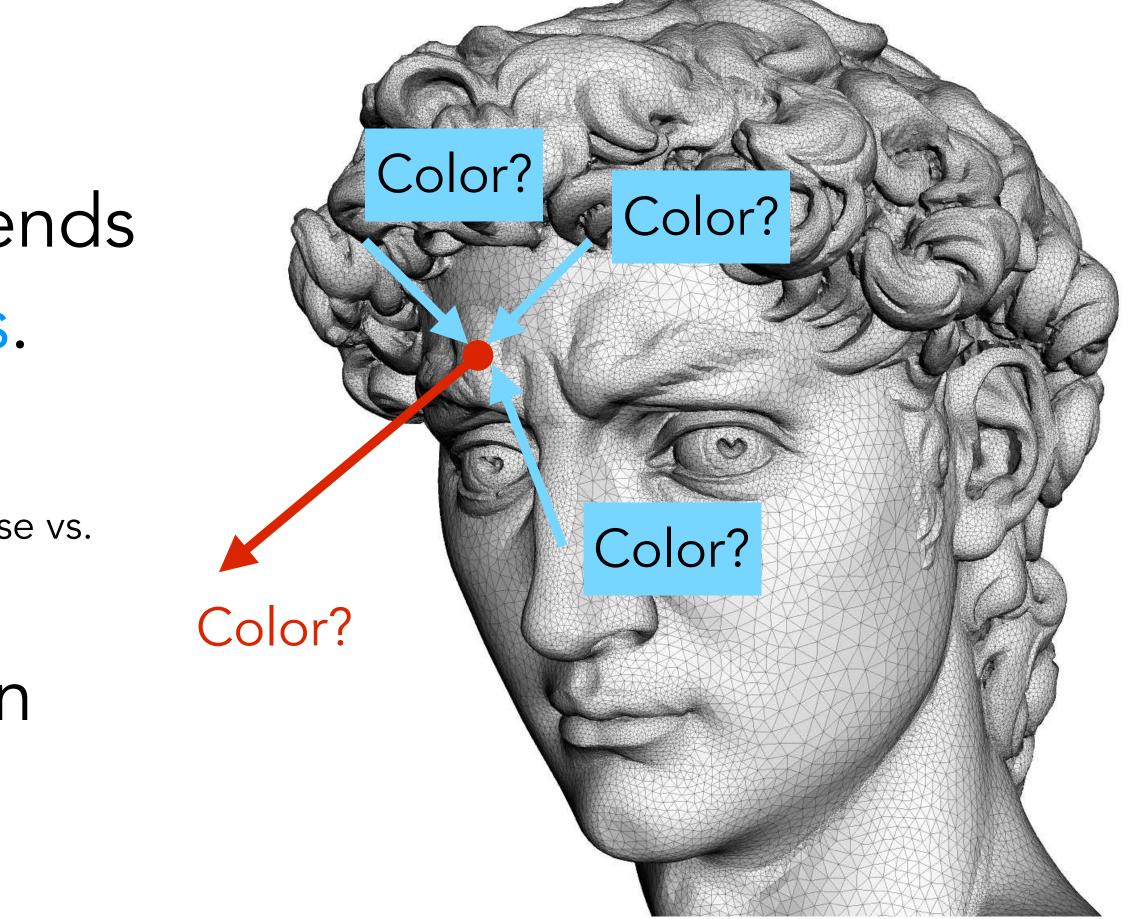


# **Recursive Ray Tracing**



# Why Recursive Ray Tracing?

- To implement realistic shading.
- The color of an exiting ray depends on the colors of all incident rays.
  - color here really means radiance.
  - also depends on the surface material (diffuse vs. specular vs. ...); later.
- How do we know the color of an incident ray? Cast more rays!



Valette, et al. [TVCG'08]



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Secondary Ray Secondary Ray Secondary Ray

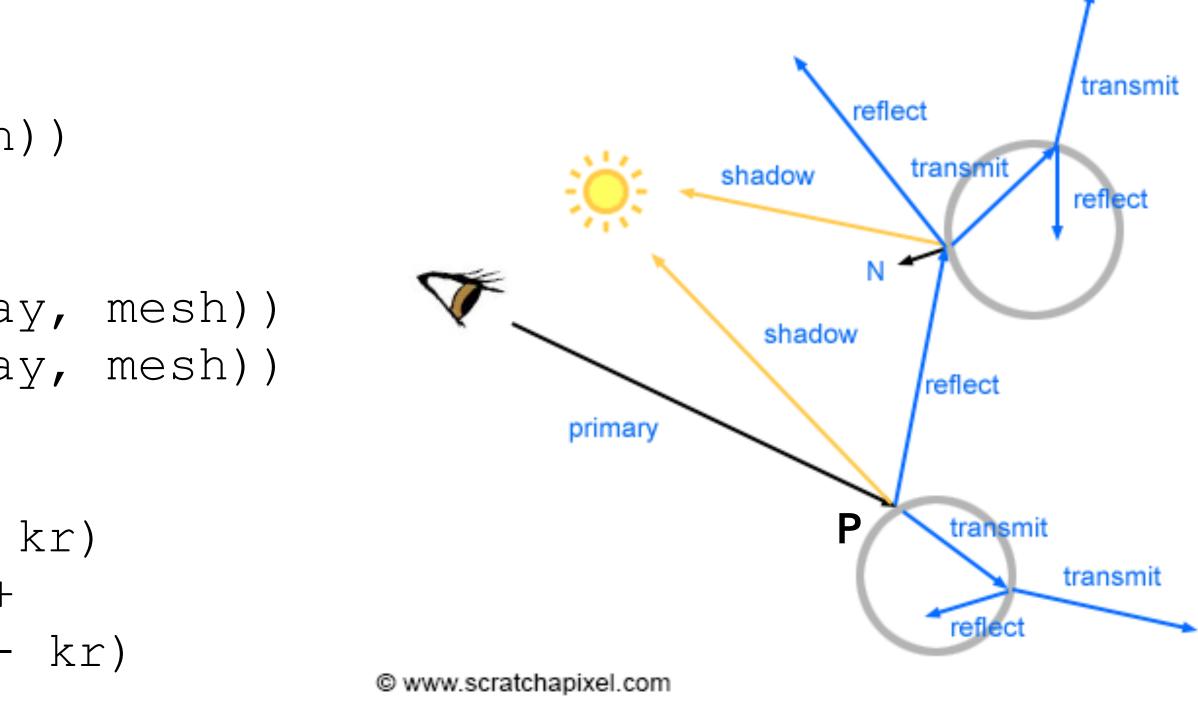
Valette, et al. [TVCG'08]



## Simple Whitted-Style Recursive Ray Tracing

A simplification of <u>Whitted-style ray tracing</u>, assuming purely transparent surface.

castRay(ray, mesh) { if (P = nearestIntersect(ray, mesh)) reflectRay = buildReflectRay(P) refractRay = buildRefractRay(P) **reflectColor** = castRay(reflectRay, mesh)) refractColor = castRay(refractRay, mesh)) float kr fresnel(dir, N, hitObject->ior, kr) P.color = reflectionColor \* kr + refractionColor \* (1 - kr) else P.color = backgroundColor

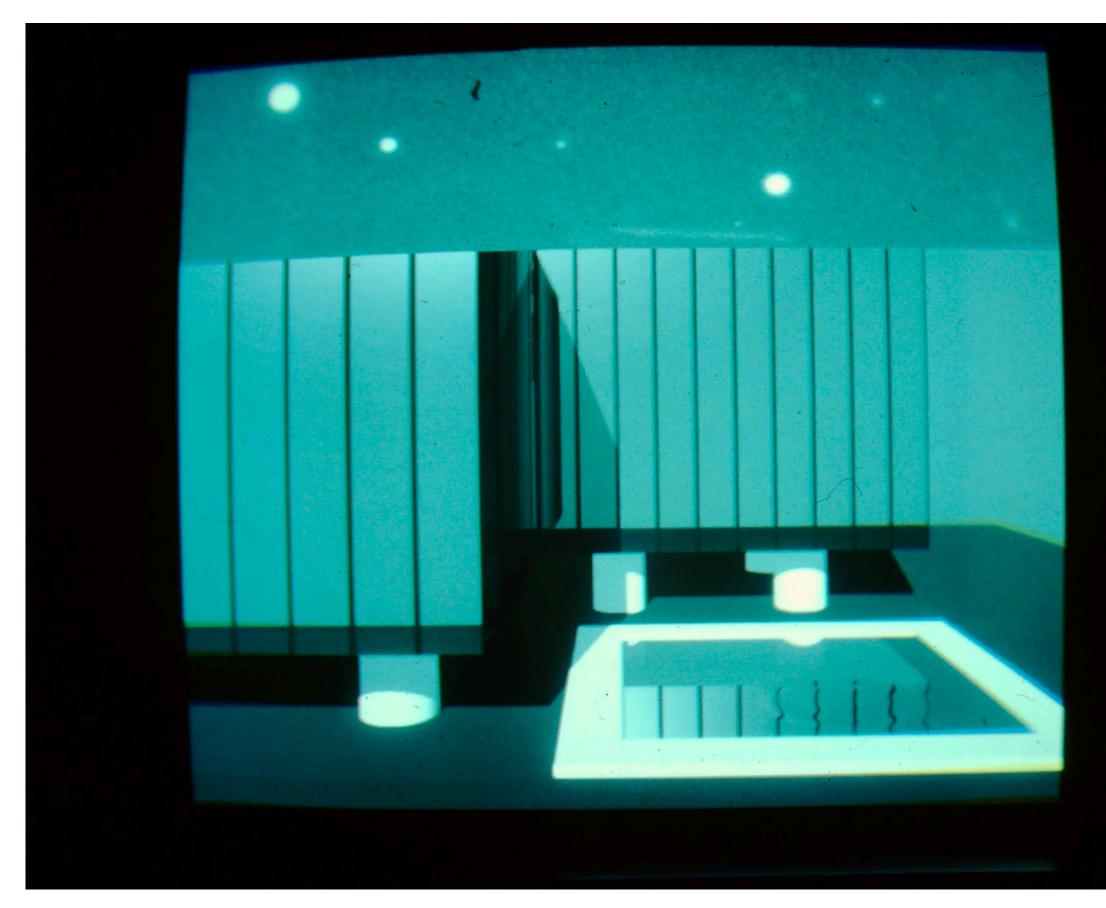


https://www.scratchapixel.com/lessons/3d-basic-rendering/ray-tracing-overview/light-transport-ray-tracing-whitted

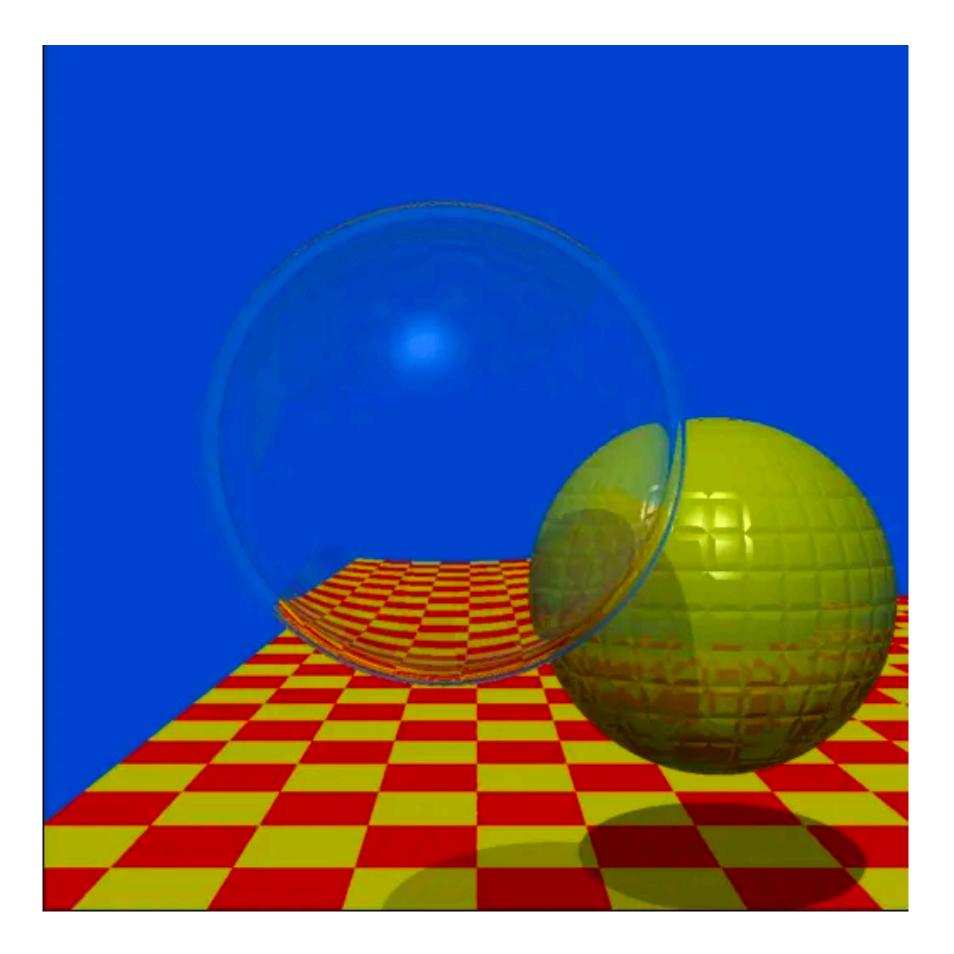




## Simple Whitted-Style Recursive Ray Tracing







https://blogs.nvidia.com/blog/2018/08/01/ray-tracing-global-illumination-turner-whitted/





## Things to Remember

Ray tracing makes it easy (conceptually) to implement realistic shading.

Compared to rasterization, ray tracing is much more time consuming, dominated by ray-scene intersection test, which is exacerbated by the need for recursive ray tracing.

We can accelerate the testing using acceleration structures that prune the search space. BVH is the most common acceleration structure.

Modern GPUs, while traditionally optimized for rasterization, now have hardware support for ray tracing (e.g., BVH traversal, ray-AABB/triangle intersection test).

