

# Using Simple Page Placement Policies to Reduce the Cost of Cache Fills in Coherent Shared-Memory Systems\*

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## Abstract

*The cost of a cache miss depends heavily on the location of the main memory that backs the missing line. For certain applications, this cost is a major factor in overall performance. We report on the utility of OS-based page placement as a mechanism to increase the frequency with which cache fills access local memory in distributed shared memory multiprocessors. Even with the very simple policy of first-use placement, we find significant improvements over round-robin placement for many applications on both hardware- and software-coherent systems. For most of our applications, first-use placement allows 35 to 75 percent of cache fills to be performed locally, resulting in performance improvements of up to 40 percent with respect to round-robin placement. We were surprised to find no performance advantage in more sophisticated policies, including page migration and page replication. In fact, in many cases the performance of our applications suffered under these policies.*

## 1 Introduction

Most modern processors use caches to hide the growing disparity between processor and memory (DRAM) speeds. On a uniprocessor, the effectiveness of a cache depends primarily on the hit rate, which in turn depends on such factors as cache and working set sizes, the amount of temporal and spatial locality in the reference stream, the degree of associativity in the cache, and the cache replacement policy.

Two additional factors come into play on a multiprocessor. First, we need a *coherence protocol* to ensure that processors do not access stale copies of data that have been modified elsewhere. Coherence is required for correctness, but may reduce the hit rate (by invalidating lines in some caches when they are modified in others), and can increase the cost of both hits and misses, by introducing extra logic into the cache lookup algorithm. Second, because

large-scale machines generally distribute physical memory among the nodes of the system, the cost of a cache miss can vary substantially, even without coherence overhead.

Minimizing the cost of coherence is arguably the most difficult task faced by the designers of large-scale multiprocessors. Given a good coherence protocol, however, the placement of data in the distributed main memory may still have a significant impact on performance, because it affects the cost of cache misses. A substantial body of research has addressed the development of good coherence protocols. This paper addresses the main-memory placement problem. We focus our attention on *behavior-driven* OS-level movement of pages between processors. We limit our consideration to the class of machines in which each physical memory address has a fixed physical location (its *home node*), and in which the hardware cache controllers are capable of filling misses from remote locations.

Ideally, the compiler for a parallel language would determine the best location for each datum at each point in time. Most current compilers, however, employ a programmer-specified data distribution (e.g. as in HPF [12]). Moreover, there will always be important programs for which reference patterns cannot be determined at compile time, e.g. because they depend on input data [13]. Even when compile-time placement is feasible, it still seems possible that OS-level placement will offer a simpler, acceptable solution. Current distributed shared memory systems use ad-hoc policies for placing shared pages in memory. For example on the Alewife multiprocessor data is placed in the memory module of the processor making the allocation call, while on DASH pages of shared data are scattered either randomly or in round-robin fashion [11].

Our work shows that we can achieve effective initial page placement with no hardware support other than the standard address translation and page fault mechanisms, and with coherence maintained either in hardware (on a CC-NUMA machine) or in kernel-level software (on a non-coherent NUMA machine). We also evaluate dynamic page migration and page replication (with invalidations for coherence) in an attempt to adapt to changes in program reference patterns, but observe little or no performance benefit and often a performance loss for our application suite.

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## 2 Related Work

Page migration and replication have been used on cache-less NUMA multiprocessors in order to take advantage of the lower cost of accessing local memory instead of remote memory [3, 5, 10]. By using efficient block-transfer hardware to transfer page-size blocks, these “NUMA memory management” systems reduce the average cost per reference. This paper addresses the question of whether similar policies are still effective on machines with coherent caches.

Cache-coherent shared memory multiprocessors fall into two basic categories, termed CC-NUMA (cache coherent, non-uniform memory access) and COMA (cache only memory architecture). CC-NUMA machines include the Stanford DASH [11], the MIT Alewife [1], and the Convex SPP-1000, based on the IEEE Scalable Coherent Interface standard [7]. COMA machines include the Kendall Square KSR 1 and the Swedish Data Diffusion Machine (DDM) [6]. COMA machines organize main memory as a large secondary or tertiary cache, giving them a performance advantage over CC-NUMA machines when it comes to servicing capacity and conflict cache misses. Past work [15] has shown, however, that with additional hardware, or programmer and compiler intervention, data pages on a CC-NUMA machine can be migrated to the nodes that would miss on them the most, achieving performance comparable to that of COMA machines, at lower hardware cost. Our approach is applicable to both NUMA machines with non-coherent caches and CC-NUMA machines, and requires little or no special hardware.

Chandra *et. al.* have independently studied migration in the context of coherence [4]. They simulated several migration policies based on counting cache misses and/or TLB misses; some of the policies allowed a page to move only once; others permitted multiple migrations. One of their policies (single move on the first cache miss) is similar to our placement policy. They also found that a single-move policy can cause many cache misses to be performed locally, though our results are not directly comparable because we used different applications. We extend their work by considering replication strategies, as well as investigating the effects of placement on both eager (hardware) and lazy (software) coherent systems.

## 3 Algorithms and Methodology

### 3.1 Simulation Infrastructure

We use execution driven simulation to simulate a mesh-connected multiprocessor with up to 64 nodes. Our simulator consists of two parts: a front end, Mint [16], which simulates the execution of the processors, and a back end

System Constant Name	Default Value
TLB size	128 entries
TLB fill time	100 cycles
Interrupt (page fault) cost	140 cycles
Page table modification	320 cycles
Memory latency	12 cycles
Memory bandwidth	1 word / 4 cycles
Page size	4K bytes
Total cache per processor	16K bytes
Cache line size	64 bytes
Network path width	16 bits (bidirectional)
Link latency	2 cycles
Routing time	4 cycles
Directory lookup cost	10 cycles
Cache purge time	1 cycle/line
Page move time	approx. 4300 cycles

Table 1: Default values for system parameters, assuming a 100-MHz processor.

that simulates the memory system. The front end calls the back end on every data reference (instruction fetches are assumed to always be cache hits). The back end decides which processors block waiting for memory and which continue execution. Since the decision is made on-line, the back end affects the timing of the front end, so that the control flow of the application, and the interleaving of instructions across processors, can depend on the behavior of the memory system.

The front end implements the MIPS II instruction set. Interchangeable modules in the back end allow us to explore the design space of software and hardware coherence. Our hardware-coherent modules are quite detailed, with finite-size caches, write buffers, full protocol emulation, distance-dependent network delays, and memory access costs (including memory contention). Our simulator is capable of capturing contention within the network, but only at a substantial cost in execution time; the results reported here model network contention at the sending and receiving nodes of a message, but not at the intermediate nodes. Our software-coherent modules add a detailed simulation of TLB behavior. To avoid the complexities of instruction-level simulation of interrupt handlers, we assume a constant overhead for page fault interrupt handling. We have chosen to simulate small caches in order to capture the impact of eviction misses. Page placement becomes significantly more important when an application’s working set does not fit in the cache. In such situations careful page placement can turn main memory into a large tertiary cache, significantly improving program performance. Table 1 summarizes the default parameters used in our simulations.

The CC-NUMA machine uses the directory-based write-invalidate coherence protocol of the Stanford DASH machine. Our software-coherent NUMA machine uses a more complicated, multi-writer protocol [9]. This protocol employs a variant of lazy release consistency [8], in which invalidation messages are sent only at synchronization *release* points, and processed (locally) only at synchronization *acquire* points. At an acquire, a processor is required to flush from its own cache all lines of all pages that have been modified by any other processor since the current processor’s last acquire. It is also required to unmap the page, so that future accesses will generate a page fault. At a release, a process is required to write back all dirty words in its cache.<sup>1</sup> To allow a processor to determine which pages to un-map (and flush the corresponding cache lines) on an acquire, we maintain a distributed *weak list* of pages for which out-of-date cached copies may exist. When a processor first accesses a page (or accesses it for the first time after un-mapping it), the handler for the resulting page fault adds the page to the processor’s page table and communicates with the page’s home node to update a list of sharing processors. If the only previously-existing mapping had read-write permissions, or if the current fault was a write fault and all previously-existing mappings were read-only, then the page is added to the weak list.

### 3.2 Page Placement Mechanisms

The changes required to add page placement to both the hardware and software coherence protocols were straightforward. The basic idea is that the first processor to touch a given page of shared memory becomes that page’s home node. To deal with the common case in which one processor initializes all of shared memory before parallel computation begins, we created an executable “done with initialization” annotation that programmers can call at the point at which the system should begin to migrate (place) pages. In anticipation of programs in which the pattern of accesses to shared memory might undergo a major change in the middle of execution, we also created a “phase change” annotation that programmers could call when the system should re-evaluate its placement decisions.

At the beginning of execution, shared memory pages are unmapped (this was already true for the software protocol, but not for the hardware one). The first processor to suffer a page fault on a page (or the first one after initialization or a phase change) becomes the page’s home node. That processor requests the page from the current home, then blocks until the page arrives.

Ideally, one would want to place a page on the processor

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<sup>1</sup>Because there may be multiple dirty copies of a given line, non-dirty words must *not* be written back. To distinguish the dirty words, we assume that the cache includes per-word dirty bits.

that will suffer the most cache misses for that page. Unfortunately, this is not possible without future knowledge, so we place a page based on its past behavior. We simulated a policy, based on extra hardware, in which the first processor to perform  $n$  cache fills on a page becomes the page’s home node, but found no significant improvement over the “first reference” policy. The first reference policy does not attempt to determine which processor uses a page the most, but does ensure that no processor is home to pages that it does not use.

### 3.3 Application Suite

Our application suite consists of five programs. Two (`sor` and `mgrid`) are locally-written kernels. The others (`mp3d`, `appbt`, and `water`) are full applications.

`SOR` performs banded red-black successive over-relaxation on a  $640 \times 640$  grid to calculate the temperature at each point of a flat rectangular panel. We simulated 10 iterations. `Mgrid` is a simplified shared-memory version of the multigrid kernel from the NAS Parallel Benchmarks [2]. It performs a more elaborate over-relaxation using multigrid techniques to compute an approximate solution to the Poisson equation on the unit cube. We simulated 2 iterations, with 5 relaxation steps on each grid, and grid sizes from  $64 \times 64 \times 32$  down to  $16 \times 16 \times 8$ .

`Mp3d` is part of the SPLASH suite [14]. It simulates rarefied fluid flow using a Monte Carlo algorithm. We simulated 20,000 particles for 10 time steps. `Water`, also from the SPLASH suite, simulates the evolution of a system of water molecules by numerically solving the Newtonian equations of motion at each time step. We simulated 256 molecules for 5 time steps.

`Appbt` is from the NAS Parallel Benchmarks suite. It computes an approximate solution to the Navier-Stokes equations. We simulated a  $16 \times 16 \times 16$  grid for 5 time steps.

These applications were chosen in order to encompass various common caching and sharing behaviors. The input sizes we chose, although small (due to simulation constraints), deliver reasonable scalability for most of our applications. We deliberately kept the cache sizes small, so that the ratio between cache size and working set size would be about the same as one would expect in a full-size machine and problem. As we will show in the next section, most of the applications exhibit behavior for which dynamic page placement is beneficial.

## 4 Results

In this section we discuss results, starting with the performance impact of the simple “first touch” placement pol-

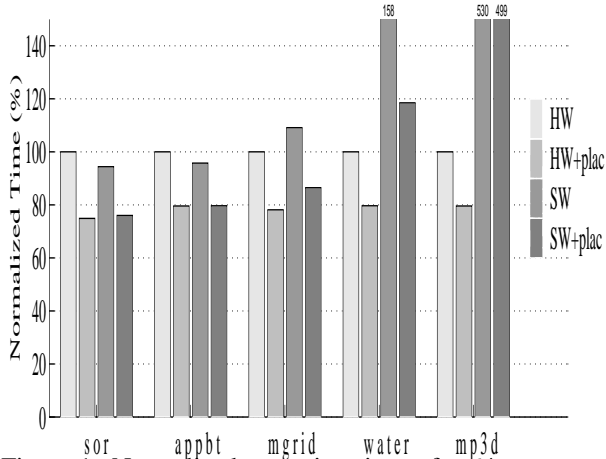


Figure 1: Normalized execution times, for 64 processors and 64-byte cache blocks.

icy. We then proceed to discuss why the more complicated policies provide no additional performance benefits.

#### 4.1 Dynamic Page Placement

In this section, we show that the “first reference” page placement scheme can result in significant performance improvements with respect to round-robin placement in both hardware- and software-coherent systems. Figure 1 shows the execution time for each of the applications in our suite, under each of the coherence systems. The times for each application are normalized so that the hardware-coherent system without dynamic placement is at 100%. For most applications, placement improves performance by 20 to 40 percent, by allowing cache misses (and, secondarily, writebacks) to happen locally.

The software and hardware coherence systems generally exhibit comparable performance both with and without dynamic placement. Our applications exhibit coarse grained sharing and therefore scale nicely under both coherence schemes. The principal exception is `mp3d`, which requires several modifications to work well on a software coherent system [9]. These modifications were not applied to the code in these experiments.

Figure 2 shows the percentage of cache misses and writebacks that occur on pages that are local after migration. Without dynamic placement, the applications in our suite satisfy less than two percent of their misses locally, as would be expected from round-robin placement on 64 processors. Dynamic placement allows 35 to 75 percent of cache misses and 50 to 100 percent of writebacks to be satisfied locally.

Figure 3 shows the average cache fill time for each application under both hardware and software coherence. Dynamic page placement reduces the average fill time by 20 to 40 percent for the hardware coherent system, and 30 to 50 percent for the software coherent system.

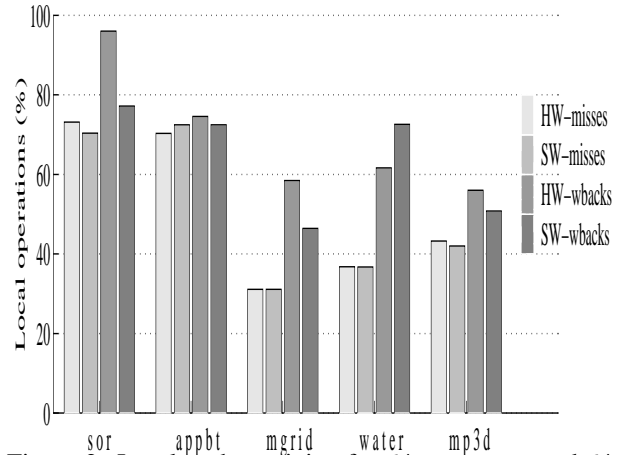


Figure 2: Local cache activity, for 64 processors and 64-byte cache blocks.

`mgrid` and `sor` are statically block-scheduled, and exhibit pair-wise sharing. They obtain a benefit from dynamic placement even for cache fills and writebacks that are *not* satisfied locally, because neighbors in the block-scheduled code tend to be physically close to one another in the mesh-based interconnection network.

In most cases, the eager hardware-coherent system benefits more from dynamic placement than does the lazy software-coherent system. Our hardware-coherent system sends invalidation messages immediately at the time of a write, and waits for acknowledgments when a lock is released. The software system sends write notices at the time of a release, and invalidates written blocks at the time of an acquire. As a result, the hardware system incurs more misses caused by false sharing, and therefore exhibits a slightly higher miss rate. Thus, any reduction in the average cost of a miss has a greater impact on the hardware system’s performance.

Our placement strategy works well for a variety of cache block sizes. Figure 4 shows the performance of the hardware system<sup>2</sup> for block sizes ranging from 16 to 256 bytes. Each bar represents the execution time of an application for a particular block size; the height of the bar is the execution time with dynamic placement relative to the execution time without it for the same block size. For example, dynamic page placement provides more performance gains for `sor` when the cache blocks are small. For programs with good spatial locality, such as `sor` and `water`, increasing the block size decreases the miss rate, reducing the relative performance gain.

For small block sizes, cold-start misses are significant, as are evictions if the working set size is greater than the cache size. Dynamic placement speeds up cold-start misses

<sup>2</sup>Similar results (not shown here) were obtained for the software system.

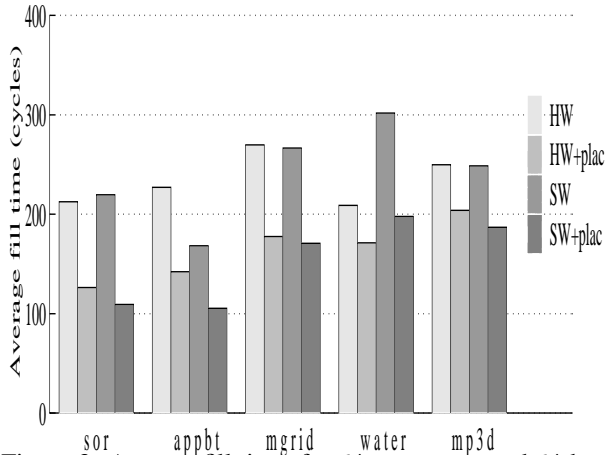


Figure 3: Average fill time, for 64 processors and 64-byte cache blocks.

by making one block transfer over the network and then performing the misses locally. Eviction misses always access blocks that were previously accessed; if the page containing those blocks is moved to the local memory, the misses can be serviced significantly faster. This is most effective if the local processor will perform more cache fills on the page than any other processor. Large cache blocks amortize the latency of a miss over a large amount of data, but are more likely to suffer from false sharing and evictions. For programs with good spatial locality, fetching large blocks reduces the miss rate but increases the cost of a miss. The miss rate is the dominant effect, making large cache blocks a net win, but the increased cost of misses mitigates this to some extent, so dynamic placement remains worthwhile.

## 4.2 Page Migration and Replication

Though dynamic placement provides a significant performance gain for many applications, it seemed likely that the reference behavior of some programs may vary significantly during execution. Therefore we provided an executable “phase change” annotation which indicates to the operating system or runtime that the program behavior has changed. In our simulations, the runtime system uses this as a signal to discard all placement decisions and allow the pages to migrate to another processor.

Most of our applications do not have well-defined phase changes. The exception is `mgrid`, because its access pattern changes as the grid size changes. Adding the phase change annotation was simple, involving only two lines of code. However, dynamic migration did not improve the performance of `mgrid`; in fact, it reduced the performance by 13 percent. This is due to the fact that in `mgrid`, each phase uses eight times as much data as the previous (smaller) phase. Therefore data locality is primarily determined by the last phase. The cost of migrating pages to

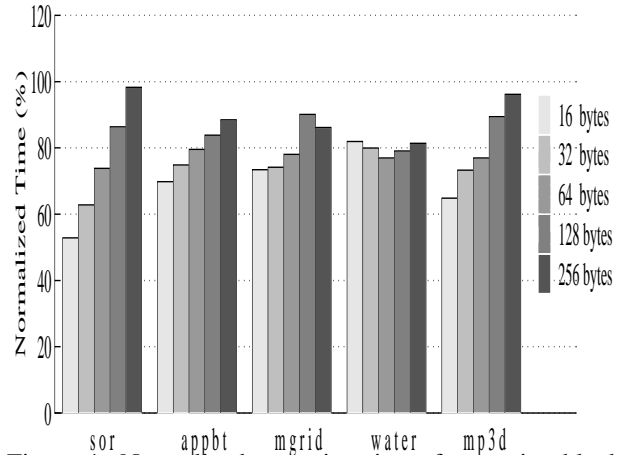


Figure 4: Normalized execution times for varying block sizes under hardware coherence.

local memory for the smaller phases, and migrating them again for larger phases, exceeds the cost of performing remote cache fills for the smaller phases.

We have also investigated several policies for replicating pages of data. These are:

- **Time policy:** if a page remains mapped for  $n$  cycles, copy it to local memory the next time it is mapped.
- **Counter policy:** if  $n$  cache fills are performed on a page before it is unmapped, copy it to local memory the next time it is mapped. This requires some hardware support.
- **Counter-interrupt policy:** if  $n$  cache fills have been performed on a page since it was mapped, copy it to local memory immediately. This also requires hardware support.

For our simulations, we selected several applications which we believed would be most likely to benefit from replication. For these applications, the policy which performed best was the counter policy. Figure 5 shows the relative performance of our applications with page replication. `SOR` is the only program for which we found a significant performance gain from replication (13%).

We believe that the failure of replication is a result of the sharing patterns exhibited by our applications. In particular, many replicated pages tended to be accessed very little before being written again by another processor, invalidating the copy. Even assuming high network and memory bandwidths (1 word per cycle), the high cost of replicating those pages caused performance degradation. Additionally, the reference patterns of some applications may contain frequent writes, which will not allow very many pages to be replicated. Replication may still be useful if it is limited to data structures that are mostly read, such as lookup tables

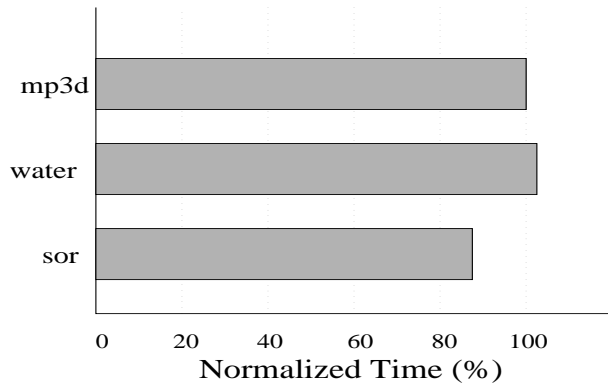


Figure 5: Execution times under software coherence with page replication, as a percentage of time with first-use placement only.

written only during initialization. We are considering the use of program annotations to identify such data.

## 5 Conclusions

We have studied the performance impact of simple behavior-driven page placement policies under both hardware and software cache coherence. We find that for applications whose working sets do not fit entirely in cache, dynamic page placement provides substantial performance benefits, by allowing capacity misses to be serviced from local memory, thus incurring reduced miss penalties. We have also shown that a very simple policy suffices to achieve good results and that complicated hardware is not required in devising an effective page placement strategy. Finally we have investigated the performance impact of dynamic page migration and page replication on cache coherent multiprocessors but found no performance benefits for our application suite. We believe that the reference pattern favoring replication is uncommon in scientific applications, and that dynamic placement suffices to improve the miss penalties of the applications that run on these machines.

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